



KNU PHYSICS SEMINAR

August 29 2022

**Exploring the 3D structure
of nucleon resonances
based on transition GPD
measurements at JLAB**

JUSTUS-LIEBIG-



**UNIVERSITÄT
GIESSEN**



Stefan Diehl

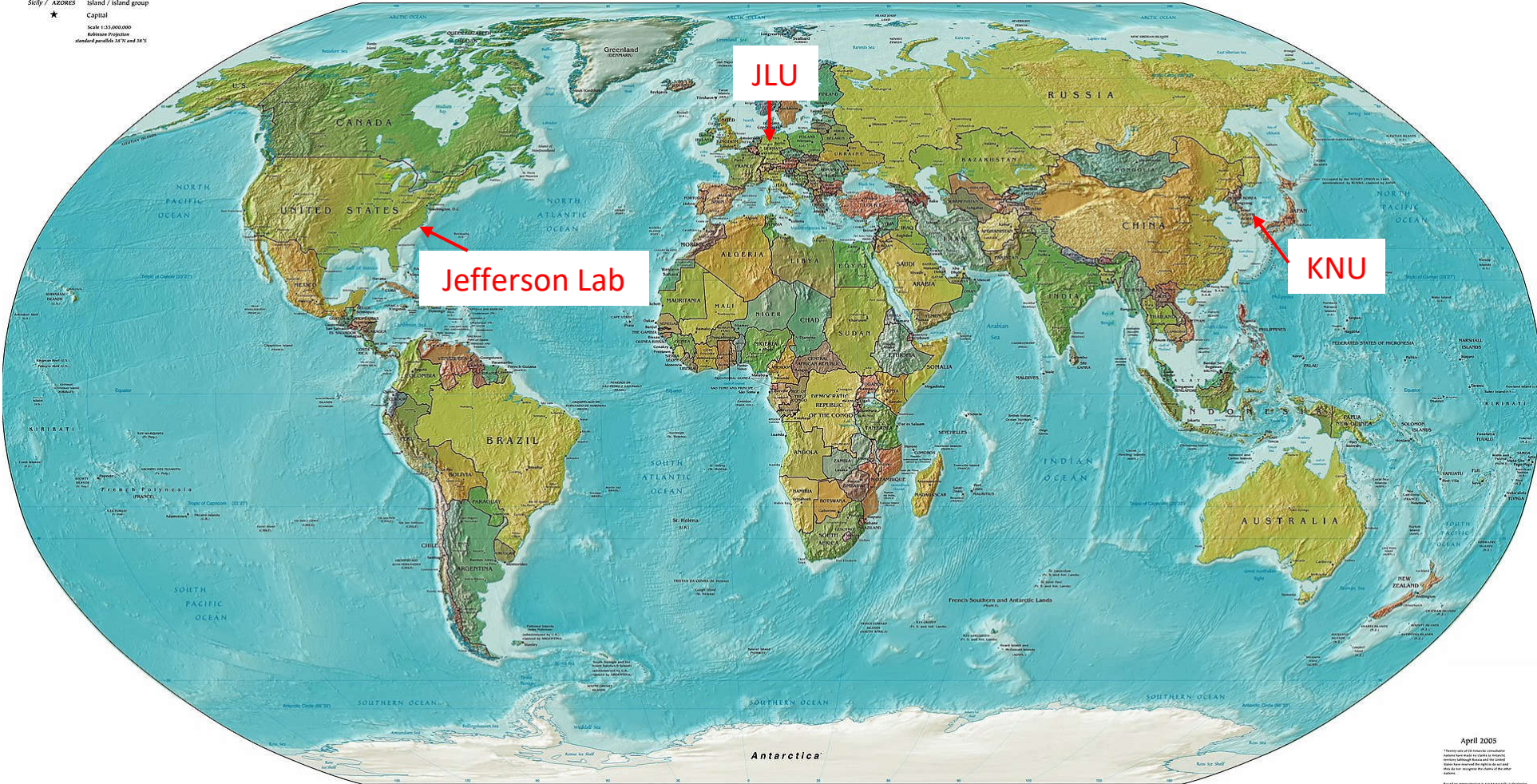
Justus Liebig University Giessen

University of Connecticut

08/29/2022

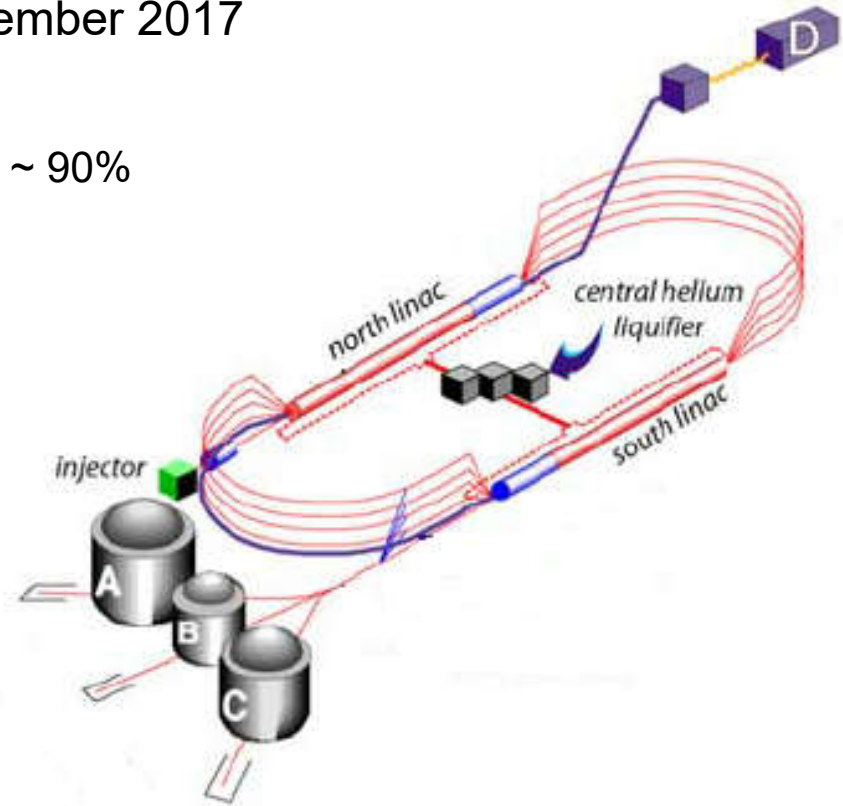
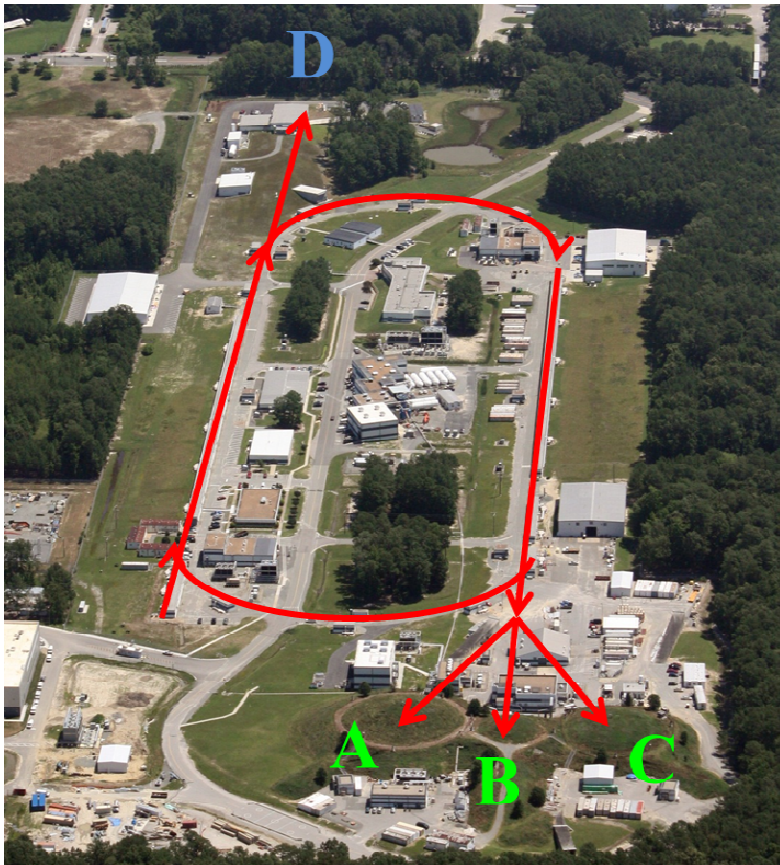
Thomas Jefferson National Accelerator Facility (JLAB)

Sicily / AZORES Island / island group
★ Capital
Scale 1:35,000,000
Robinson Projection
Standard parallels 45°N and 35°S



Thomas Jefferson National Accelerator Facility (JLAB)

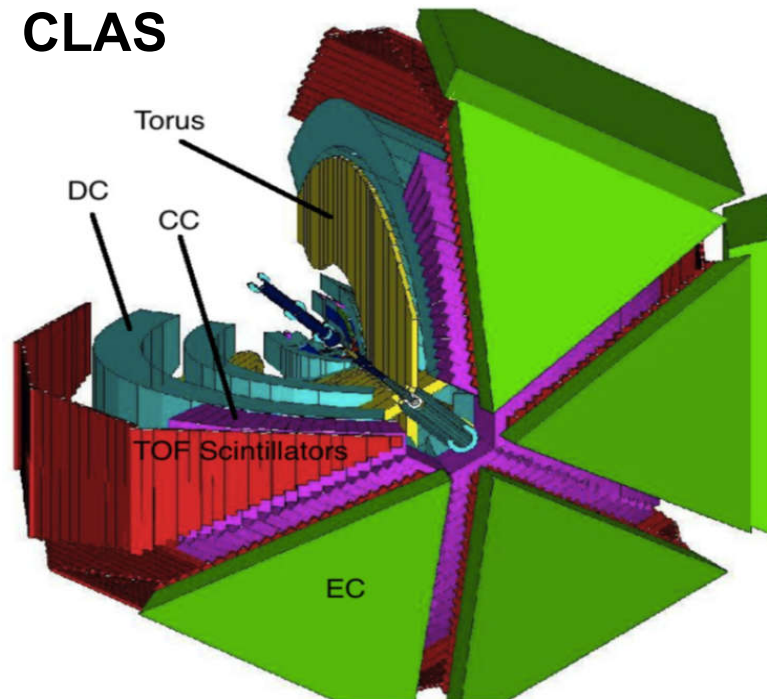
- CEBAF Upgrade completed in September 2017
 - electron beam
 - $E_{\max} = 12 \text{ GeV}$, $I_{\max} = 90 \text{ } \mu\text{A}$, $\text{Pol}_{\max} \sim 90\%$



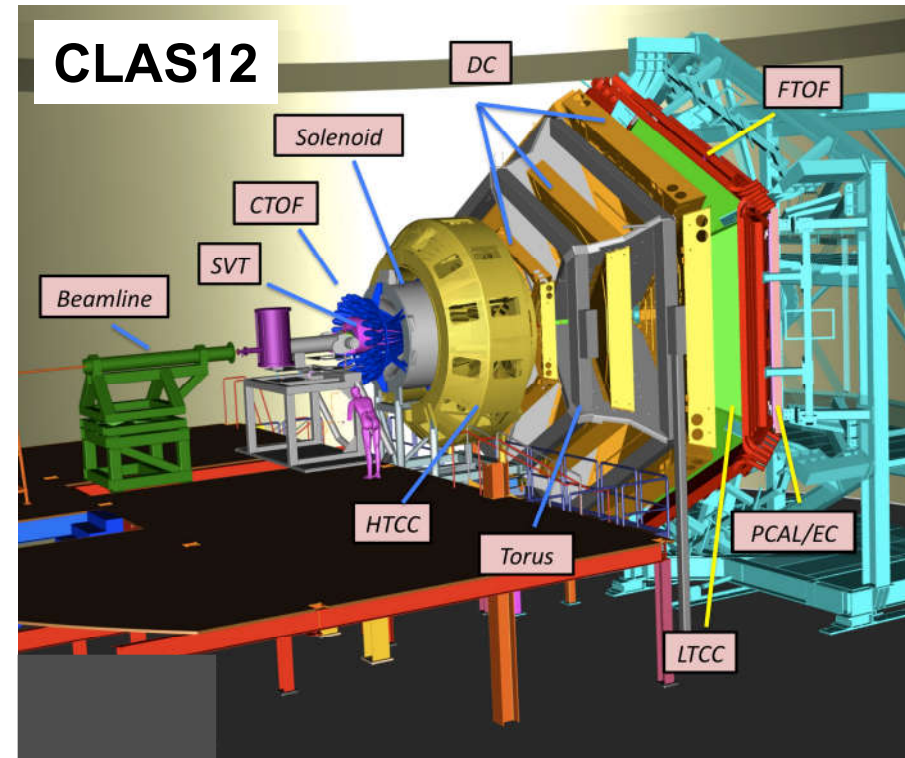
- 4 halls running simultaneously since January 2018

CLAS / CLAS12 in Hall B at JLAB

CLAS

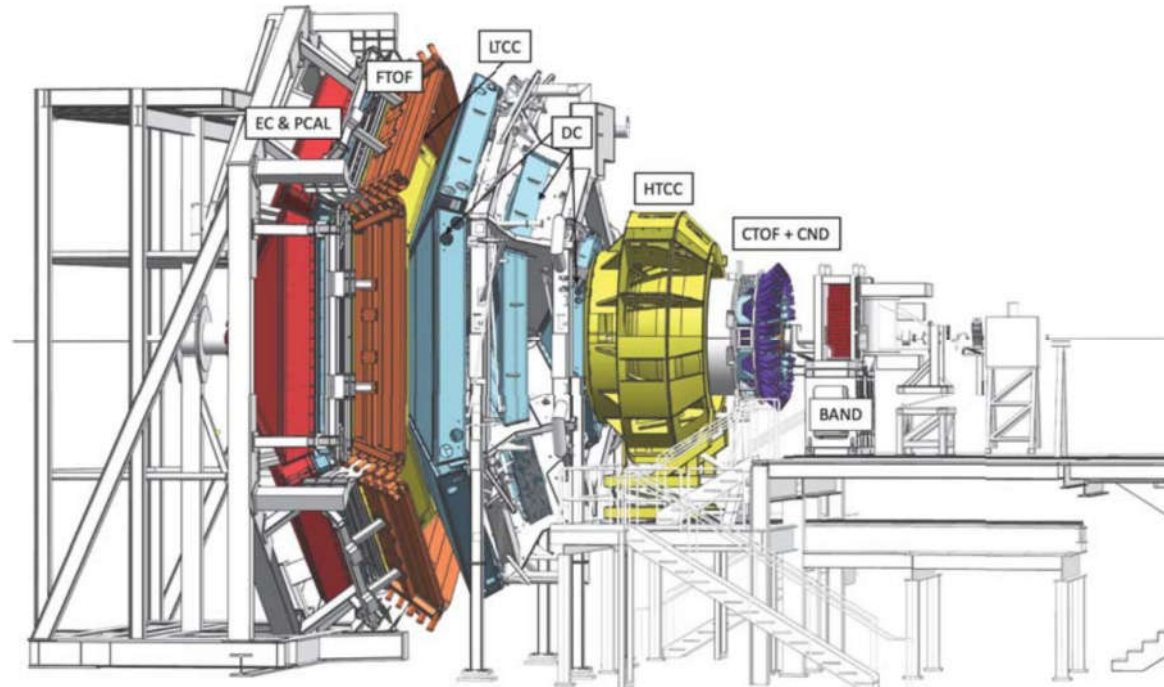


CLAS12



- ▶ $\mathcal{L} = 1 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$
- ▶ Inclusive electron trigger (all reactions will be analyzed in parallel)

CLAS12 Experimental Setup in Hall B at JLAB



V. Burkert et al., Nucl. Instrum. Meth.A 959 (2020) 163419

- Data of this talk was recorded with CLAS12 during fall 2018 and spring 2019
- 10.6 / 10.2 GeV e^- beam → ~87 % average polarization → liquid H_2 target
- Analysed data ~ 35 % of the approved RG-A beam time

QCD Science Questions

How are the quarks and gluons, and their intrinsic spins distributed in space & momentum inside the nucleon?

How can we recover the well-known characteristics of the nucleon from the properties of its **colored building blocks**?

Mass? Spin? Charge? ...

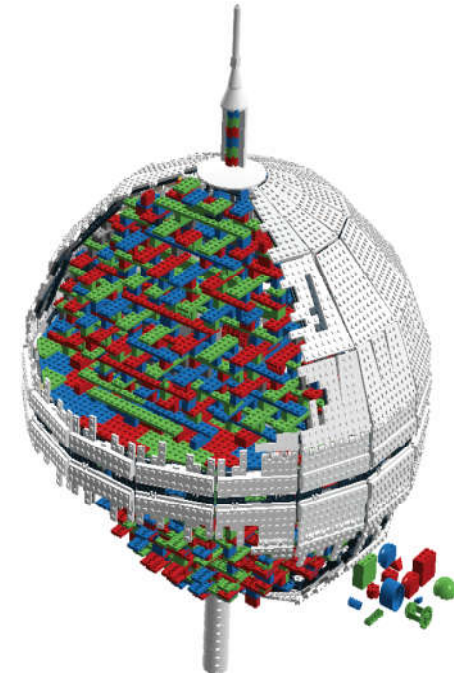
What are the relevant **effective degrees of freedom** and **effective interaction** at large distance?

What is the role of orbital angular motion?

Classical: $L \sim \mathbf{r} \times \mathbf{p}$

We need something three-dimensional!

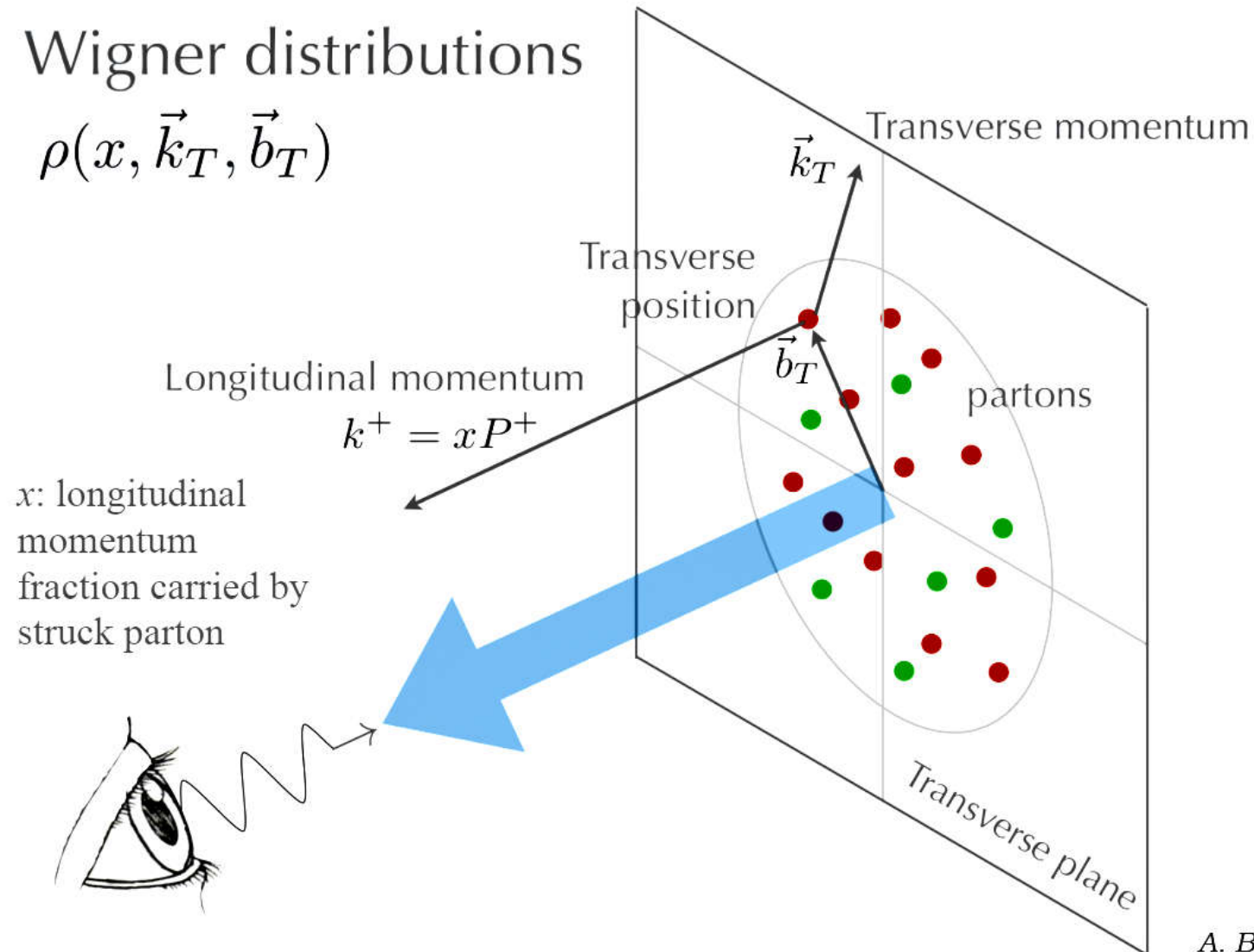
We need to investigate the 3D nucleon structure!



3-Dimensional Imaging of Quarks and Gluons

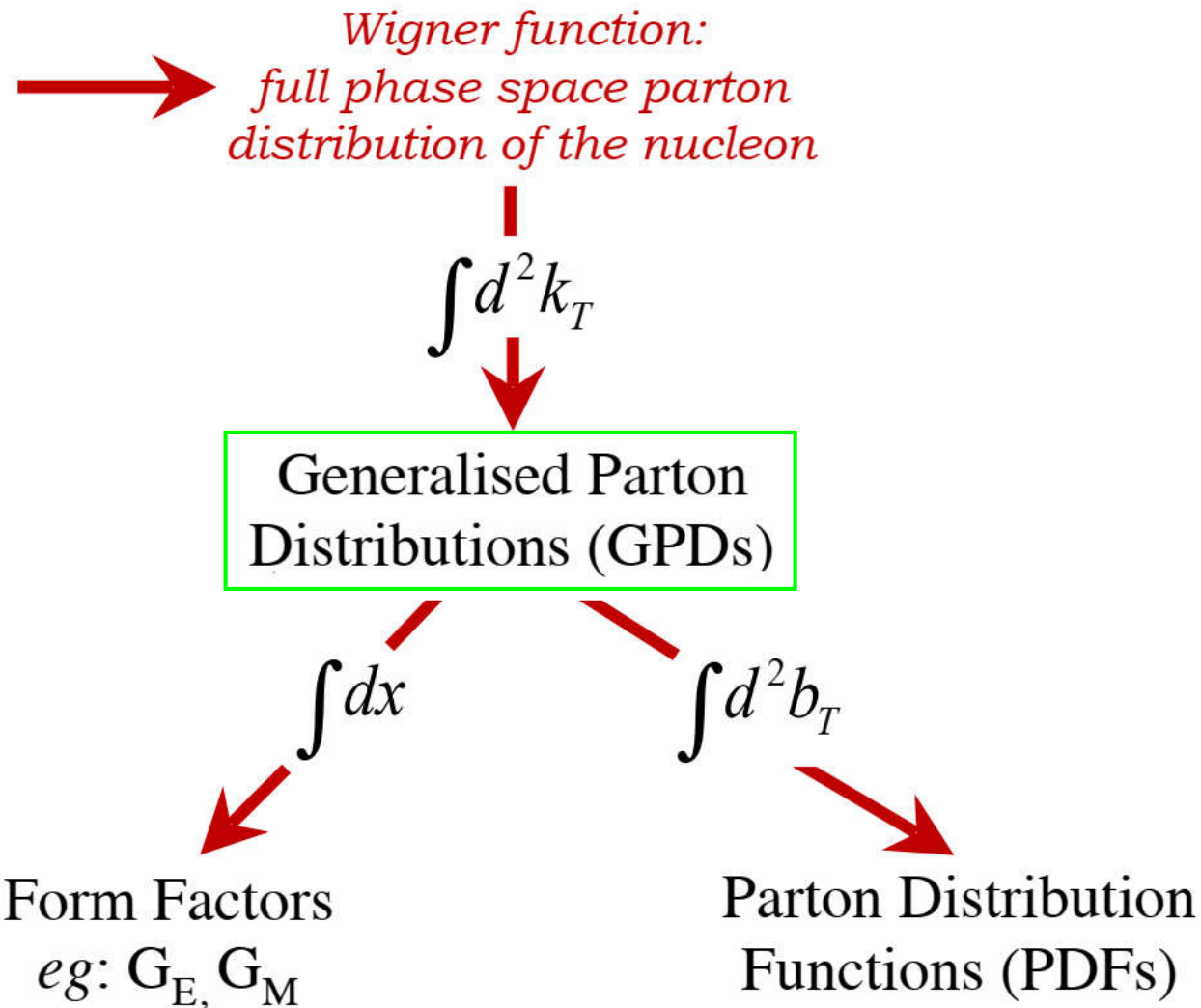
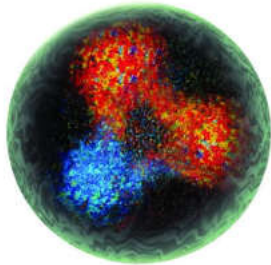
Wigner distributions

$$\rho(x, \vec{k}_T, \vec{b}_T)$$



A. Bacchetta

3-Dimensional Imaging of Quarks and Gluons



Generalized Parton Distributions (GPDs)

Generalized Parton Distributions
(GPD)



3-D nucleon images in the
transverse coordinate and
longitudinal momentum space

quark pol.

	N/q	U	L	T
U		H		\bar{E}_T
L			\tilde{H}	\tilde{E}_T
T		E	\tilde{E}	H_T, \tilde{H}_T

nucleon pol.

$$\bar{E}_T = 2\tilde{H}_T + E_T$$

4 chiral even GPDs

4 chiral odd GPDs

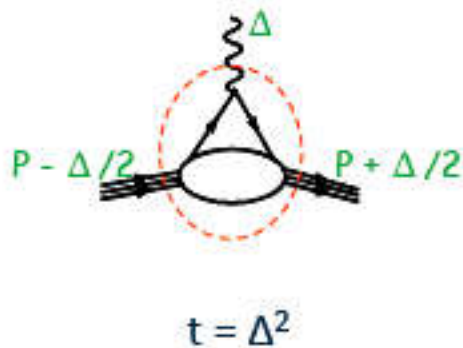
Interpretation of GPDs in the kinematic limits

→ in forward kinematics ($\xi=0, t=0$) : **PDF limit**

$$H^q(x, \xi = 0, t = 0) = q(x)$$

$$\xi \sim x_B / (2 - x_B)$$

→ first moments of GPDs : **elastic form factor limit**



$$\int_{-1}^{+1} dx H^q(x, \xi, t) = F_1^q(t) \rightarrow \text{Dirac FF}$$

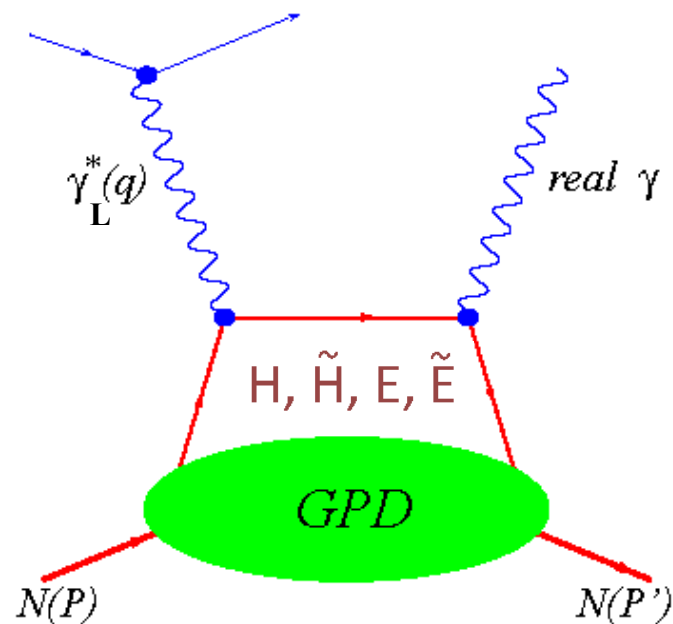
$$\int_{-1}^{+1} dx E^q(x, \xi, t) = F_2^q(t) \rightarrow \text{Pauli FF}$$

$$\int_{-1}^{+1} dx \tilde{H}^q(x, \xi, t) = G_A^q(t) \rightarrow \text{axial FF}$$

$$\int_{-1}^{+1} dx \tilde{E}^q(x, \xi, t) = G_P^q(t) \rightarrow \text{pseudoscalar FF}$$

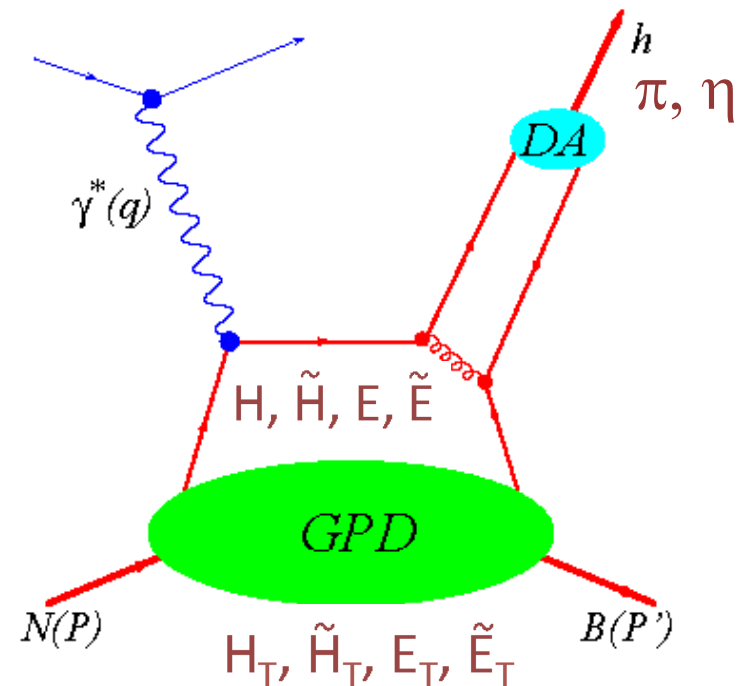
Study GPDs: Deeply Virtual Exclusive Processes

Deeply Virtual Compton Scattering (DVCS)



- + Clean process
- Only sensitive to chiral even GPDs

Deeply Virtual Meson Production (DVMP)



- + Enables Flavour decomposition of GPDs
- + Access to transversity degrees of freedom described by chiral-odd GPDs
- Distribution Amplitude (DA) is involved as additional soft non pert. quantity

Physics content of GPDs

- GPDs provide indirect access to mechanical properties of the nucleon (encoded in gravitational form factors of the energy-momentum tensor)

X. D. Ji, *PRD* **55**, 7114-7125 (1997)

M. Polyakov, *PLB* **555**, 57-62 (2016)

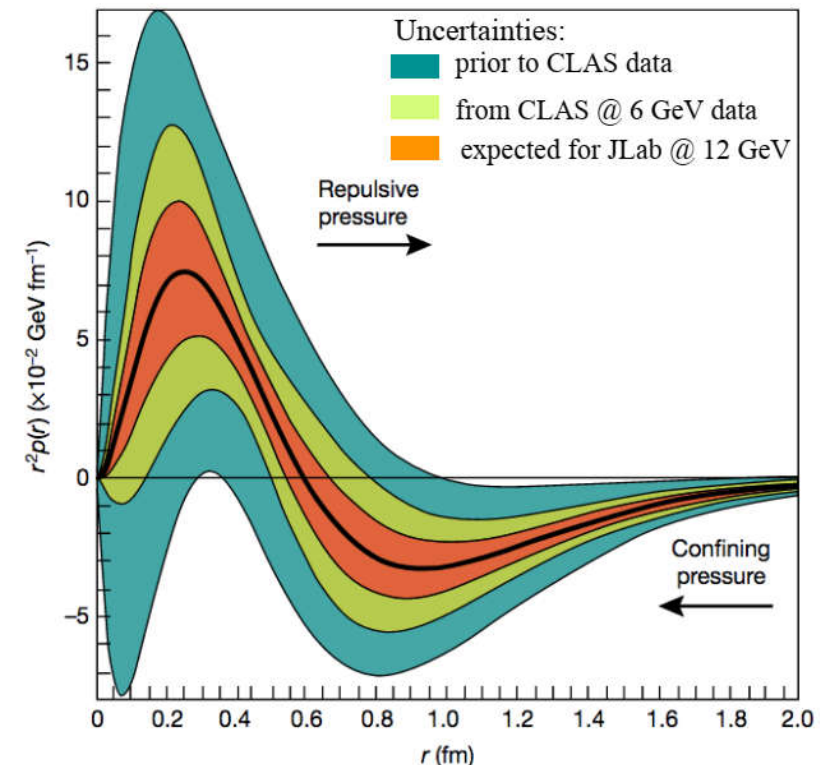
GFFs are related to GPDs via sum rules:

$$\int x [H(x, \xi, t) + E(x, \xi, t)] dx = 2J(t) \quad \text{angular momentum}$$

$$\int x H(x, \xi, t) dx = M_2(t) + \frac{4}{5} \xi^2 d_1(t)$$

mass
pressure and shear forces

→ Possibility to extract pressure distributions

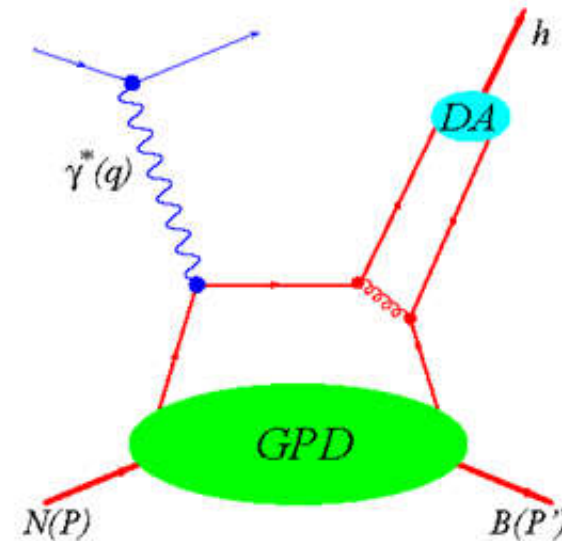


V. Burkert, L. Elouadrhiri, F.-X. Girod, *Nature* **557**, 396-399 (2018)

K. Kumerički, *Nature* **570**, E1-E2 (2019)

Physics content of DVMP results

	Meson	Flavor
$\mathcal{H}_T, \overline{\mathcal{E}}_T$	π^+	$\Delta u - \Delta d$
	π^0	$2\Delta u + \Delta d$
	η	$2\Delta u - \Delta d + 2\Delta s$
\mathcal{H}, \mathcal{E}	ρ^+	$u - d$
	ρ^0	$2u + d$
	ω	$2u - d$
	ϕ	g



$$\kappa_T^u = \int dx \bar{E}_T^u(x, \xi, t=0)$$

$$\kappa_T^d = \int dx \bar{E}_T^d(x, \xi, t=0)$$

\bar{E}_T is related to the protons
anomalous tensor magnetic moment

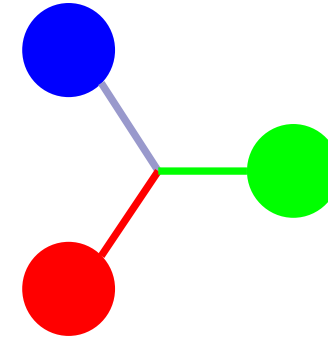
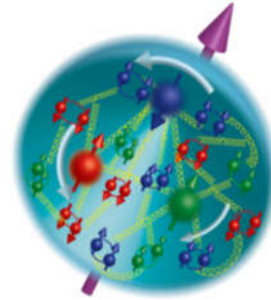
$$\delta_T^u = \int dx H_T^u(x, \xi, t=0)$$

$$\delta_T^d = \int dx H_T^d(x, \xi, t=0)$$

H_T is related to the protons tensor charge
→ Absolute magnitude of transversely polarized
valence quarks inside a transv. polarized nucleon

From the ground state nucleon to resonances

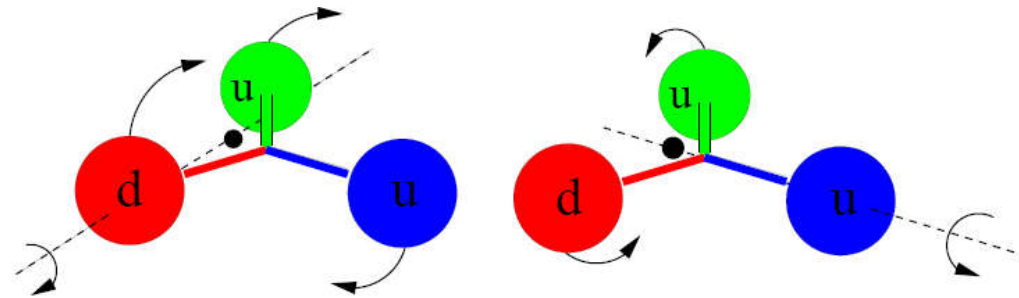
Ground state nucleon:
(proton, neutron)



Nucleon resonances:

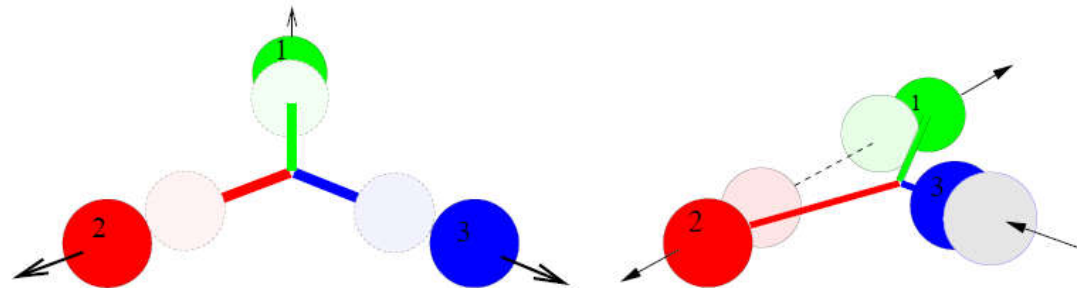
➤ Orbital excitations

i.e N(1535)



➤ Radial excitations

i.e N(1440)



From classical GPD to transition GPDs

Past: Extensive studies of transition form factors (**2D picture** of transv. position)

But: How does the excitation affect the **3D structure** of the Nucleon?

→ Pressure distributions, tensor charge, ... of resonances?

→ Information encoded in **transition GPDs**

→ More difficult theoretical description due to additional degrees of freedom

Simplest case: $N \rightarrow \Delta$ transition → **16 transition GPDs**

- 8 helicity non-flip transition GPDs (twist 2)
- 8 helicity flip transition GPDs

Transition GPDs in the twist-2 sector

N→Δ transition: 8 twist-2 helicity non-flip transition GPDs

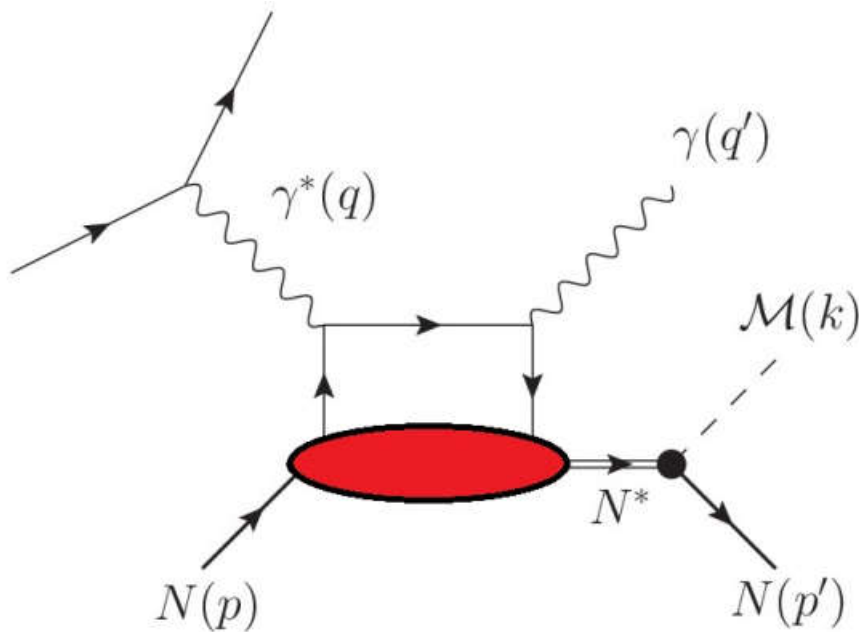
unpolarized:		polarized:	
$\int_{-1}^1 dx H_M(x; \xi; t) = 2G_M^*(t)$ $\int_{-1}^1 dx H_E(x; \xi; t) = 2G_E^*(t)$ $\int_{-1}^1 dx H_C(x; \xi; t) = 2G_C^*(t)$ $\int_{-1}^1 dx H_4(x; \xi; t) = 0$	Jones-Scardon EM FF for the N → transition	$\int_{-1}^1 dx C_1(x; \xi; t) = 2C_5^A(t)$ $\int_{-1}^1 dx C_2(x; \xi; t) = 2C_6^A(t)$ $\int_{-1}^1 dx C_3(x; \xi; t) = 2C_3^A(t)$ $\int_{-1}^1 dx C_4(x; \xi; t) = 2C_4^A(t)$	Adler form factors

- 3 of them are dominating in the large N_C limit
- Connection to proton-proton GPDs via symmetry considerations
- ➔ Description of leading twist effects / longitudinal virtual photons (σ_L)
- First theoretical works available

Experimental Access to Transition GPDs (twist 2)

Experimental access: Non diagonal DVCS process

$$\gamma^* p \rightarrow N^* \gamma \rightarrow N \text{ meson } \gamma$$



Two final states have been studied:

$$\gamma^* p \rightarrow N^* \gamma \rightarrow p \pi^0 \gamma \rightarrow p \gamma \gamma \gamma$$

$$\gamma^* p \rightarrow N^* \gamma \rightarrow n \pi^+ \gamma$$

factorisation for: $-t/Q^2$ small, x_B fixed

First Theoretical Description of the Δ Region

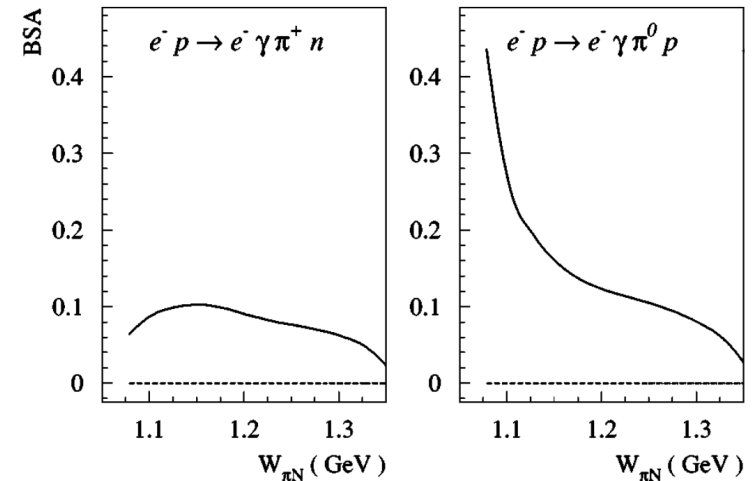
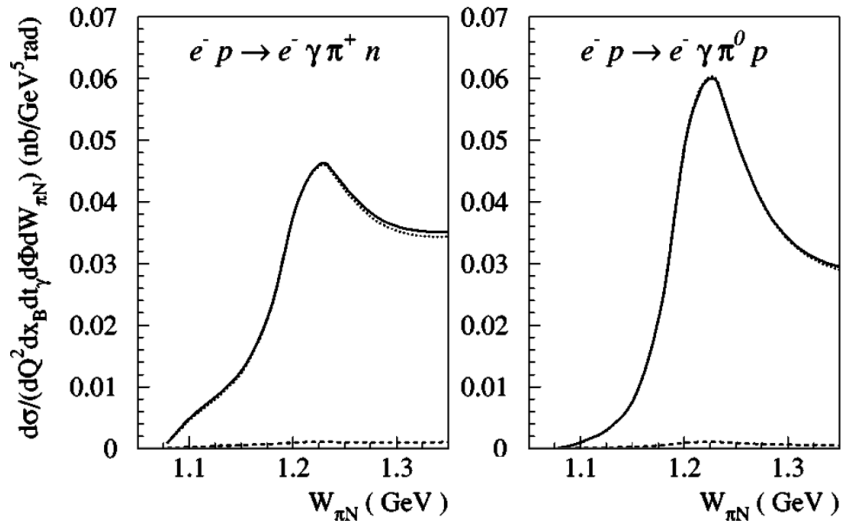
P.A.M Guichon, L. Mosse, M. Vanderhaeghen, Phys. Rev. D68 (2003) 034018

$E_e = 6 \text{ GeV}$

$Q^2 = 2.5 \text{ GeV}^2$

$x_B = 0.3$

$t_\gamma = -0.5 \text{ GeV}^2$

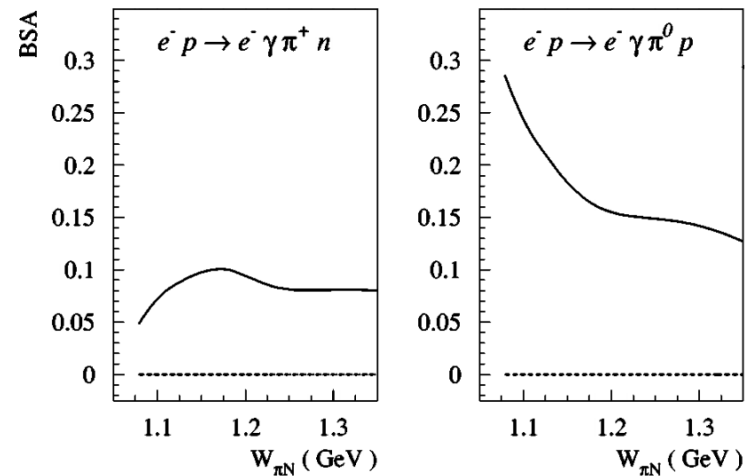
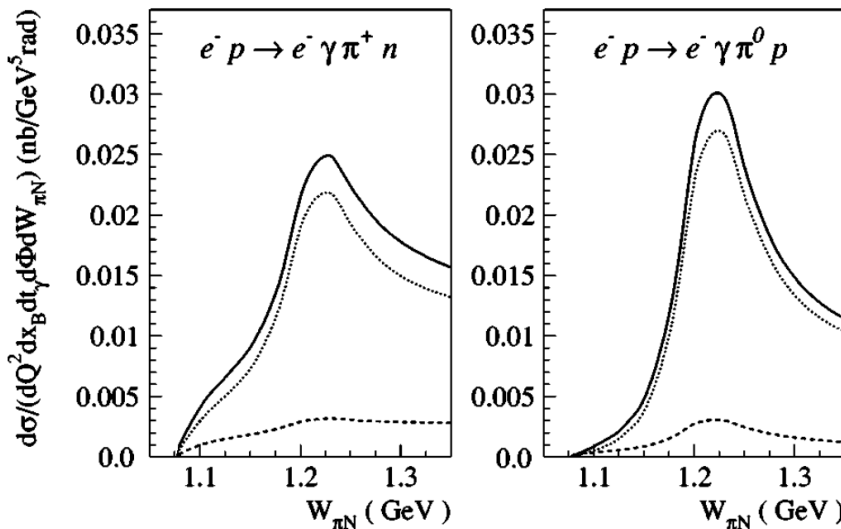


$E_e = 27 \text{ GeV}$

$Q^2 = 2.5 \text{ GeV}^2$

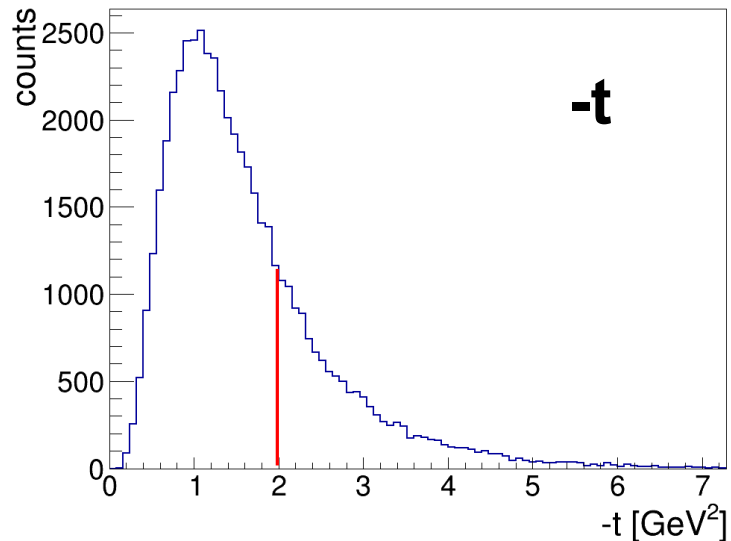
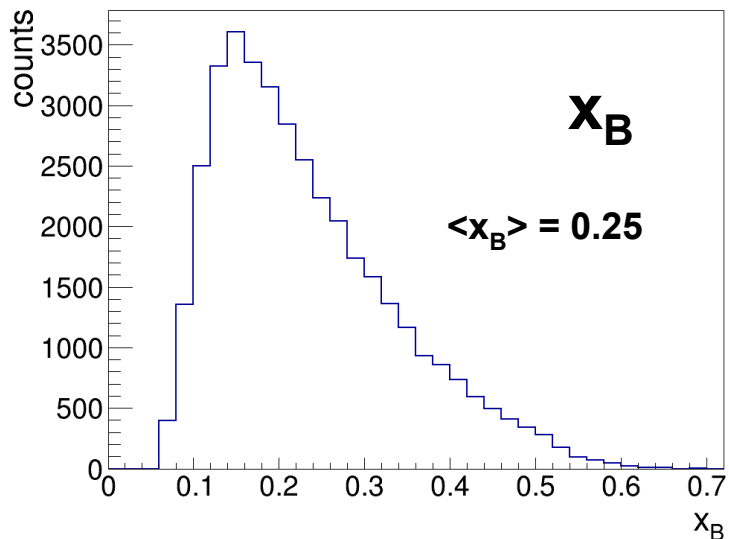
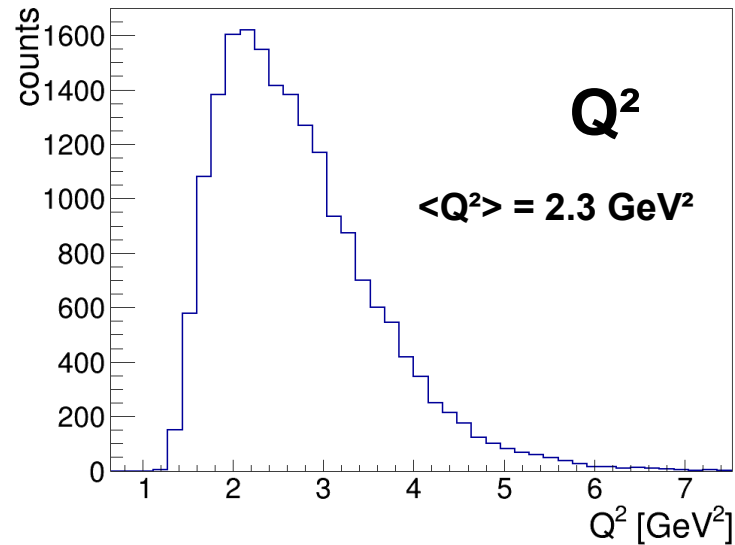
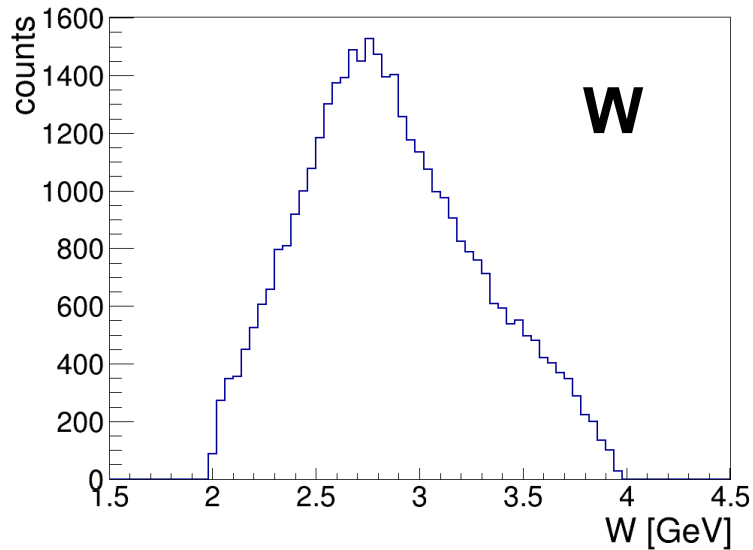
$x_B = 0.15$

$t_\gamma = -0.25 \text{ GeV}^2$



--- Δ -DVCS BH

Accessible Kinematic Region with CLAS12 (10.6 GeV)



exclusivity cuts
were applied
for event
selection

Kinematic cuts:

$$W > 2 \text{ GeV}$$

$$Q^2 > 1 \text{ GeV}^2$$

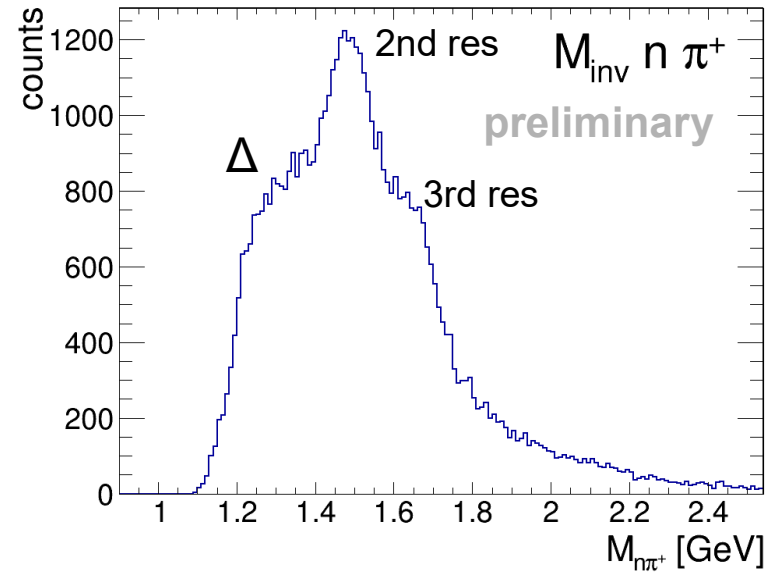
$$y < 0.8$$

$$-t < 2 \text{ GeV}^2$$

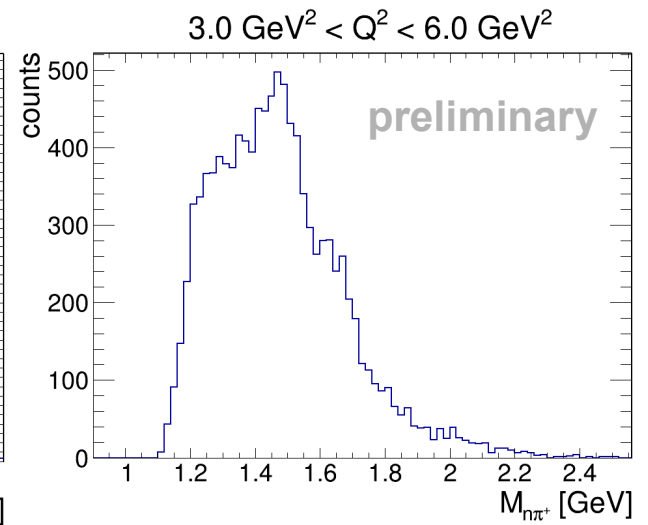
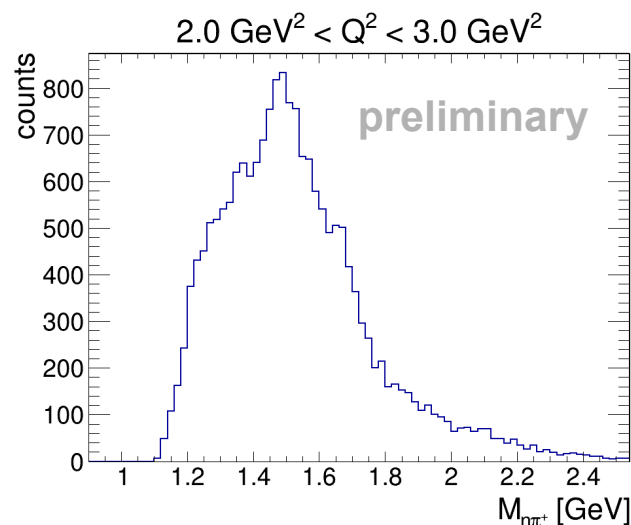
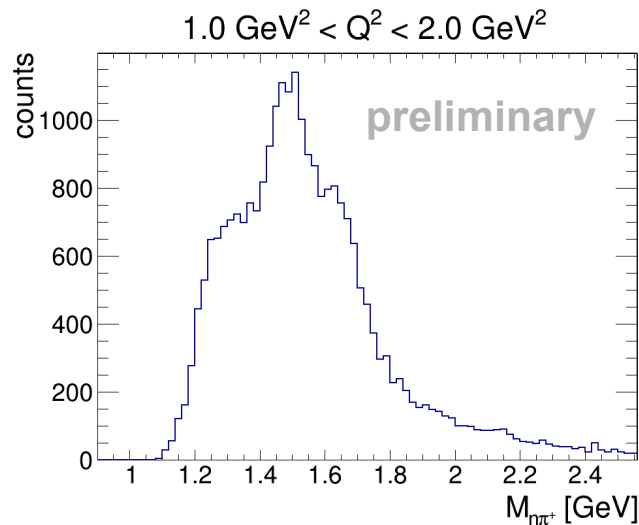
$$E_{\text{DVCS}} > 2 \text{ GeV}$$

Resonance Mass Spectrum for $N^* \rightarrow n\pi^+$

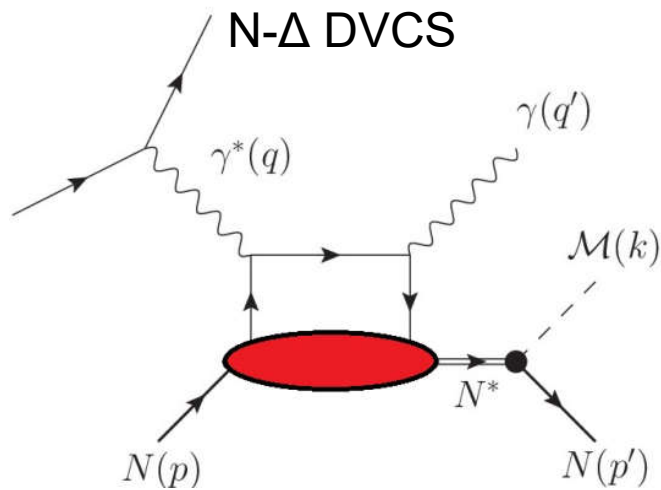
$e n \pi^+ \gamma$



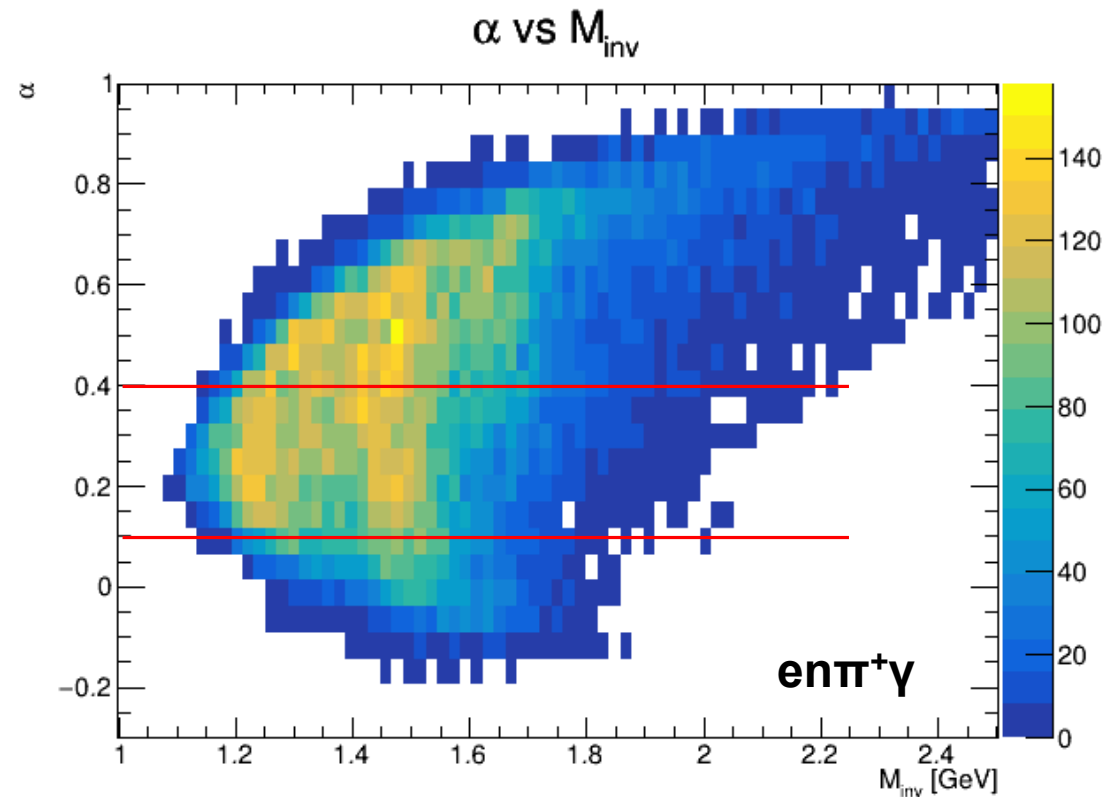
preliminary



The Pion Longitudinal Momentum Fraction



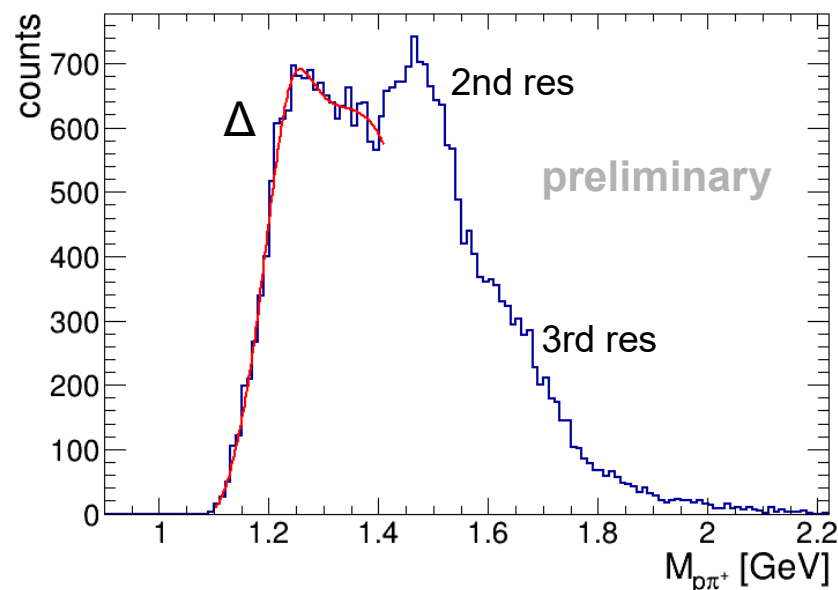
$$\alpha = \frac{(p'+k) \cdot k}{(p'+k)^2}$$



preliminary

Resonance Mass Spectrum for $0.1 < \alpha < 0.4$

$e n \pi^+ \gamma$



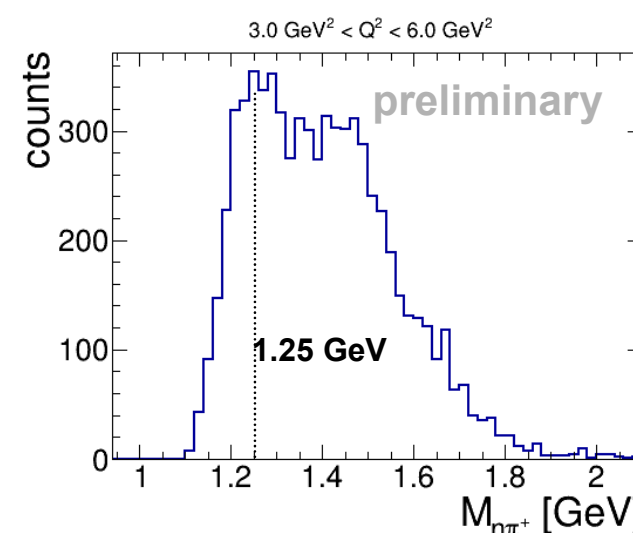
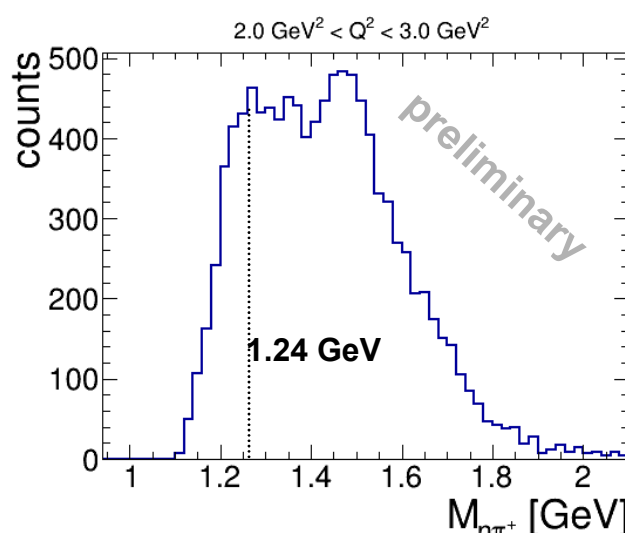
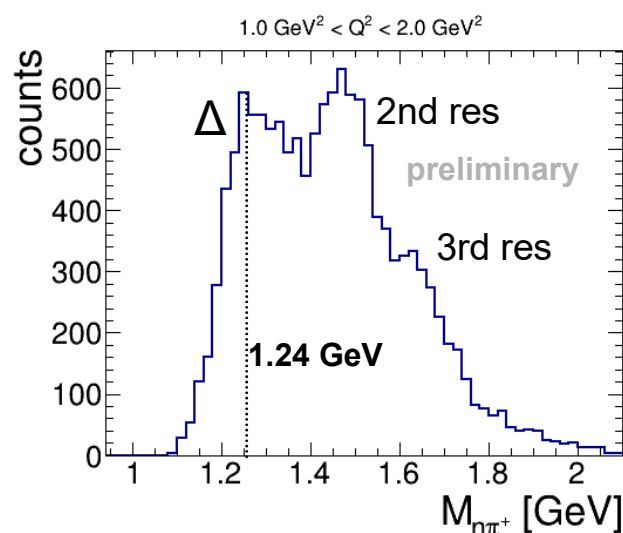
preliminary

Δ -fit: Breit-Wigner
+ polyn. backgr.

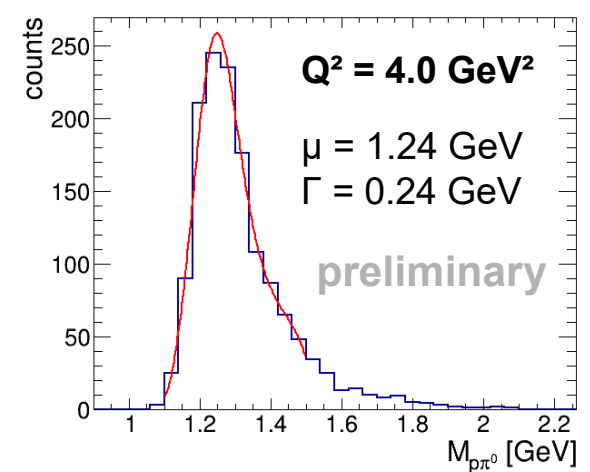
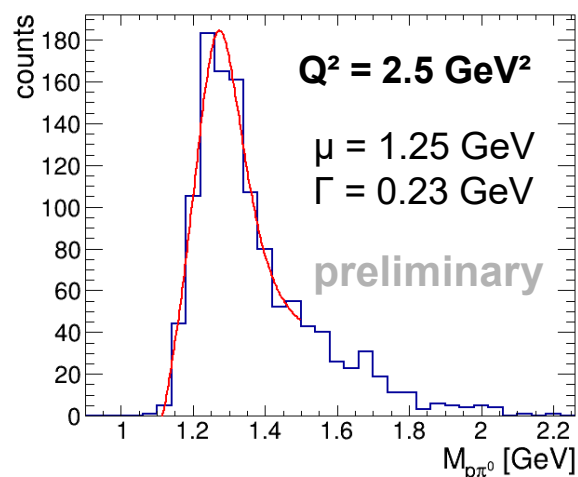
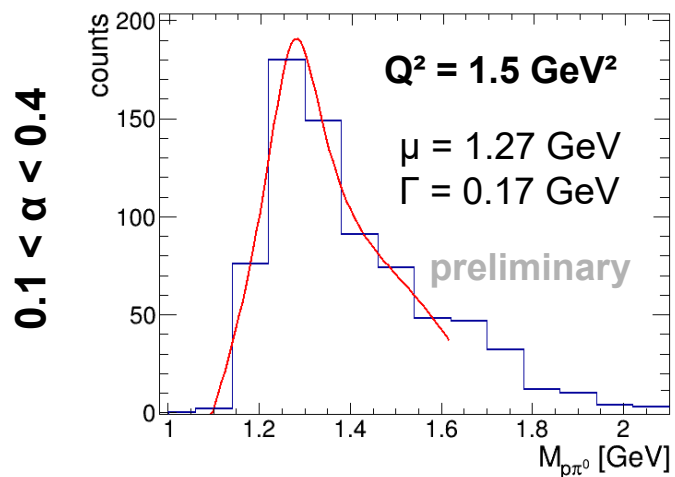
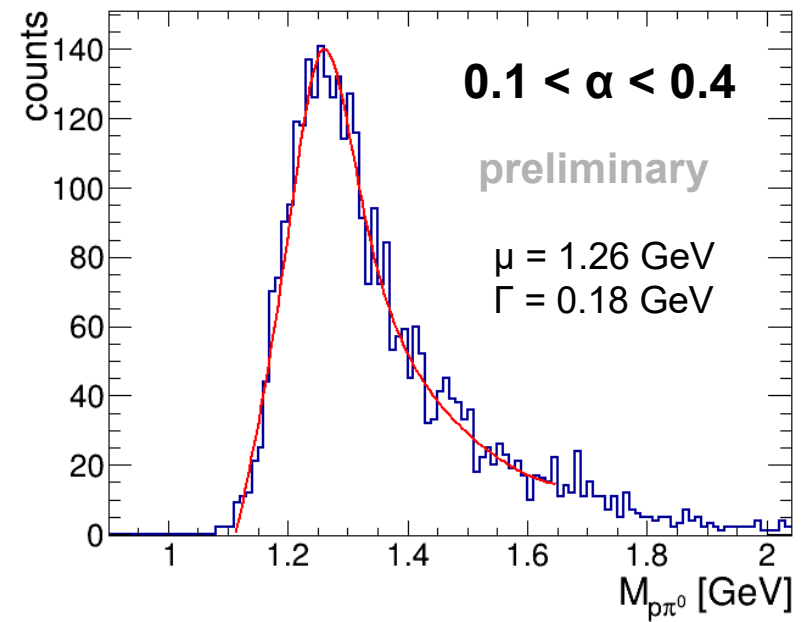
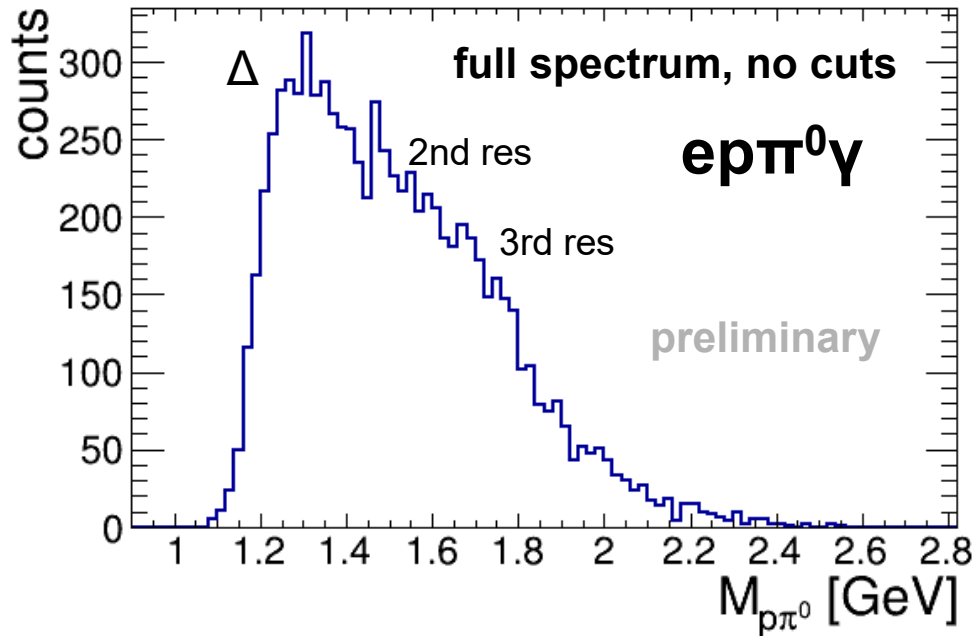
$$\mu = 1.235 \text{ GeV}$$

$$\Gamma = 0.15 \text{ GeV}$$

Q^2 dependence:

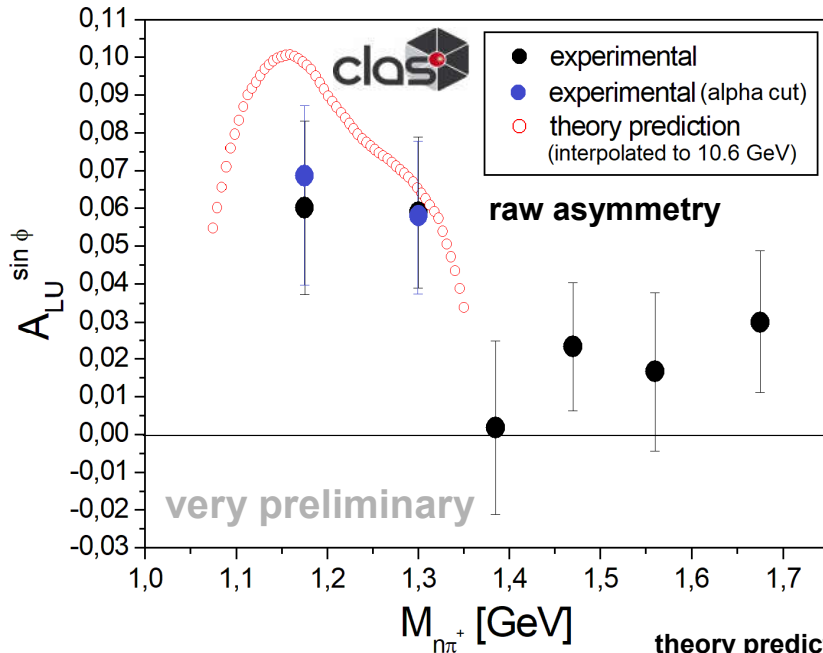
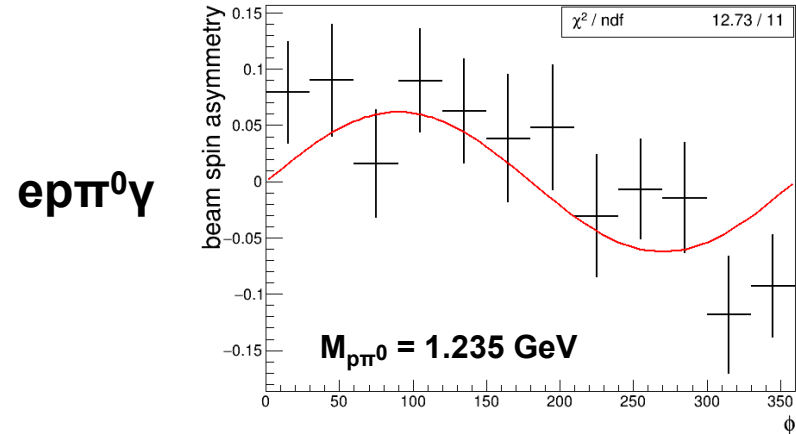
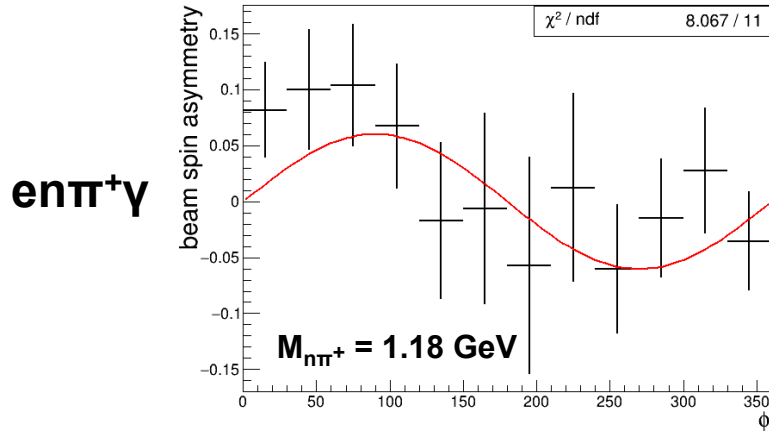


Resonance Mass Spectrum for $N^* \rightarrow p\pi^0$

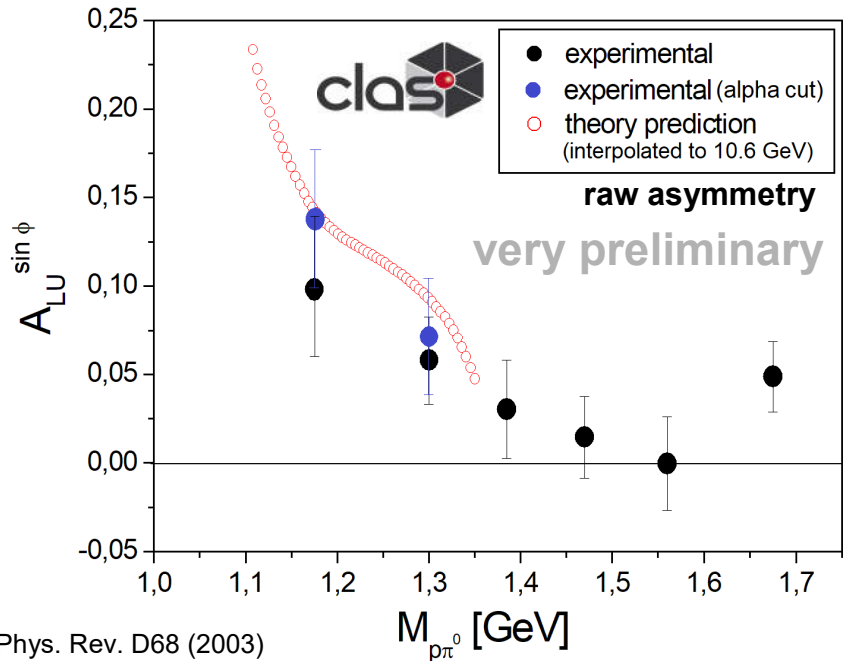


Raw beam spin asymmetries

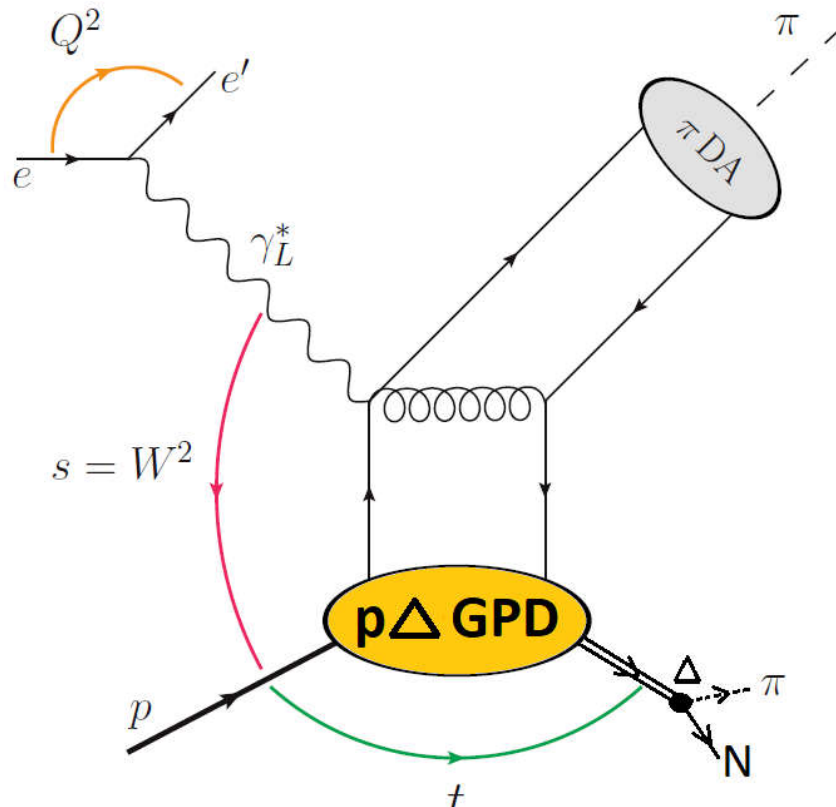
$$A = \frac{1}{P} \frac{N^+ - N^-}{N^+ + N^-} \approx A_{LU}^{\sin \phi} \sin \phi$$



theory prediction: Phys. Rev. D68 (2003)



The non-diagonal DVMP processes



$$ep \rightarrow e\Delta^0\pi^+ \rightarrow e(p\pi^-)\pi^+$$

$$ep \rightarrow e\Delta^0\pi^+ \rightarrow e(n\pi^0)\pi^+$$

$$ep \rightarrow e\Delta^+\pi^0 \rightarrow e(n\pi^+)\pi^0$$

$$ep \rightarrow e\Delta^+\pi^0 \rightarrow e(p\pi^0)\pi^0$$

$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow ep\pi^+\pi^-$$

8 helicity non-flip trans. GPDs

+

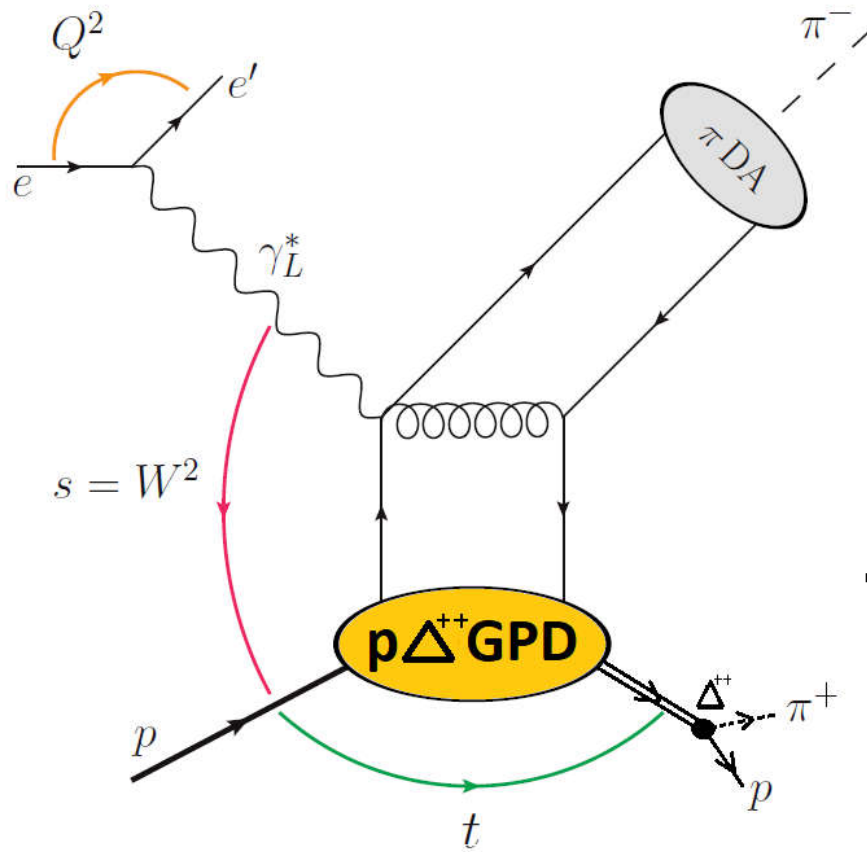
8 helicity flip trans. GPDs

→ Needed for twist-3 sector

→ No publications so far

Hard exclusive $\pi^-\Delta^{++}$ production

$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow ep\pi^+\pi^-$$



Factorisation expected for:

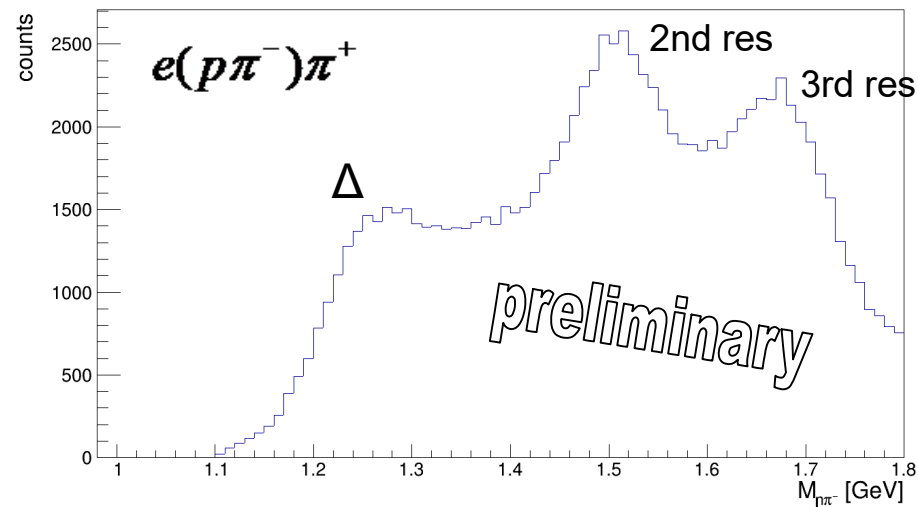
$$-t / Q^2 \ll 1 \quad \text{and} \quad Q^2 > M_\Delta^2$$

x_B fixed

→ Non-diagonal π^\pm production is expected to be especially sensitive to the tensor charge of the resonance

Why is $\pi^-\Delta^{++}$ special?

Other non - diagonal DVMP channels, i.e. $ep \rightarrow e\Delta^0\pi^+ \rightarrow e(p\pi^-)\pi^+$



$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow e\underbrace{p\pi^+}_{I_z = +3/2}\pi^-$$

→ The $p\pi^+$ final state can **only** be populated by **Δ -resonances**

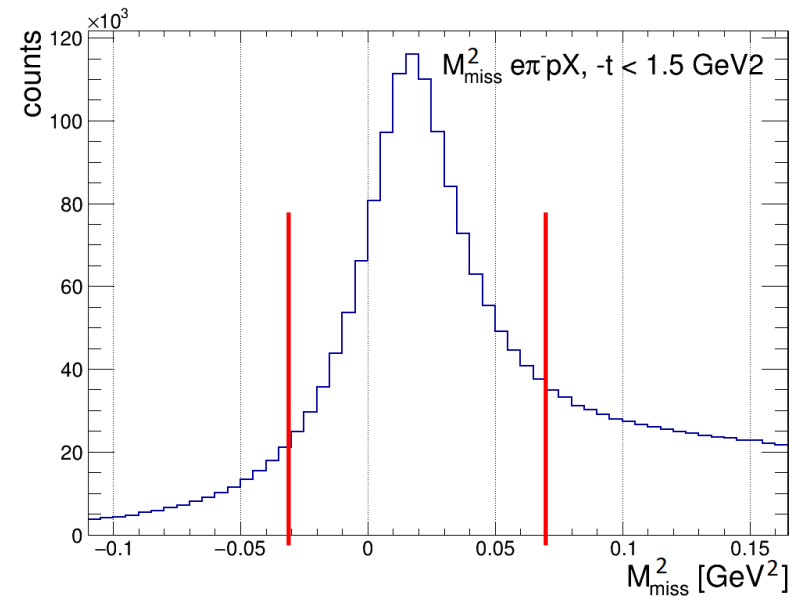
→ Large gap between $\Delta(1232)$ and higher resonances

Event Selection and Kinematic Cuts

$$ep \rightarrow e\Delta^{++}\pi^{-} \rightarrow ep\pi^{-}X$$

$$X = \pi^{+}$$

→ 2 σ cut around the missing π^{+}

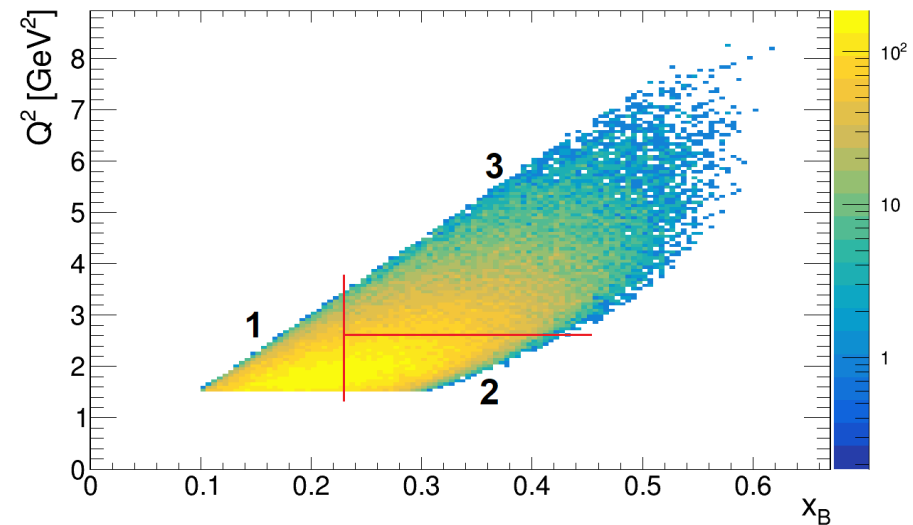


Kinematic cuts:

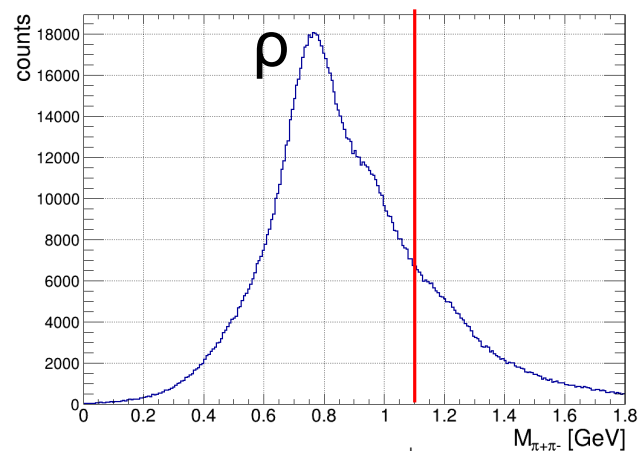
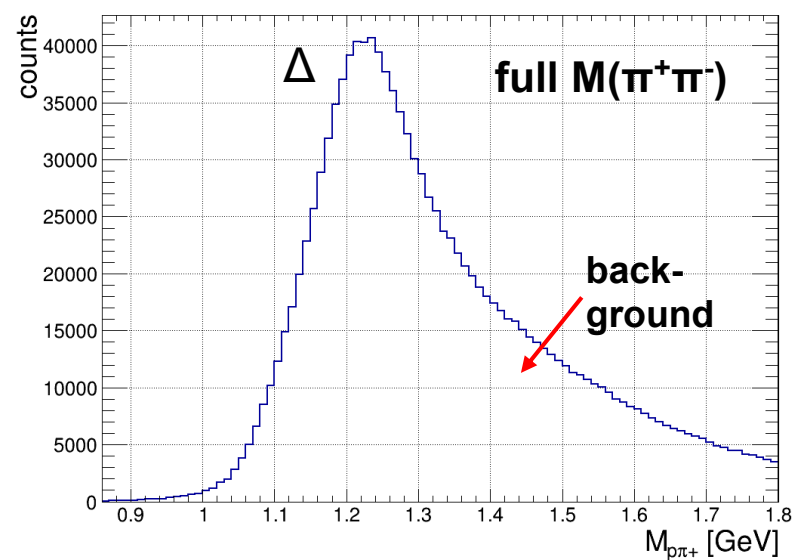
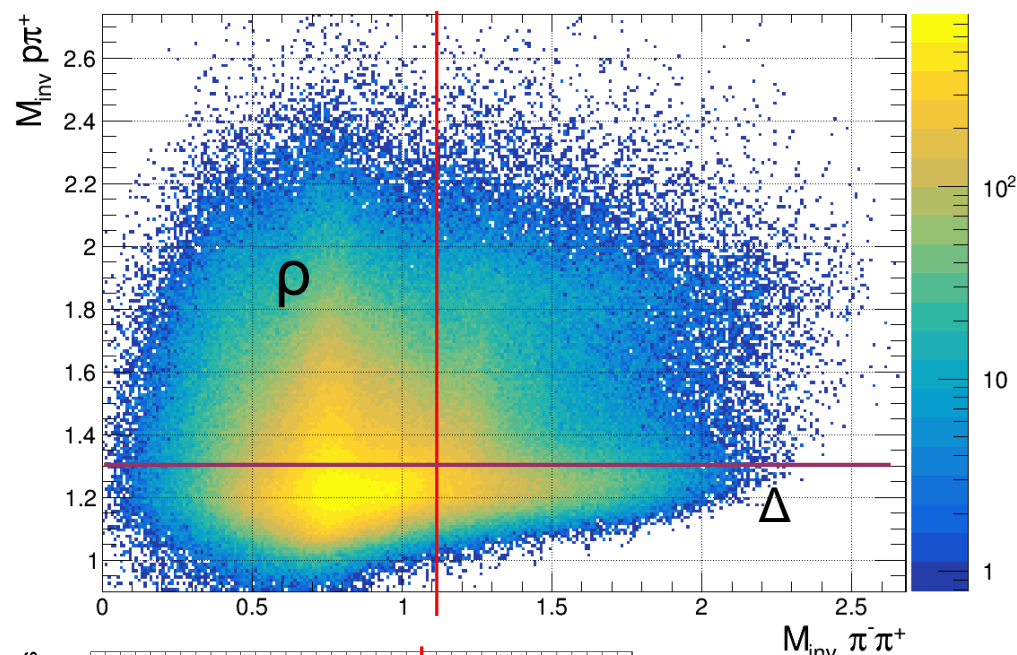
$$Q^2 > 1.5 \text{ GeV}^2 \quad W > 2 \text{ GeV}$$

$$y < 0.75$$

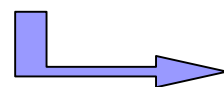
$$-t < 1.5 \text{ GeV}^2 \text{ (forward region)}$$



Event Selection and Background Rejection



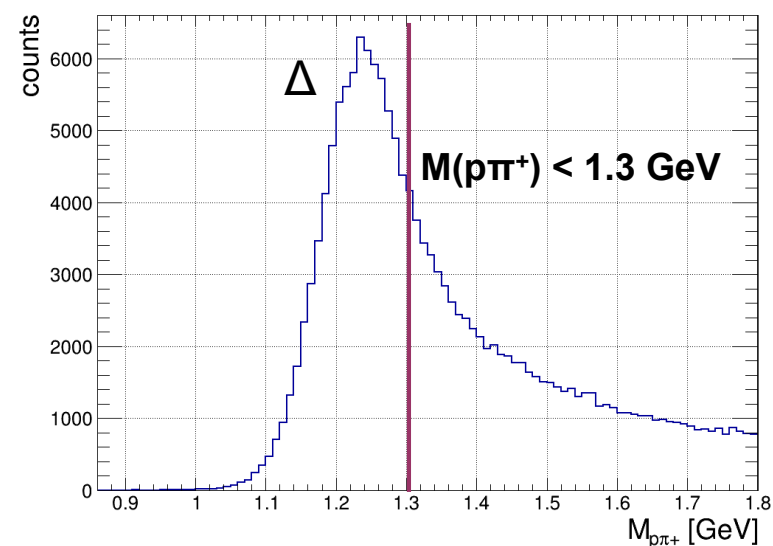
$M(\pi^+ \pi^-) > 1.1 \text{ GeV}$



ρ contamination

$< 0.8 \%$

$ep \rightarrow ep\rho \rightarrow ep\pi^+ \pi^-$



$M(p \pi^+) < 1.3 \text{ GeV}$

Monte Carlo Simulations

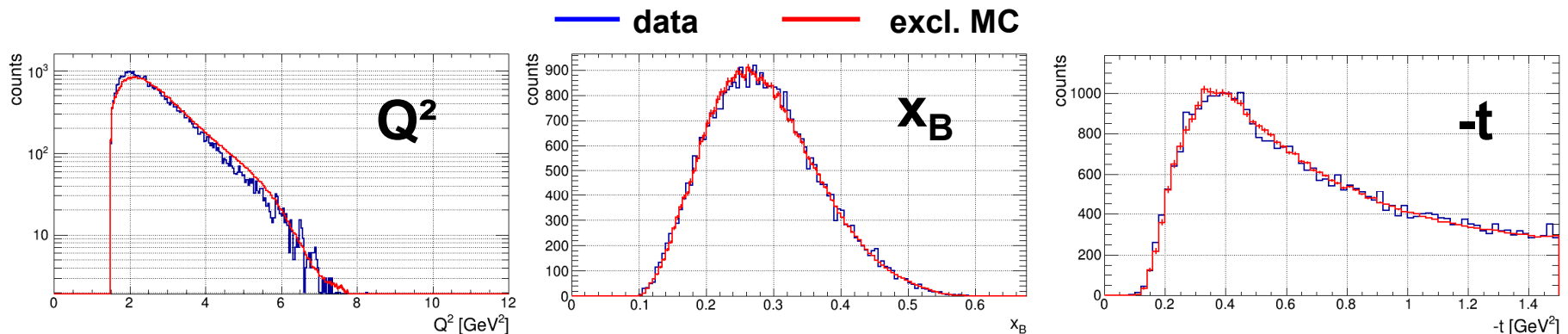
2 MC samples have been used:

a) Semi-inclusive DIS MC

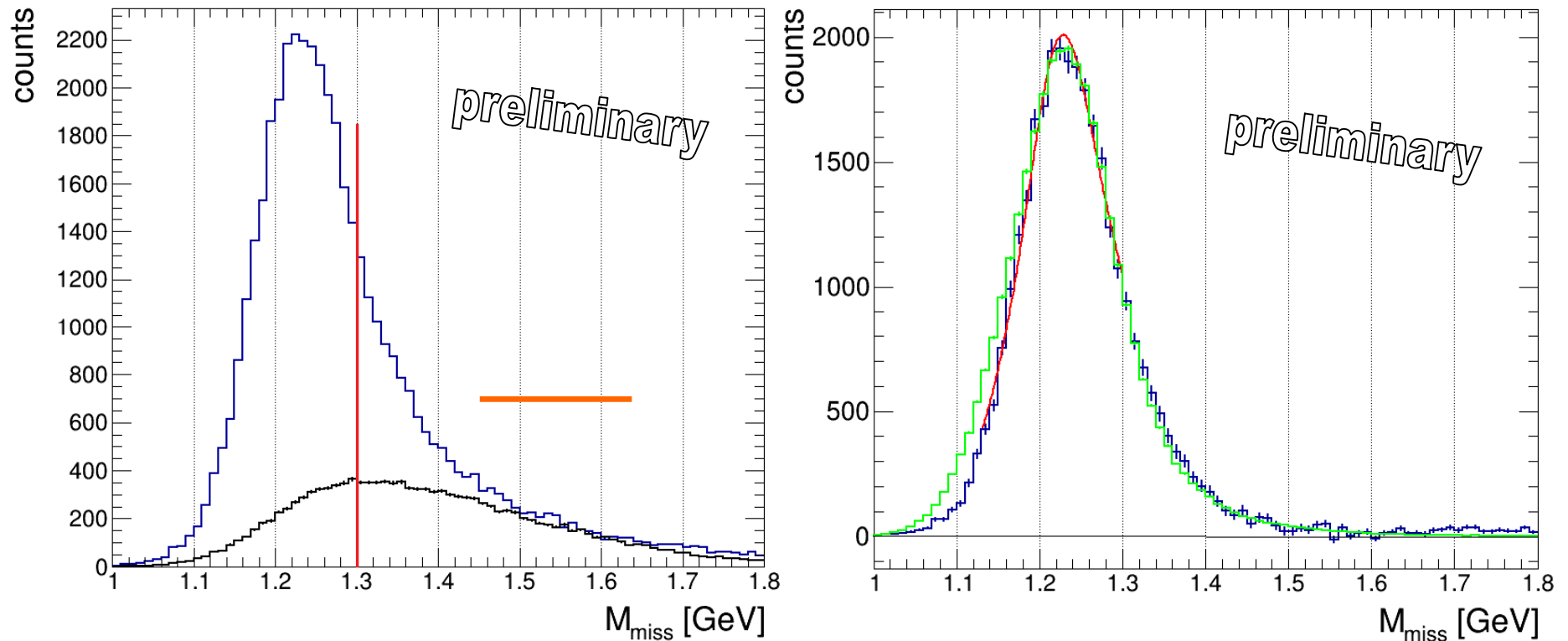
- Does not contain the $\pi\Delta^{++}$ production in „forward“ kinematics
- Contains nonres. background as well as ρ production and other potential BG channels
- Used to estimate background shape and contaminations

b) Exclusive $\pi\Delta^{++}$ MC

- Phase space simulation with a weight added to match experimental data
- Δ peak with PDG mass and FWHM
- Both MCs are processed through the full simulation and reconstruction chain



Event Selection and Background Estimate



— experimental data

— SIDIS MC (same cuts)

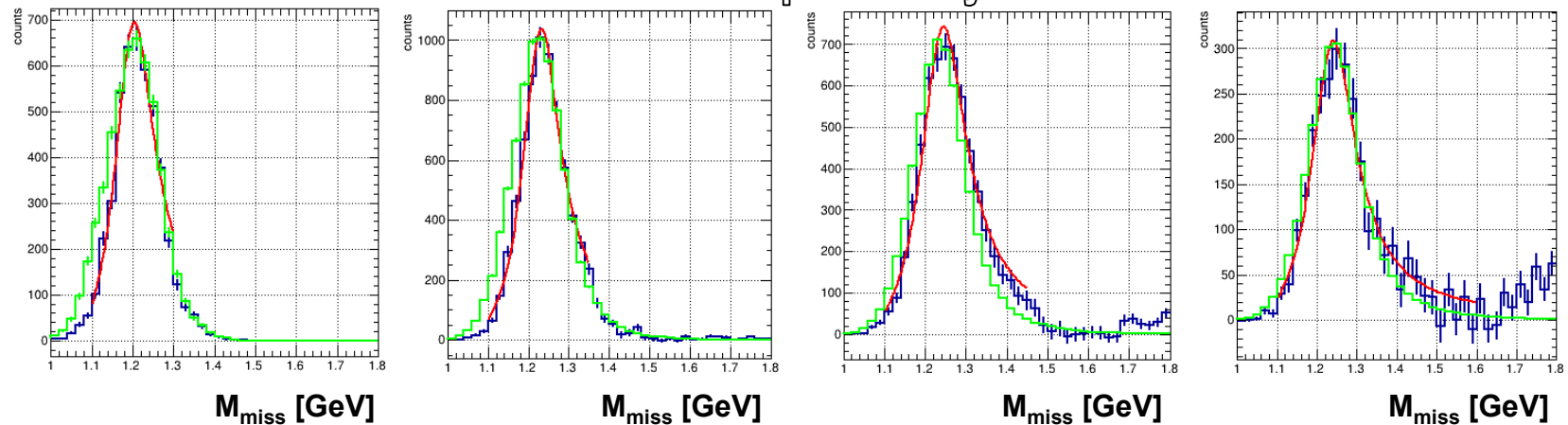
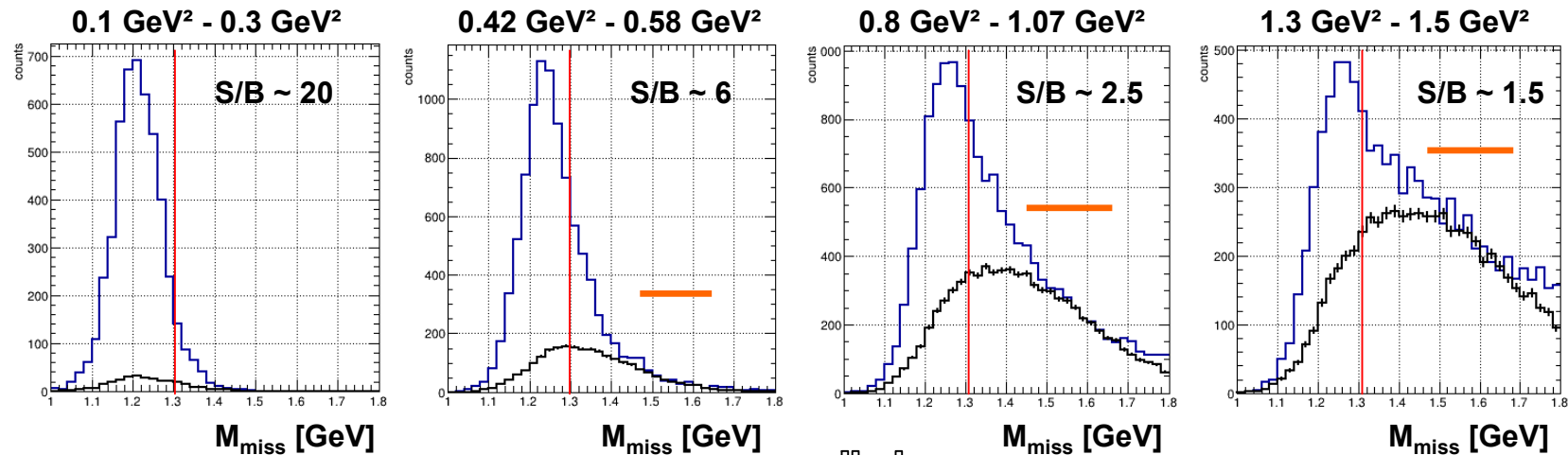
— data after SIDIS MC subtraction

— fit of a Sill function (BW with thr. effects)

— exclusive MC (for comparison)

Background: 98 – 99 % non-resonant events

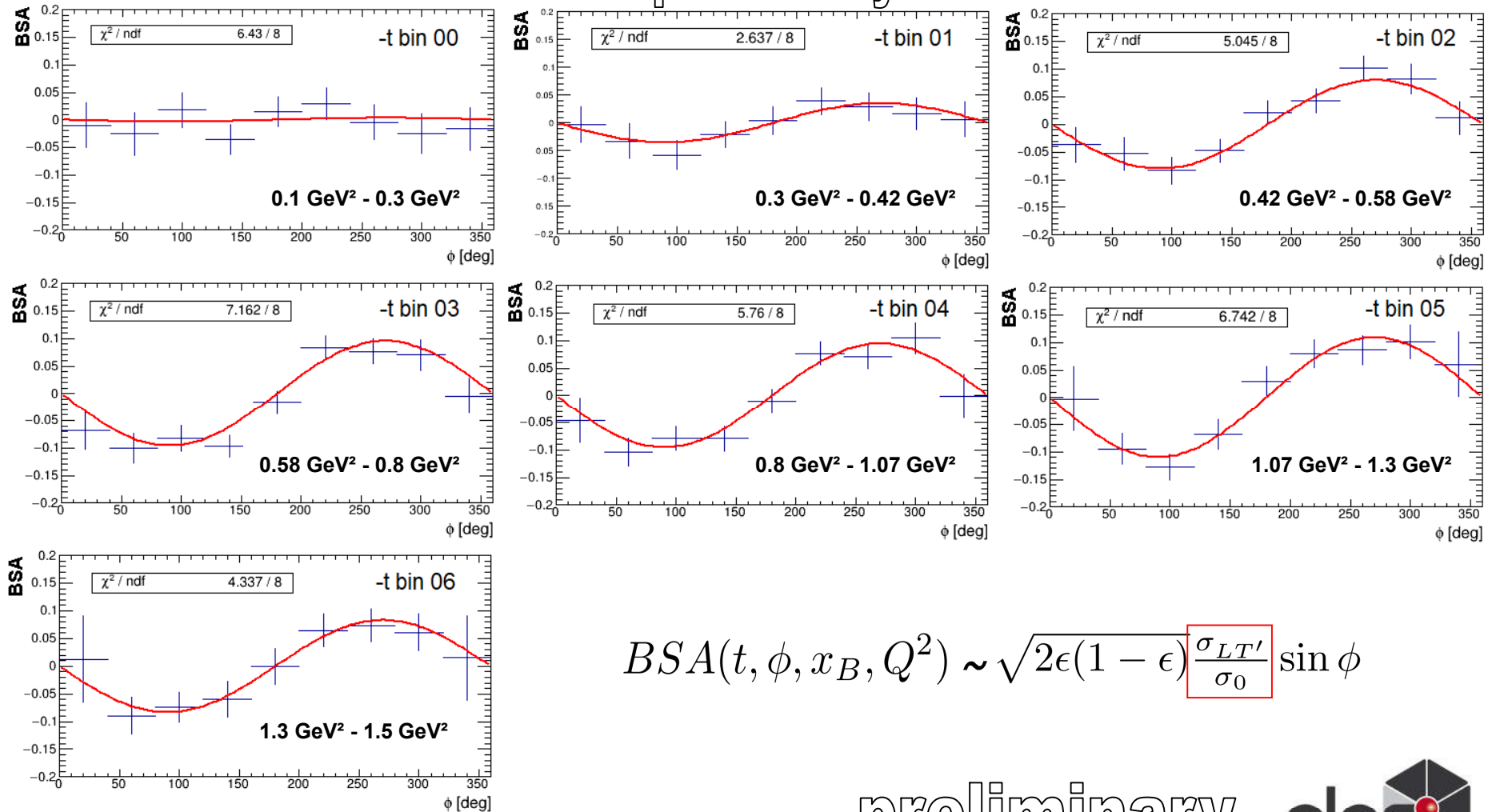
Event Selection and Background Estimate



- experimental data
- SIDIS MC (same cuts)
- data after SIDIS MC subtraction
- fit of a Sill function (BW with thr. effects)
- exclusive MC (for comparison)

Resulting Beam Spin Asymmetries (Q^2 - x_B integrated)

preliminary



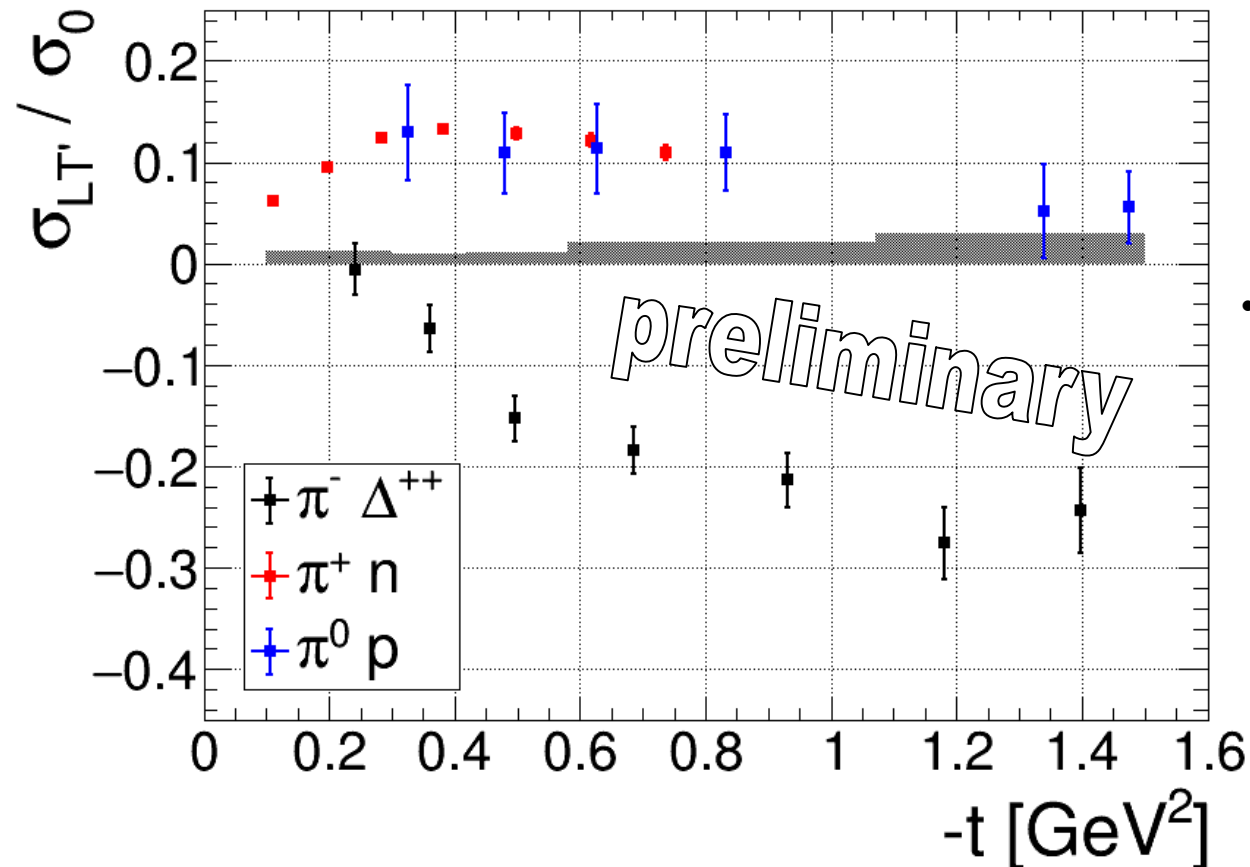
$$BSA(t, \phi, x_B, Q^2) \sim \sqrt{2\epsilon(1-\epsilon)} \frac{\sigma_{LT'}}{\sigma_0} \sin \phi$$

preliminary



$Q^2 - x_B$ Integrated Result

$$\langle Q^2 \rangle = 2.48 \text{ GeV}^2, \langle x_B \rangle = 0.27$$



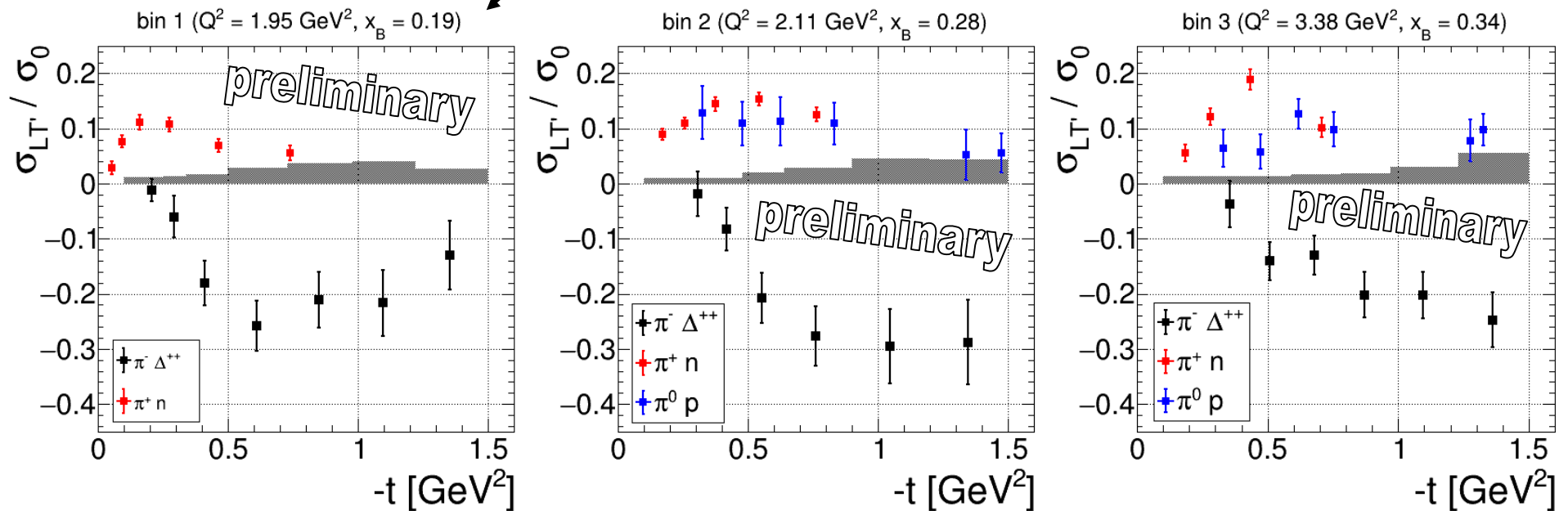
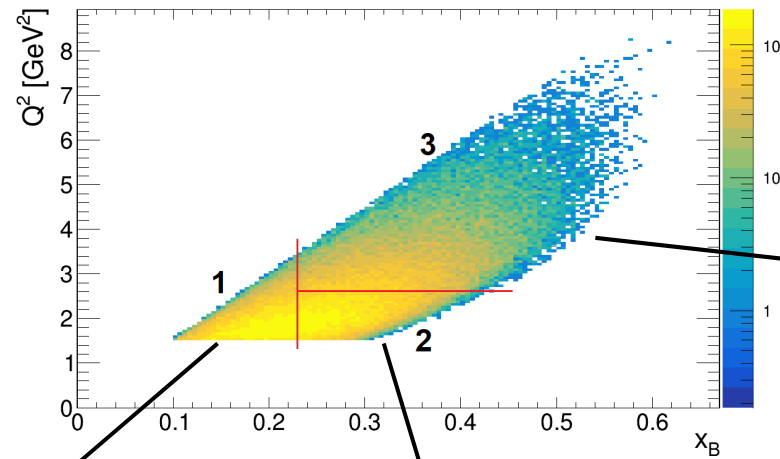
- The contribution of the non-resonant background has been subtracted

Different sources of systematic uncertainty have been studied:
 beam polarisation, background subtraction, fiducial volume, extraction method,
 acceptance, bin migration, radiative effects

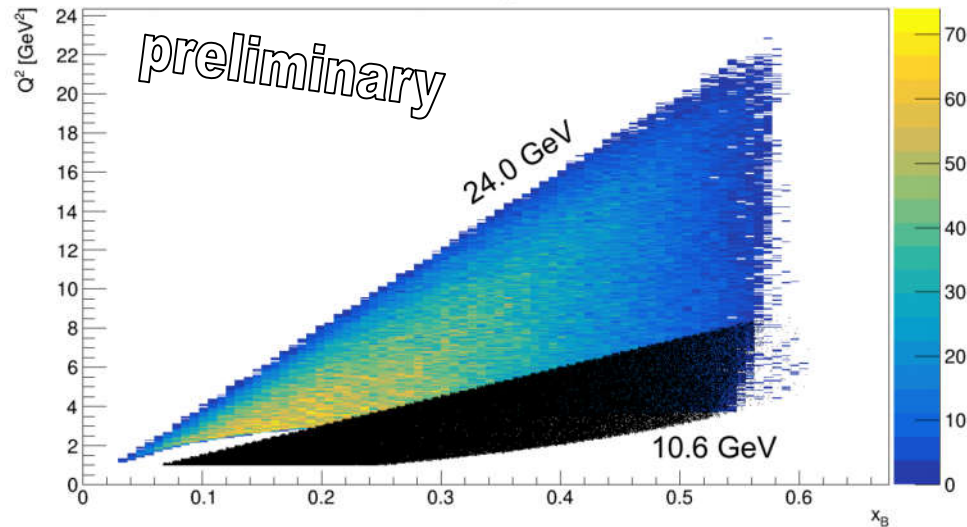
Multidimensional Results



preliminary



Perspectives for a 24 GeV JLAB upgrade



$$ep \rightarrow e\Delta^{++}\pi^- \rightarrow ep\pi^+\pi^-$$

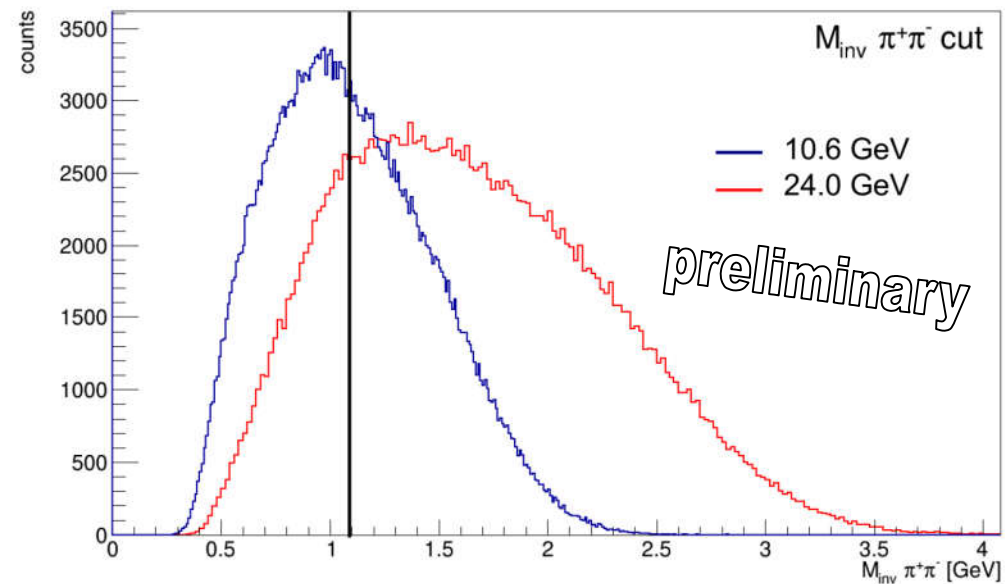
Extended Q^2 range

→ **Advantage for factorisation**

- Similar for non-diagonal DVCS

Better signal / background separation

→ **Higher efficiency**



Conclusion and Outlook

- Transition GPDs can help us to better understand the 3D structure of resonances and the excitation process itself.
- Non-diagonal DVCS and hard exclusive $\pi\Delta^{++}$ production can be well measured with CLAS12
- The extracted $\pi\Delta^{++}$ BSA is a potential first „clean“ observable sensitive to p- Δ transition GPDs
- Theory predictions are so far only available for twist-2 transition GPDs
 - ➔ Extension of the framework to the twist-3 sector needed
 - ➔ Connection of transition GPDs to physics properties (sum rules etc.) needed