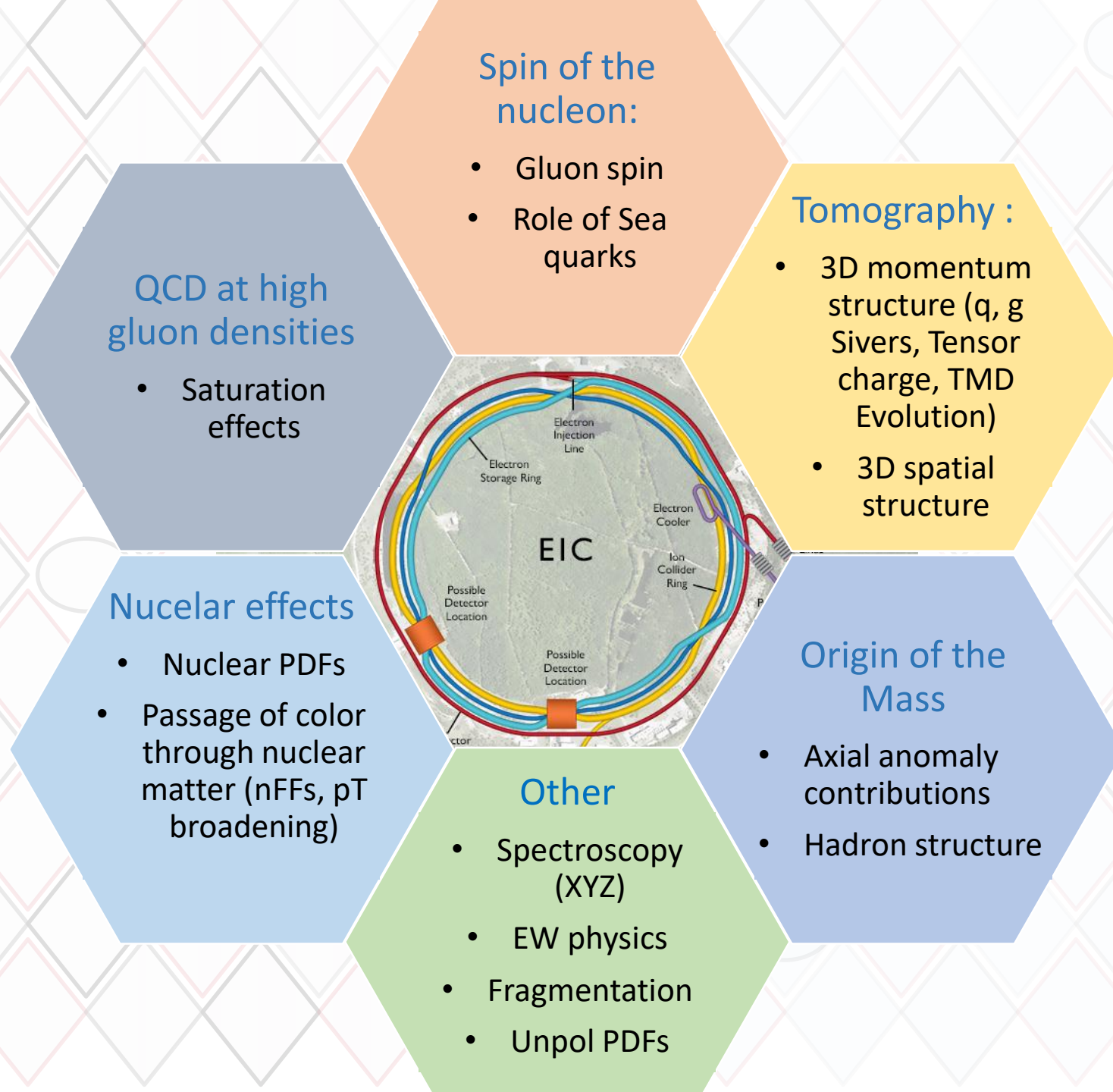


# TMDs with single hadrons at the **Electron Ion Collider**

**APCTP EIC workshop, Incheon,  
November 4, 2022,  
Ralf Seidl (RIKEN)**



### Spin of the nucleon:

- Gluon spin
- Role of Sea quarks

### Tomography :

- 3D momentum structure ( $q$ ,  $g$  Sivers, Tensor charge, TMD Evolution)
- 3D spatial structure

### QCD at high gluon densities

- Saturation effects

### Nuclear effects

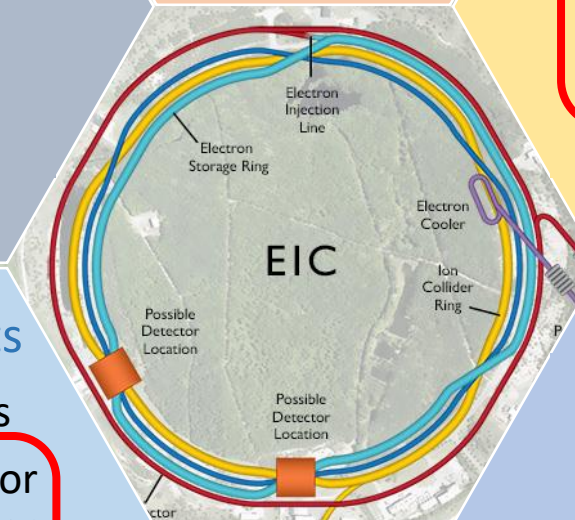
- Nuclear PDFs
- Passage of color through nuclear matter (nFFs,  $p_T$  broadening)

### Other

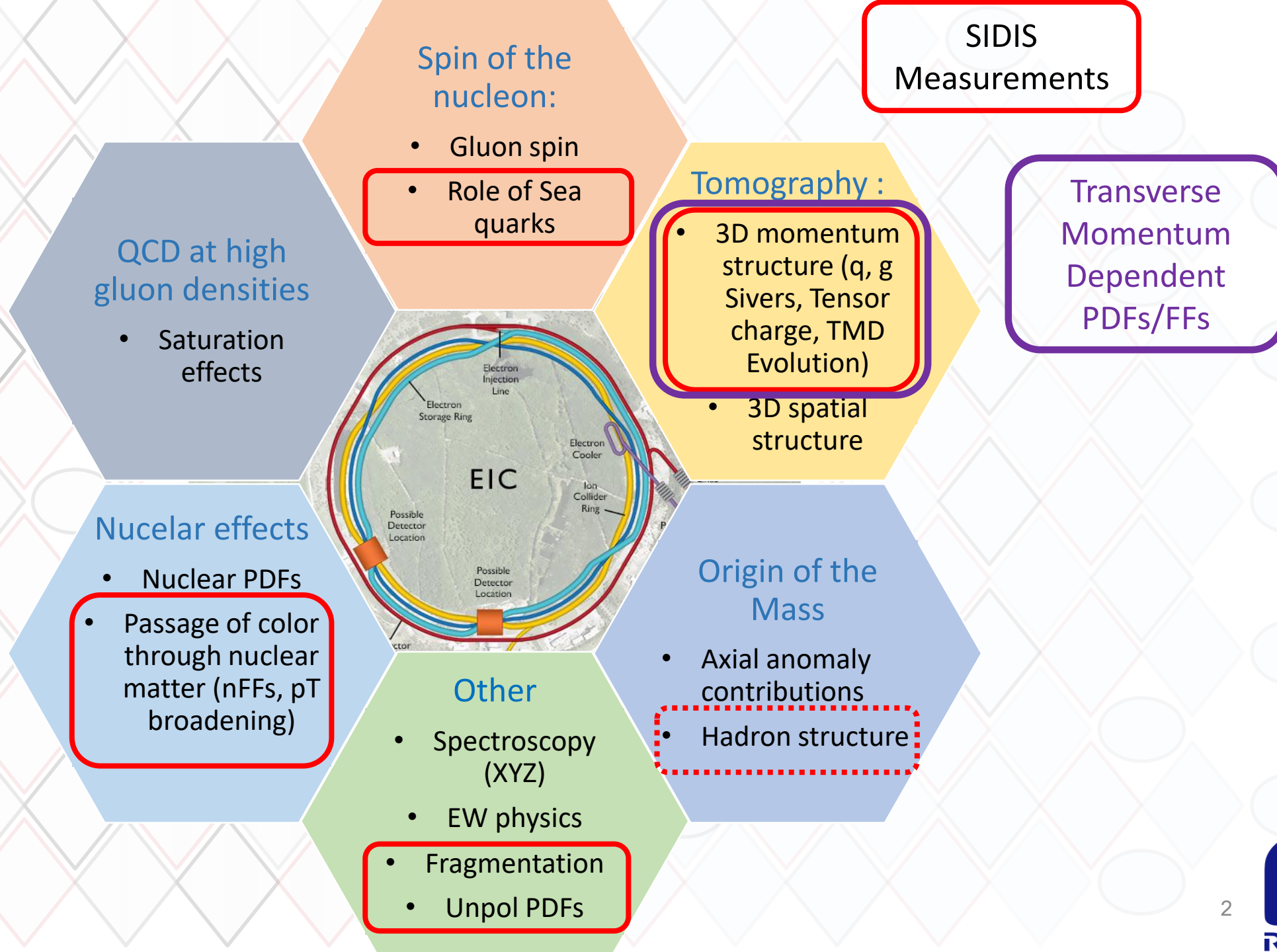
- Spectroscopy (XYZ)
- EW physics
- Fragmentation
- Unpol PDFs

### Origin of the Mass

- Axial anomaly contributions
- Hadron structure









# Transverse Spin

- Transversity

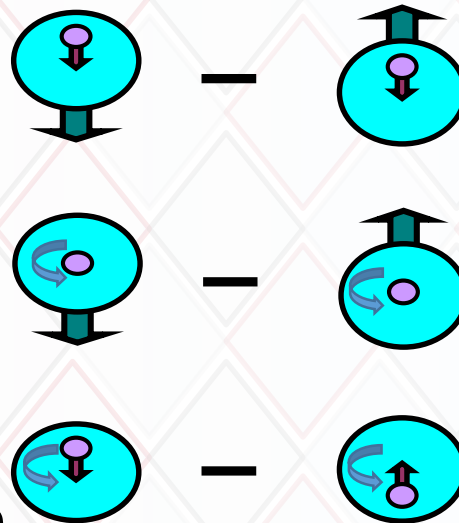
$$h_{1,q}(x)$$

- Sivers Function

$$f_{1T,q}^\perp(x, k_T)$$

- Boer Mulders function

$$h_{1T,q}^\perp(x, k_T)$$

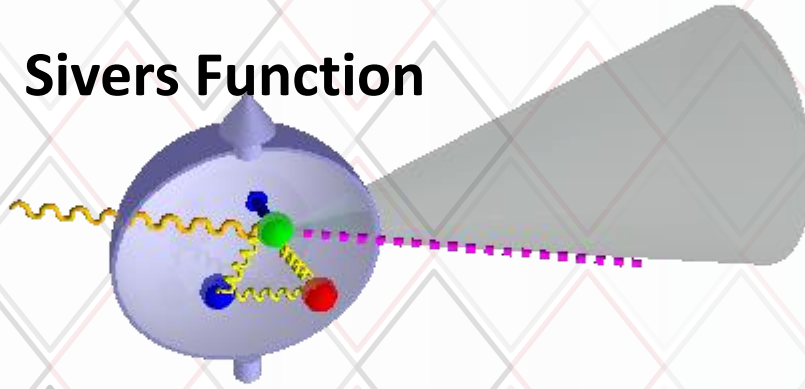


		Quark polarization		
		Unpolarized (U)	Longitudinally Polarized (L)	Transversely Polarized (T)
Nucleon Polarization	U	$f_1 = \odot$		$h_1^\perp = \uparrow - \downarrow$
	L		$g_1 = \rightarrow - \leftarrow$	$h_{1L}^\perp = \rightarrow - \leftarrow$
	T	$f_{1T}^\perp = \uparrow - \downarrow$	$g_{1T} = \rightarrow - \leftarrow$	$h_1 = \uparrow - \downarrow$ $h_{1T}^\perp = \rightarrow - \leftarrow$

Closely related:

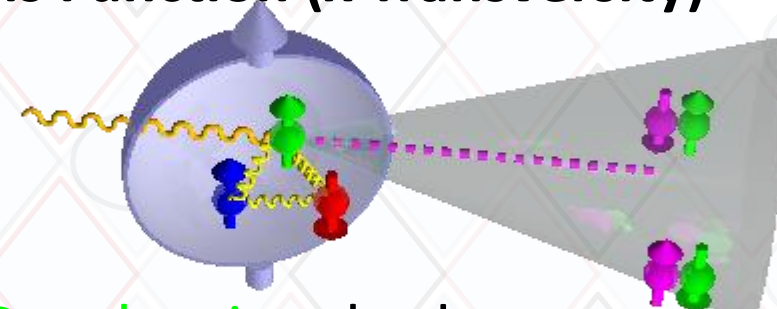
- Higher Twist correlations (TMD moments)  $T_F(x, x)$
- TMD FFs (Collins, polarizing FFs, etc)  $H_{1,q}^{\perp(1)}(z)$

## Sivers Function

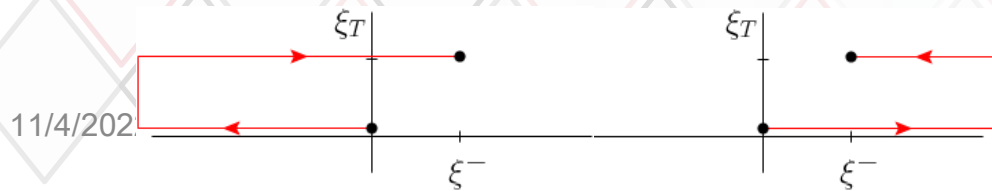


- Proton–spin – quark orbit ( $k_T$ ) correlation
- Suggested in '93 – dead due to time reversal
- Brodsky-Hwang-Schmid '02 model example of Sivers function using gauge links
- Belitsky-Yuan '02  $\rightarrow$  gauge links generally needed
- Collins  $\rightarrow$  function can exist, but modified universality (**the SIGN change**)

## Collins Function (x Transversity)

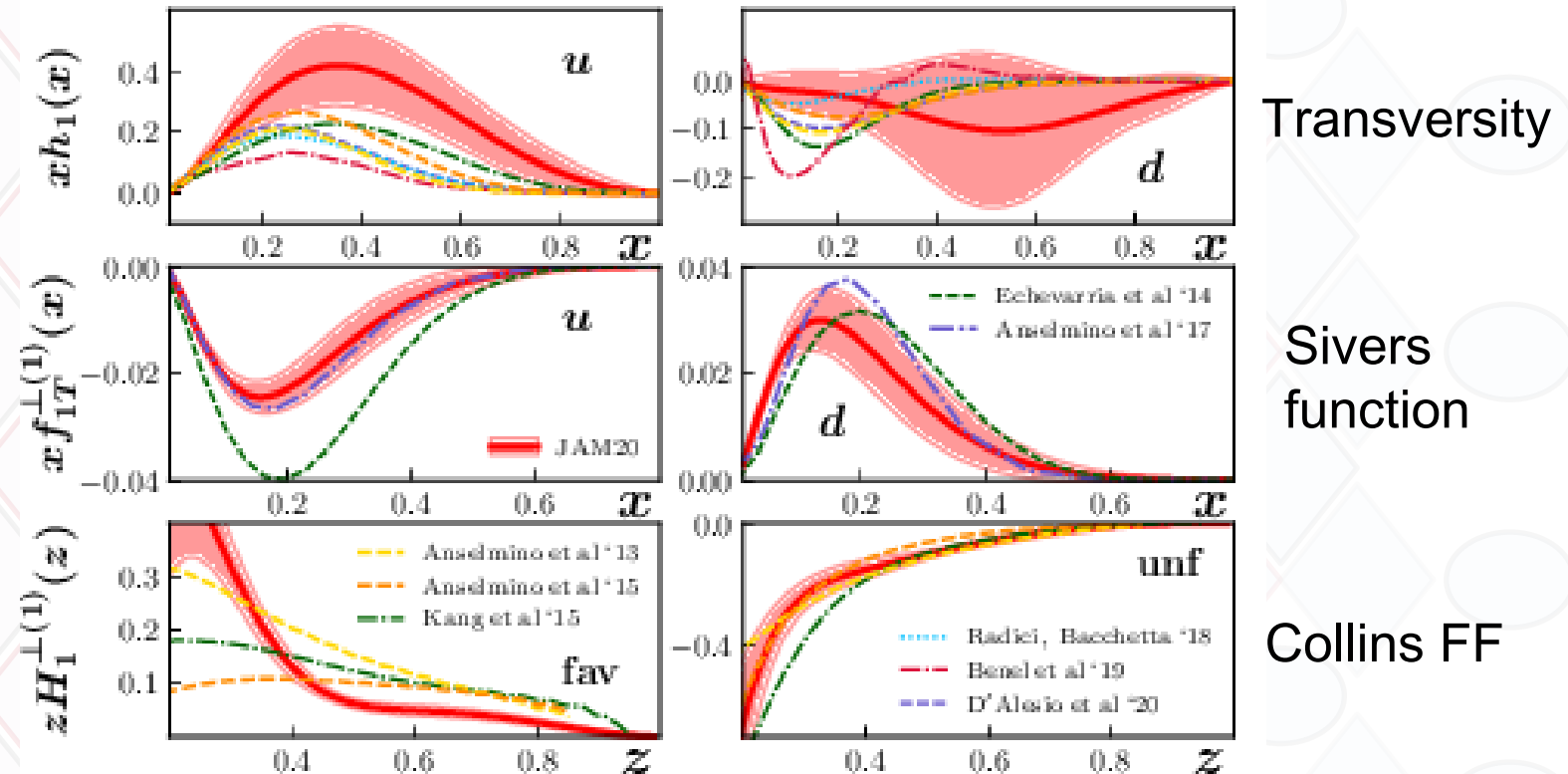


- **Quark spin** – hadron transverse momentum correlation (in fragmentation)
- Analyzer for quark transversity  $\rightarrow$  access to tensor charge (Lattice, BSM?)
- A polarized (ie signed) fragmentation function
- Transverse momentum conservation requires some compensation (Terayev-Schaefer)



# Current knowledge on these functions

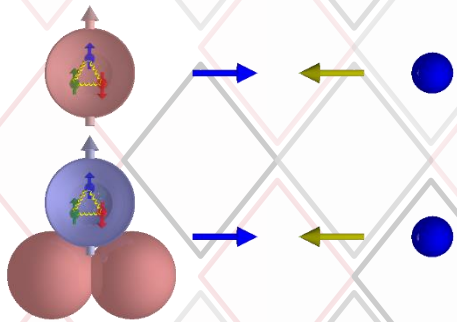
- Only valence quark Sivers and Transversity functions known at this time with substantial uncertainties
- Experimentally covered range  $0.01 < x < 0.3$
- So far no sensitivity to sea quarks and gluons\* and lower  $x$



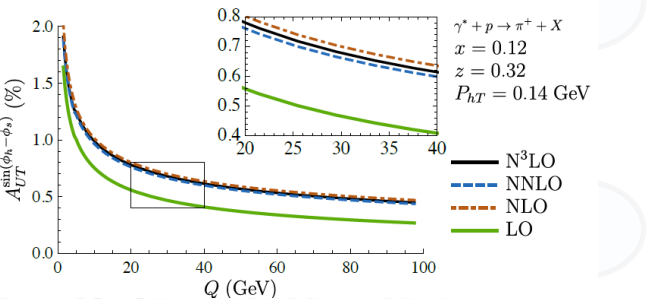
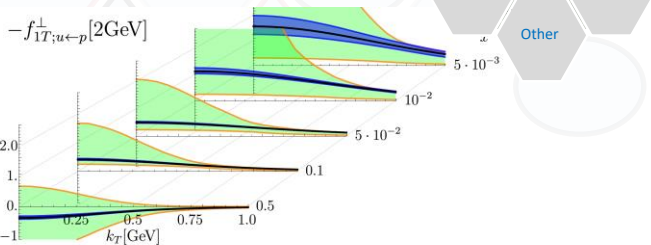
[Camarota et al, PRD 102 \(2020\) 054002](#)



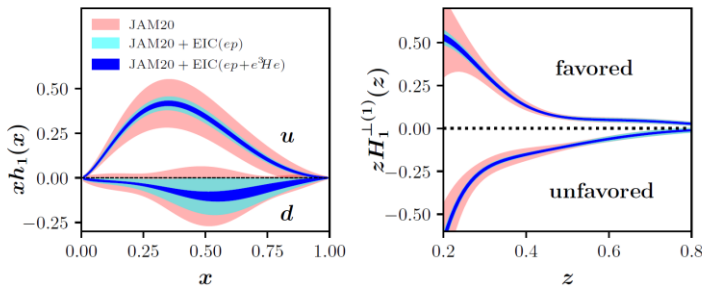
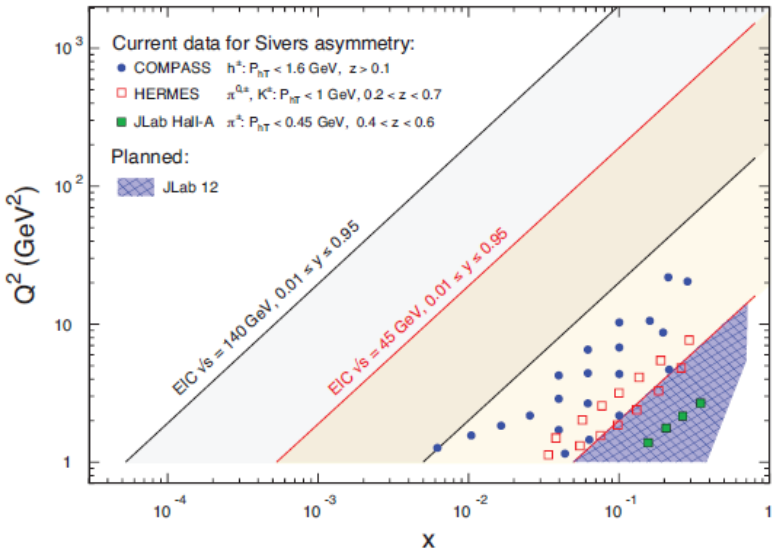
# Motivation: 3D Transverse spin and momentum structure



Deliverables	Observables	What we learn	Stage I	Stage II
Sivers & unpolarized TMD quarks and gluon	SIDIS with Transverse polarization; di-hadron (di-jet)	Quantum Interference & Spin-Orbital correlations	3D Imaging of quarks valence+sea	3D Imaging of quarks & gluon; $Q^2$ ( $P_{hT}$ ) range QCD dynamics
Chiral-odd functions: Transversity; Boer-Mulders	SIDIS with Transverse polarization	3 <sup>rd</sup> basic quark PDF; novel hadronization effects	valence+sea quarks	$Q^2$ ( $P_{hT}$ ) range for detailed QCD dynamics



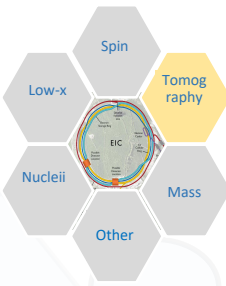
Tables from original EIC white paper



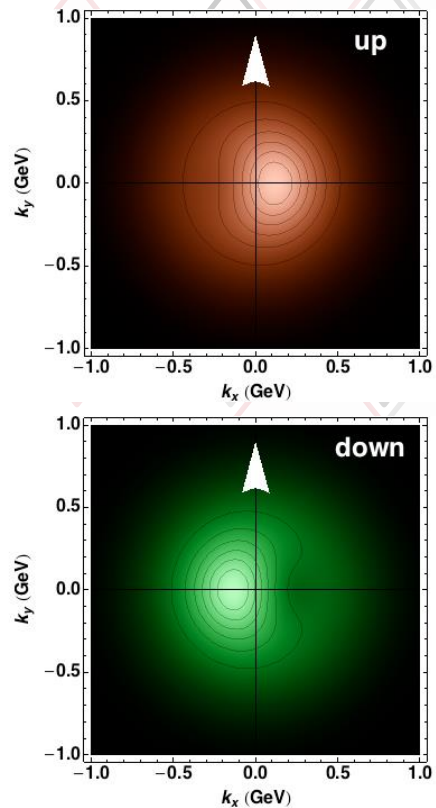
Current coverage for transverse spin related measurements

Seidl: EIC TMDs

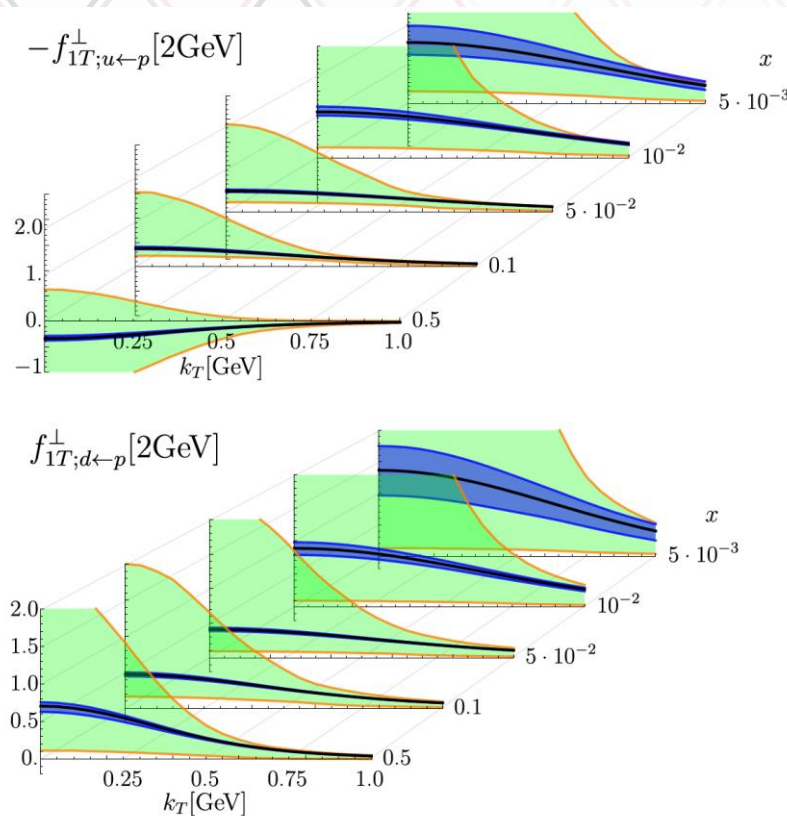
# EIC impact for Sivers Functions



Transverse momentum imbalance of unpolarized partons in a transversely polarized nucleon  $\leftrightarrow$  model dependent relation to orbital angular momentum

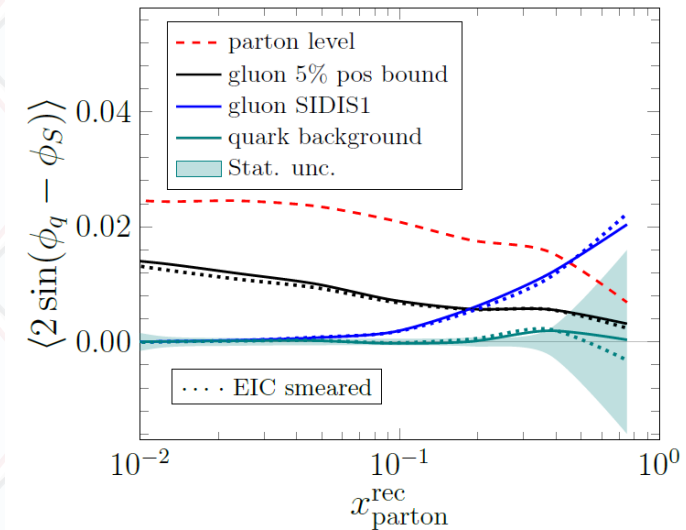


Bacchetta, Radici,  
PRL 107 (2011) 212001



[YR](#): Fig 7.53  
Vladimirov, et al

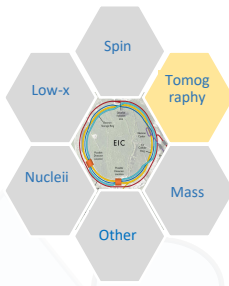
- Precise nucleon image in momentum space for quarks, sea-quarks and gluons



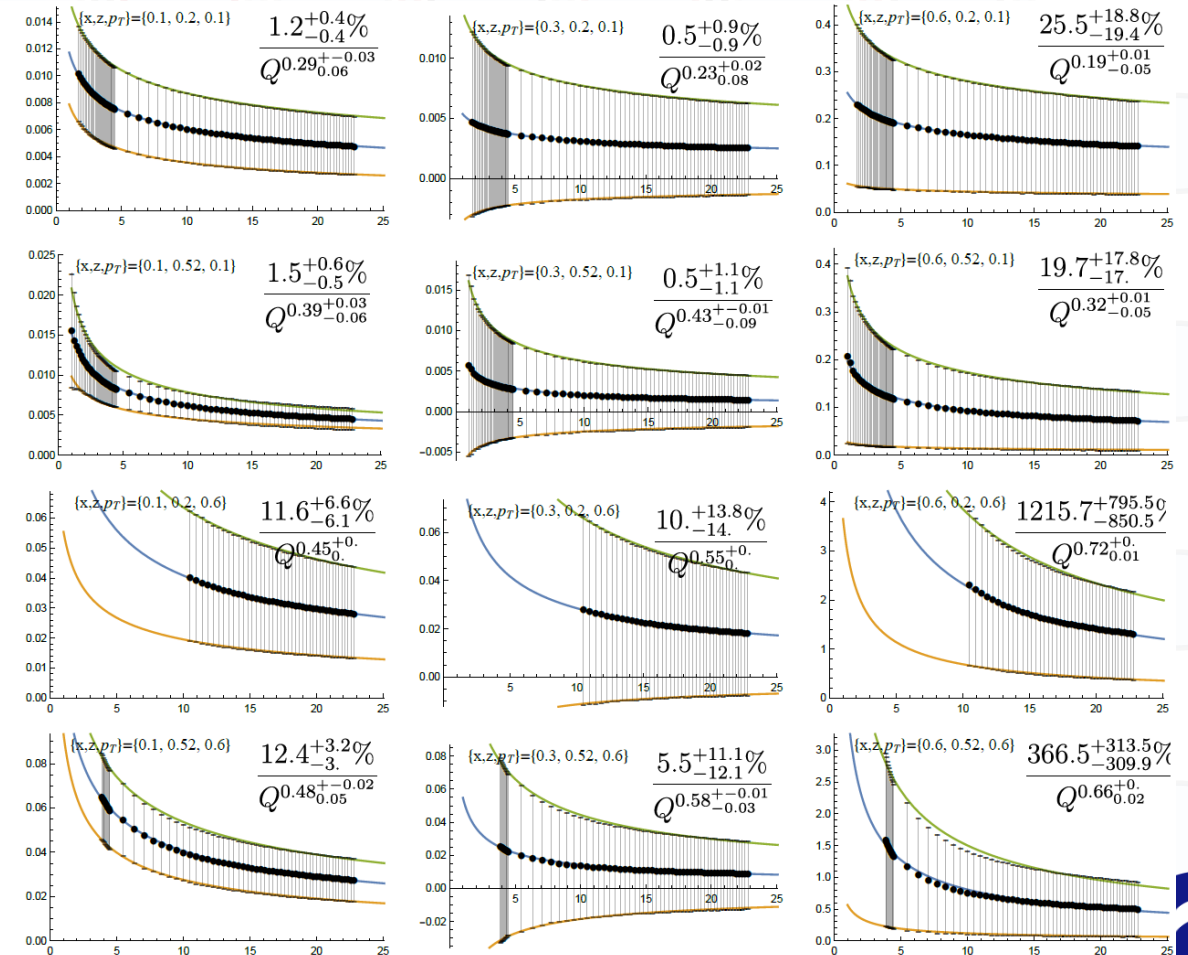
[YR](#) Fig 7.55  
Xiao, et al

# EIC access to TMD evolution

- Very important aspect is the study of TMD evolution
- Sivers asymmetries are expected to decrease at higher scales, but only logarithmically (ie they do NOT “disappear”)
- At higher x Asymmetries of several % expected
  - ➔ Well accessible with EIC over wide range in x and  $Q^2$
  - ➔ Lower x to study sea and glue (both mostly unknown)

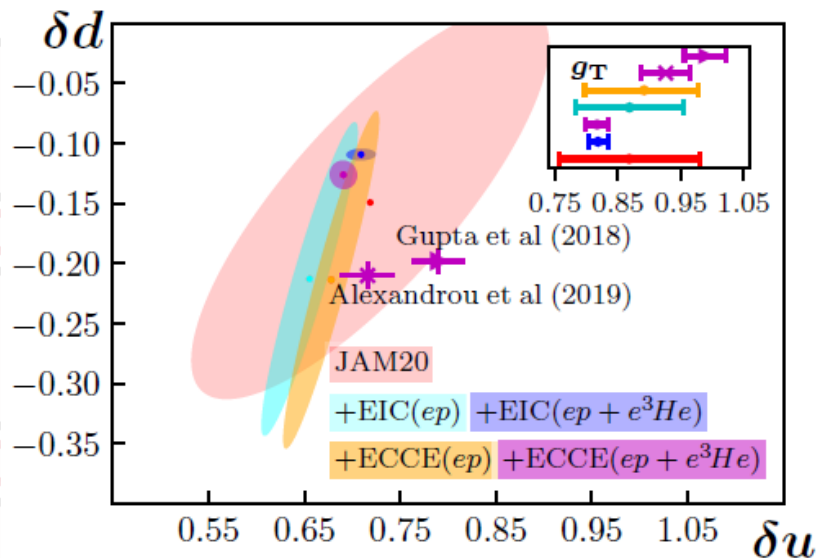
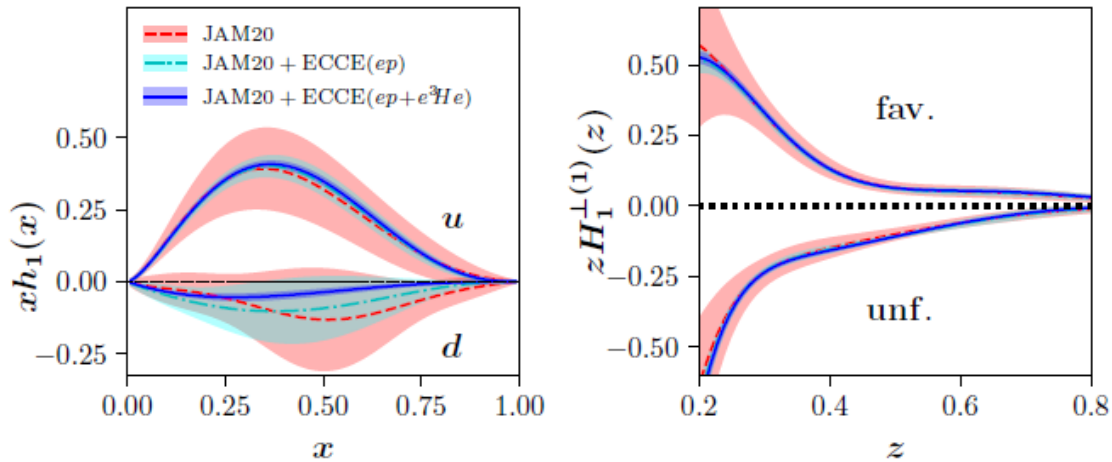
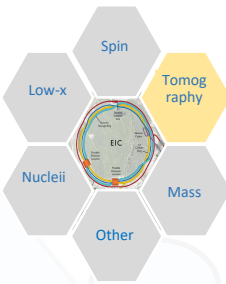


Vladimirov et al.





# Tensor charges



[hep-ex:2207.10890](https://arxiv.org/abs/hep-ex/2207.10890)

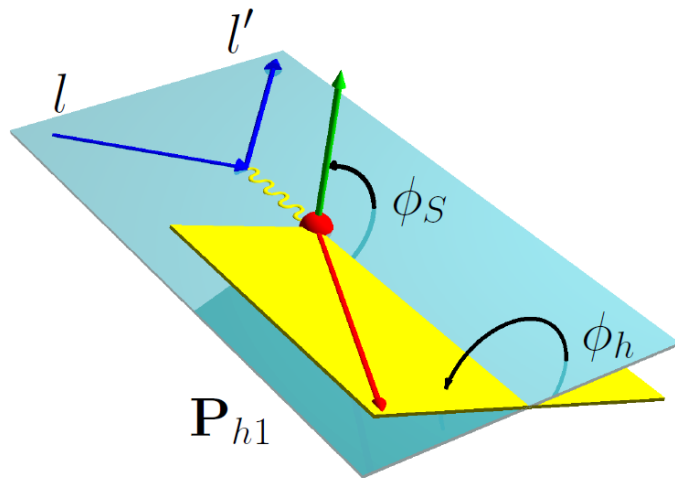
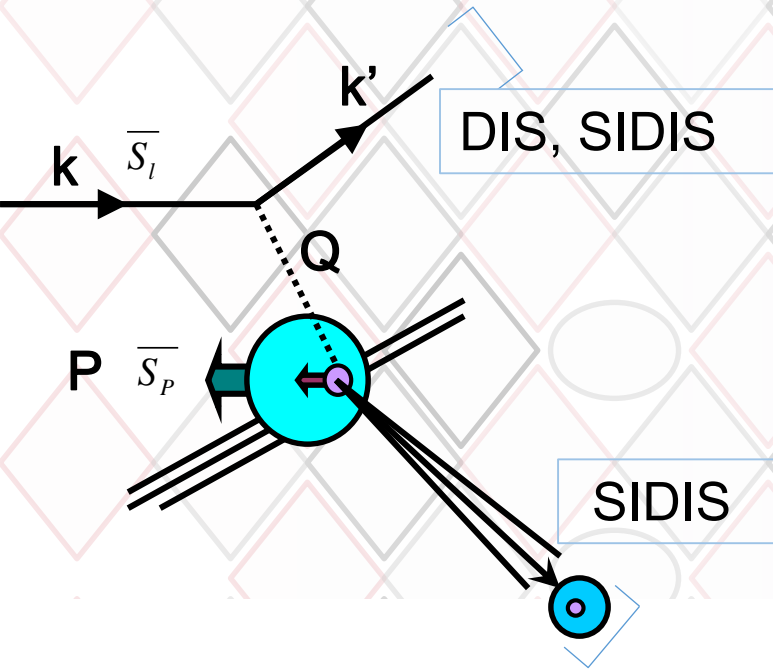
- Precise determination of tensor charges via Collins and di-hadron channels
- Better precision than lattice → potential access to BSM physics in case of discrepancies
- Preform full integrals, study role of sea quark transversity

Similarly:

Single hadron channel ([YR](#) : Fig 7.54 [Gamberg et al Phys.Lett.B 816 \(2021\) 136255](#))

Di-hadron channel ([YR](#) : Fig 7.56, Radici)

# SIDIS Kinematics



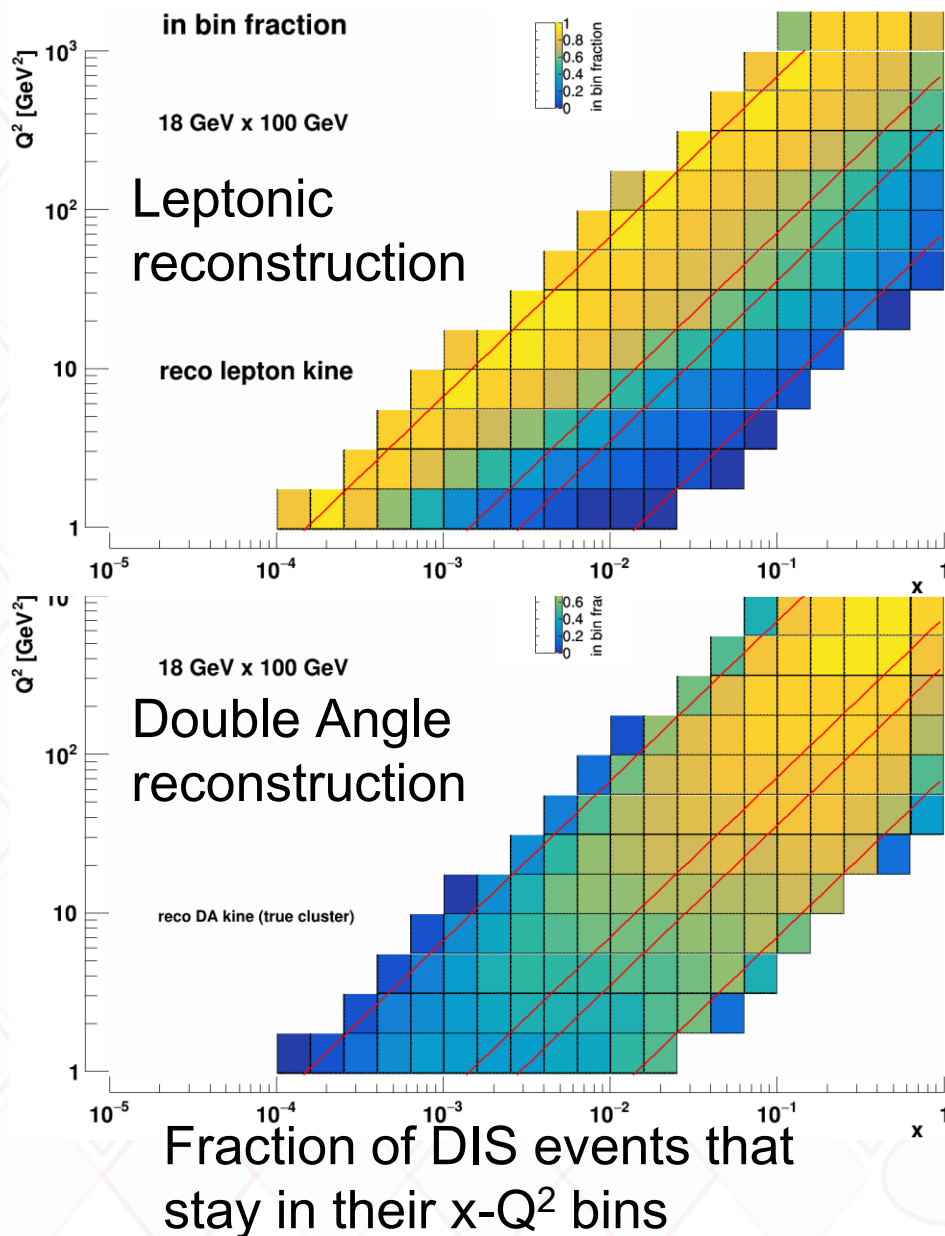
Detect also final-state hadron(s): Additional benefit of **flavor, spin and transverse momentum sensitivity** via Fragmentation functions

$$\frac{d^6\sigma}{dx dQ^2 dz dP_{hT} d\phi_S d\phi_h} \stackrel{LO}{\propto} \sum_{q,\bar{q}} e_q^2 q(x, Q^2, k_t) \otimes D_{1,q}^h(z, Q^2, p_t)$$

- |            |  |
|------------|--|
| $z$ :      | Fractional hadron momentum wrt to parton momentum ( $0 < z < 1$ )  |
| $P_{hT}$ : | transverse hadron momentum wrt to virtual photon (convolution over intrinsic transverse momenta of PDFs and FFs) |
| $\phi_S$ : | Azimuthal angle of nucleon (transverse) spin wrt to scattering plane, along virtual photon axis                  |
| $\phi_h$ : | Azimuthal angle of hadron wrt to scattering plane, along virtual photon axis                                     |

- Current fragmentation: related to struck quark (favored fragmentation  $u \rightarrow \pi^+$ ,  $d \rightarrow \pi^-$ ,  $s \rightarrow K^-$ , etc)
- Transverse momentum and angles rely also on correct boost to hadron rest system

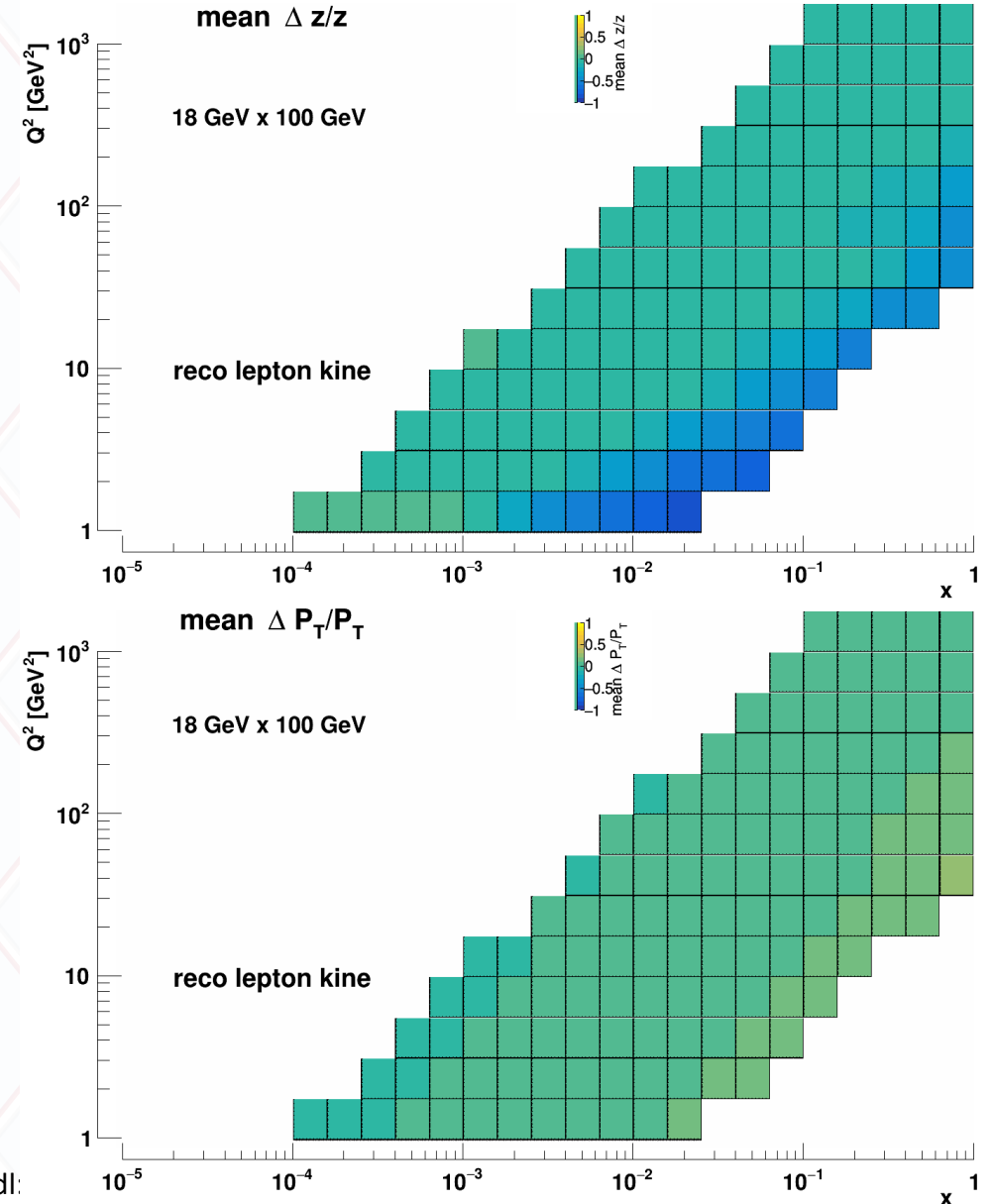
- Full Pythia6+GEANT simulations of the ECCE detector used for various (SI)DIS kinematic resolutions and for various reconstruction methods (lepton, Jaquet-Blondel, Double Angle, etc)
- x and y resolutions suffer from lepton method at lower y, partially recoverable in double angle method (hybrid of scattered lepton + hadronic final state)



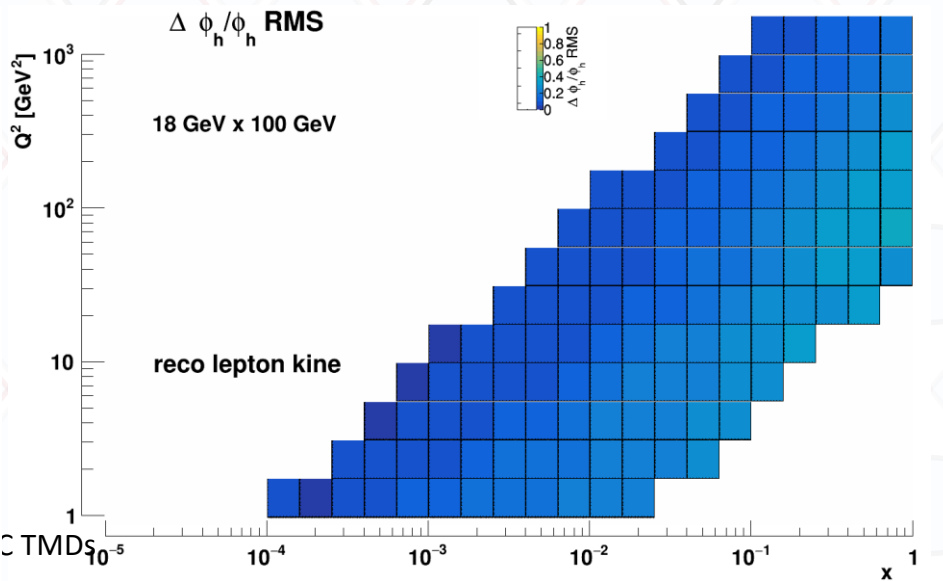
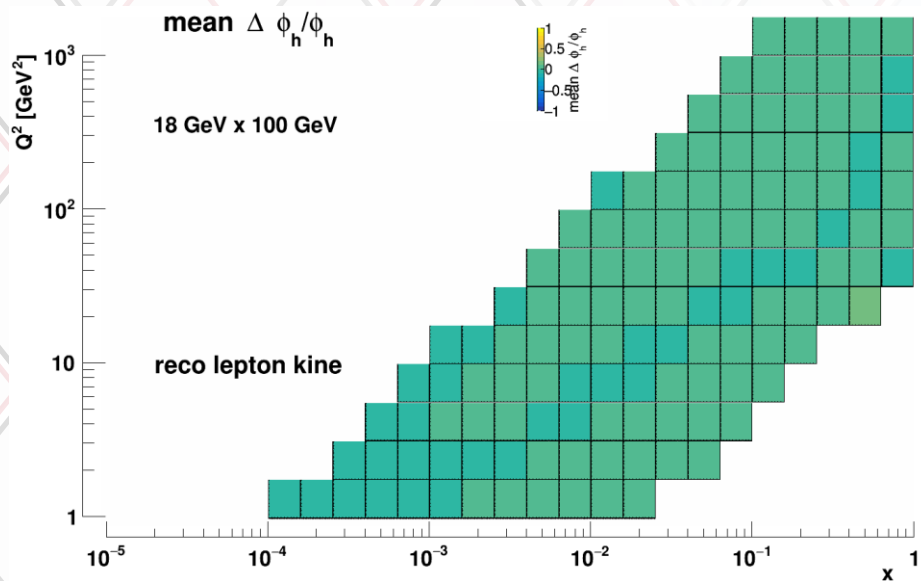
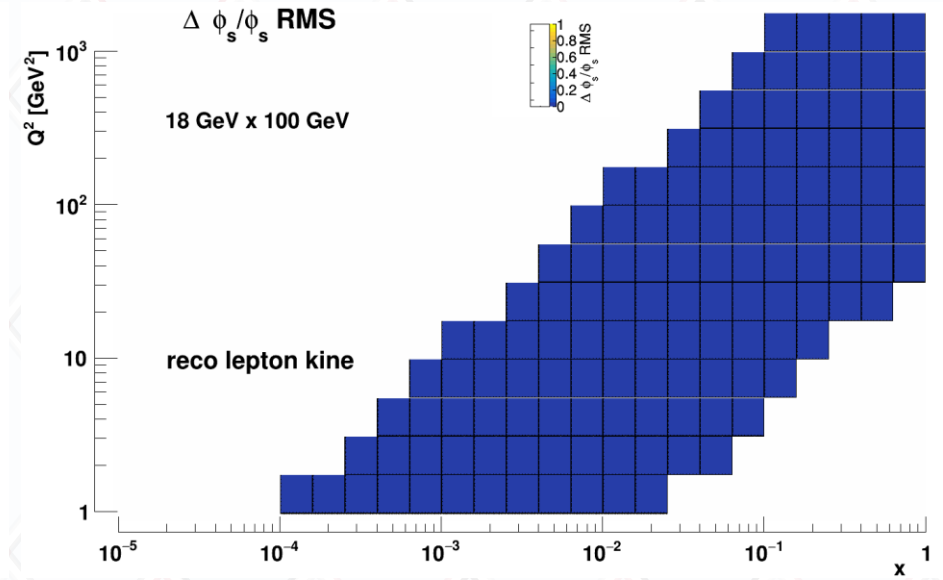
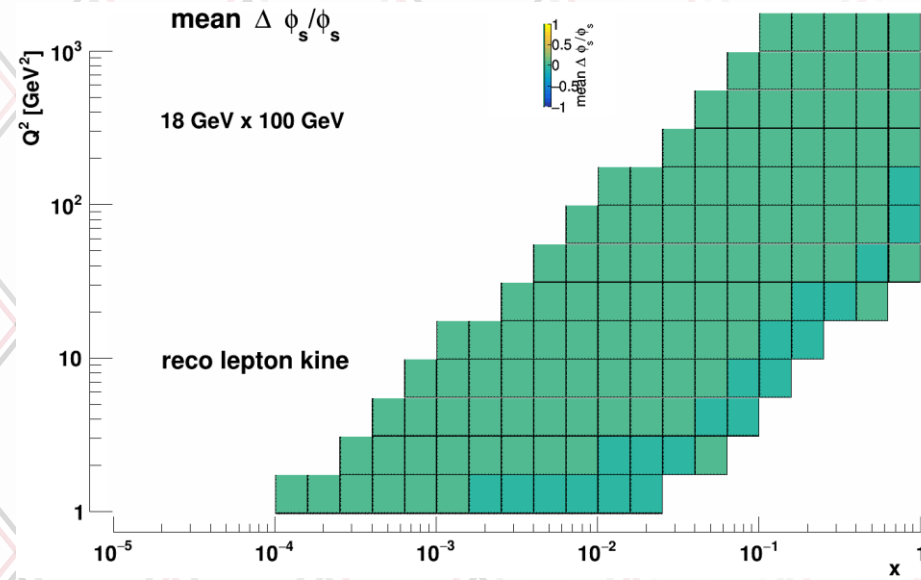


# Example of SIDIS resolutions studies

- Full Pythia6+GEANT simulations of the ECCE detector for various (SI)DIS kinematic resolution and reconstruction methods:
  - $z$  resolution suffers in lepton method at lower  $y$ , partially recoverable in double angle method
  - $p_T$  and azimuthal angles  $\phi_h$ ,  $\phi_s$  very robust

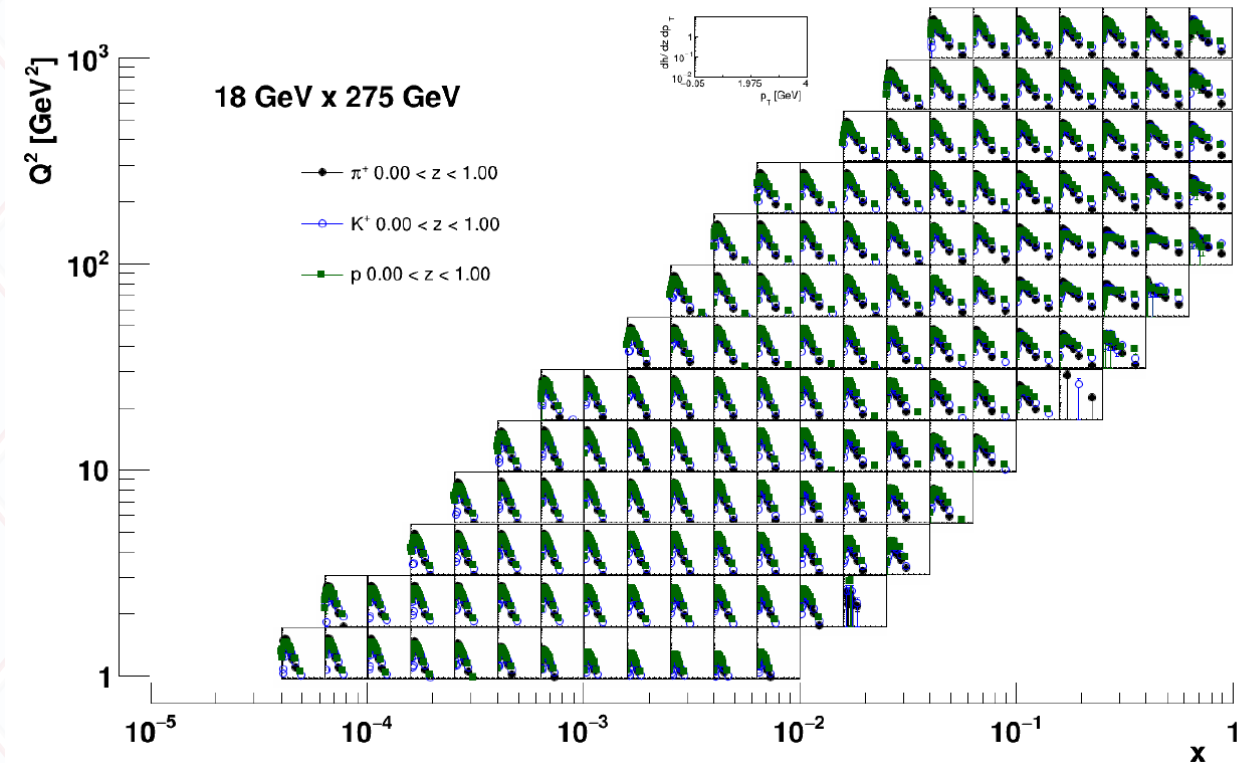


# Azimuthal angles



# ECCE simulation setup, unpolarized TMD studies

- pythiaRHIC (Pythia 6) simulations for e+p collisions at 4 energies similar to YR
- Generator output simulated through GEANT4
- Scattered lepton ( $|\eta| < 3.5$ ) DIS kinematic reconstruction using reco track momenta (assuming perfect eID)
- DIS cuts:  $0.01 < y < 0.95$ ,  $Q^2 > 1$ ,  $W^2 > 10 \text{ GeV}^2$
- SIDIS cuts: pions and kaons ( $|\eta| < 3.5$ ), using true PID (assuming successful unfolding)
- $25 \times 13 \times 12 \times 12$  kinematic bins ( $x, Q^2, z, P_T$ )
- Pion, kaon and proton multiplicities shown in all  $x$ - $Q^2$  bins as a function of  $P_T$  (integrated over  $z$ )

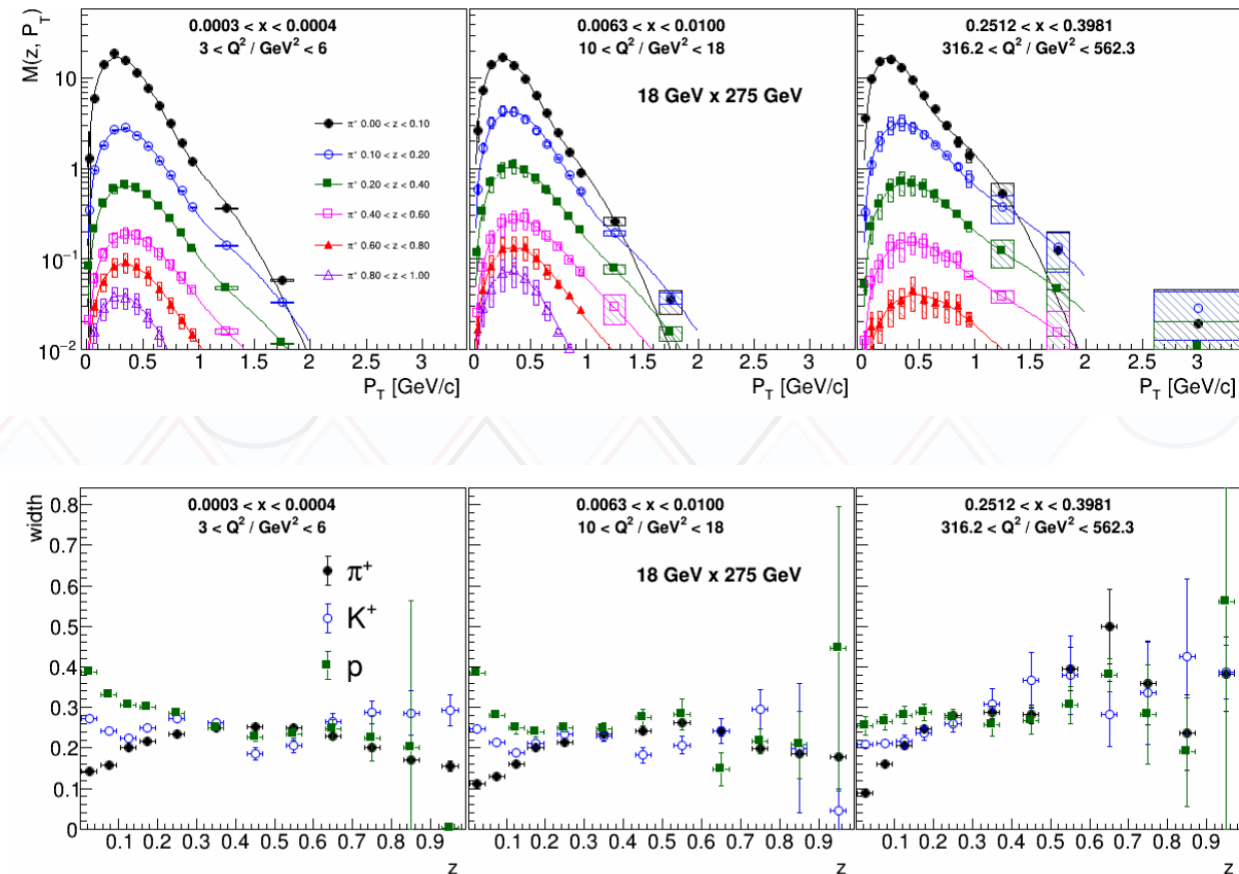


[hep-ex:2207.10893](https://arxiv.org/abs/hep-ex/2207.10893)



# z-dependence of multiplicities and widths

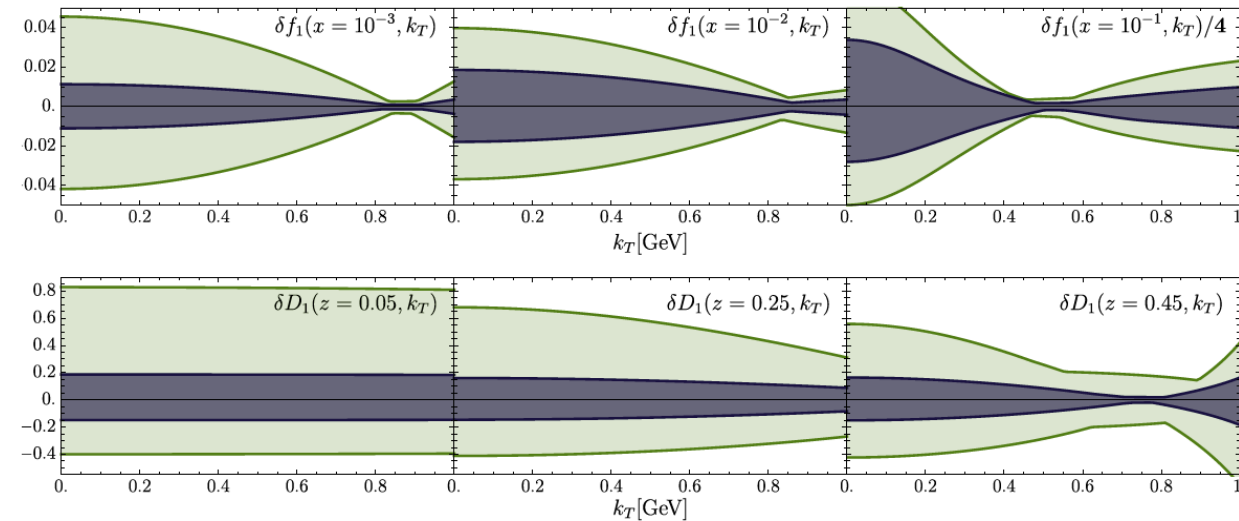
- Top: Explicit z dependence of select pion multiplicities in 3 x- $Q^2$  bins, including the double-Gaussian fits
- Bottom: behavior of the narrow Gaussian widths vs z for pions, kaons and protons
- Small z discrepancies likely due to target fragmentation



[hep-ex:2207.10893](https://arxiv.org/abs/hep-ex/2207.10893)

# Impact for unpolarized TMD functions

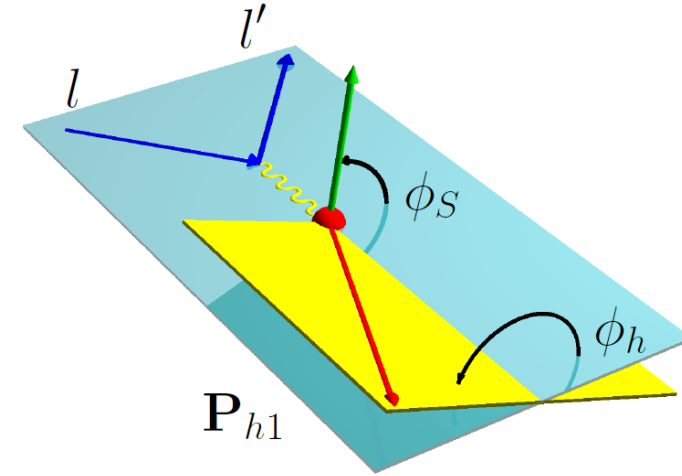
- Similar to YR impact studies following the latest SV global fit (<https://arxiv.org/abs/1912.06532>) for the unpolarized TMDs based on the existing SIDIS +DY data
- Consistent with Yellow Report expected impact



[hep-ex:2207.10893](https://arxiv.org/abs/hep-ex/2207.10893)

# Experimental access to Transversity/tensor charge and Sivers function

- Both functions are accessible as different azimuthal modulations in transversely polarized SIDIS of single hadrons
- Reweight events according to true parton flavor  $q$ , hadron  $h$ ,  $x$ ,  $z$ ,  $Q^2$ ,  $P_{hT}$ , azimuthal angles and random spin orientation
- Input structure functions (polarized and unpolarized) from Torino global fits (arXiv:0812.4366, arXiv:0805.2677) as in <https://github.com/prokudin/tmd-parametrizations/>
- Other TMD PDFs are similarly accessible via different modulations and spin orientations (though often higher twist effects present)
- Gluon Sivers via di-jet/di-HF TSSAs



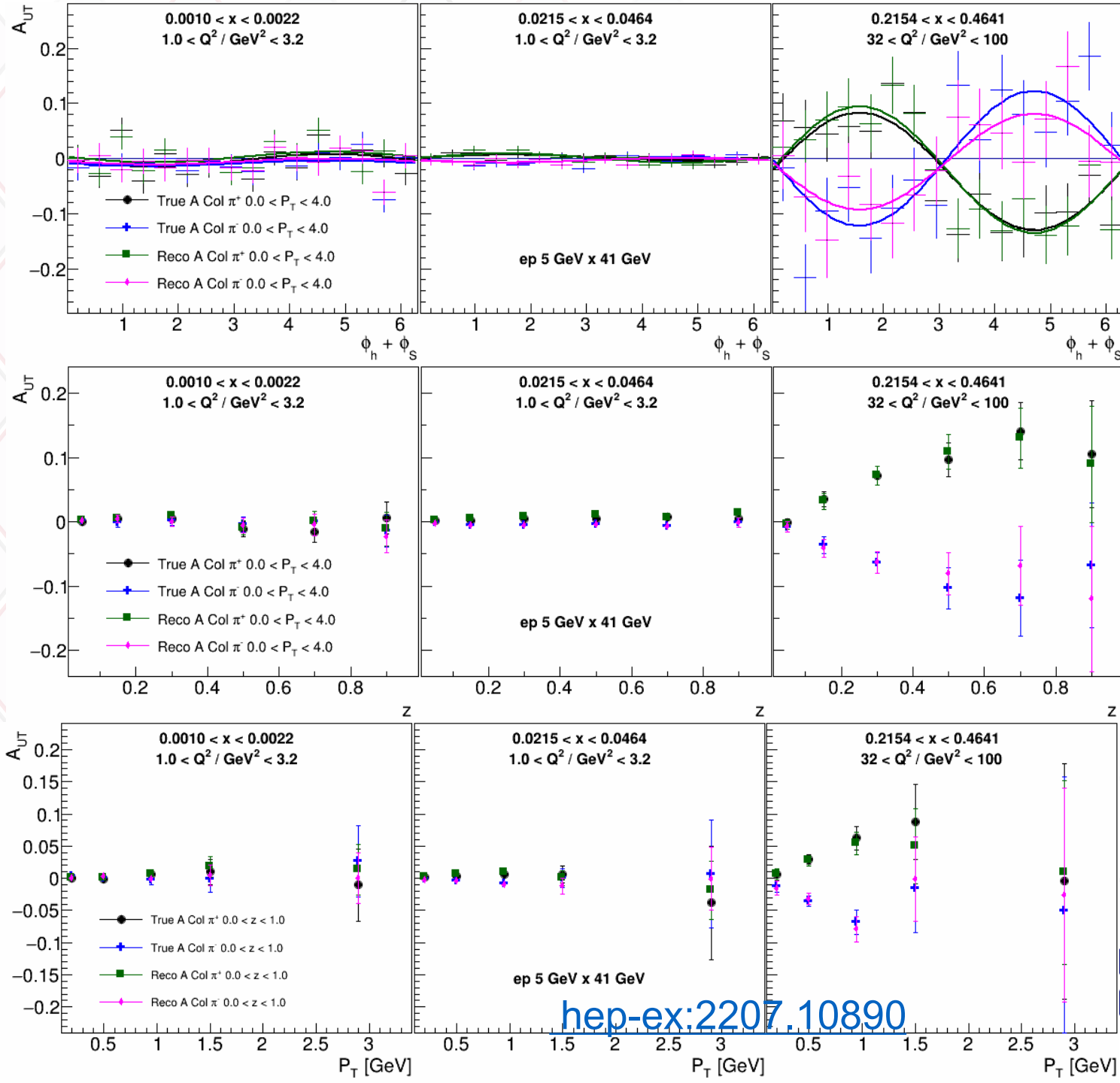
$$A_{UT}^{\sin(\phi_h + \phi_S)}(x, z, P_T) \propto \mathbf{S}_T \frac{\sum_{q, \bar{q}} e_q^2 \delta q(x, k_t) \otimes H_1^\perp(z, p_t)}{\sum_{q, \bar{q}} e_q^2 q(x, k_t) \otimes D_1(z, p_t)}$$

$$A_{UT}^{\sin(\phi_h - \phi_S)}(x, z, P_T) \propto \mathbf{S}_T \frac{\sum_{q, \bar{q}} e_q^2 f_{1T}^{\perp, q}(x, k_t) \otimes D_1(z, p_t)}{\sum_{q, \bar{q}} e_q^2 q(x, k_t) \otimes D_1(z, p_t)}$$



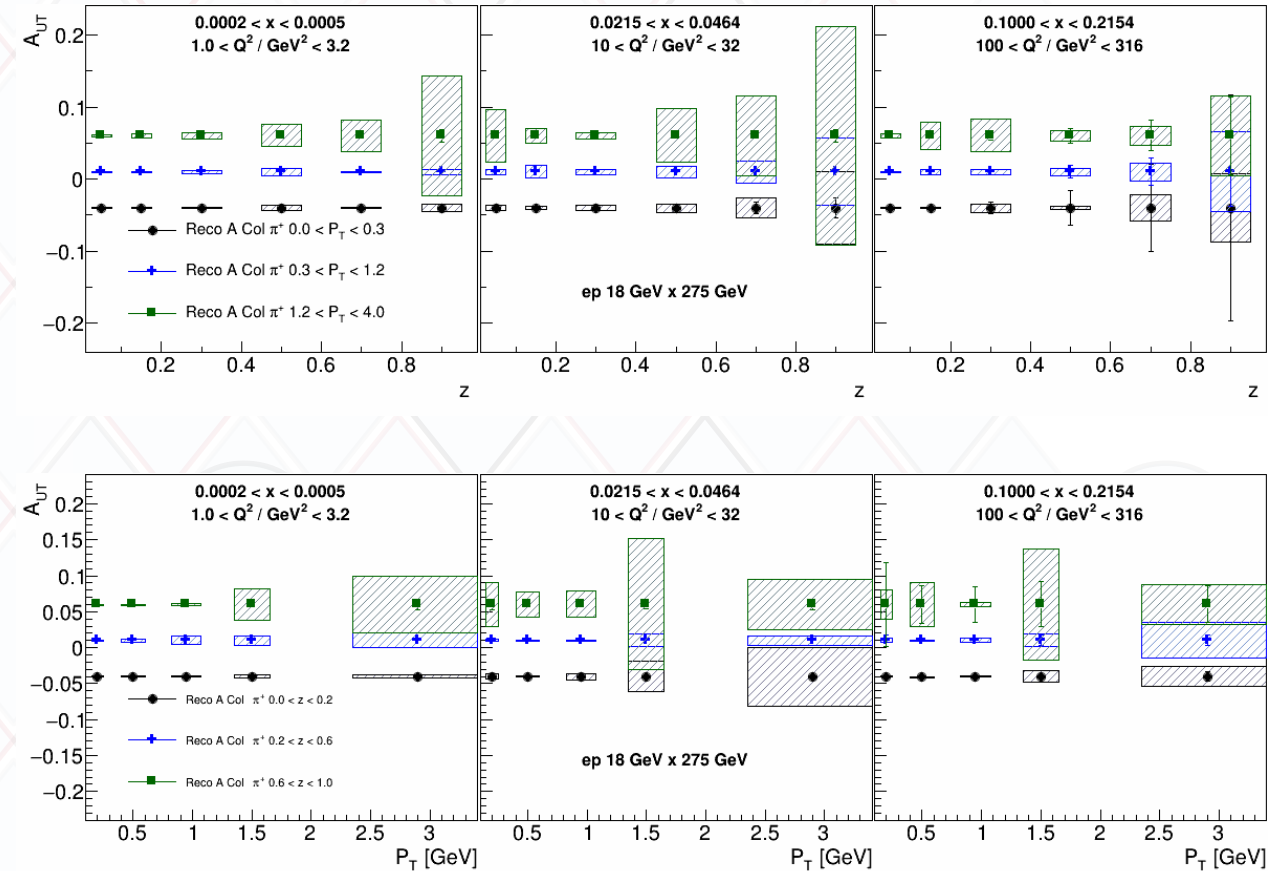
# Example Asymmetries

- Examples in 3  $x$  and  $Q^2$  bins: on top for the Collins angular combination for charged pions true and reconstructed in an intermediate  $z$  bin
- Lower figures: same, either projected vs  $z$  or vs  $P_T$



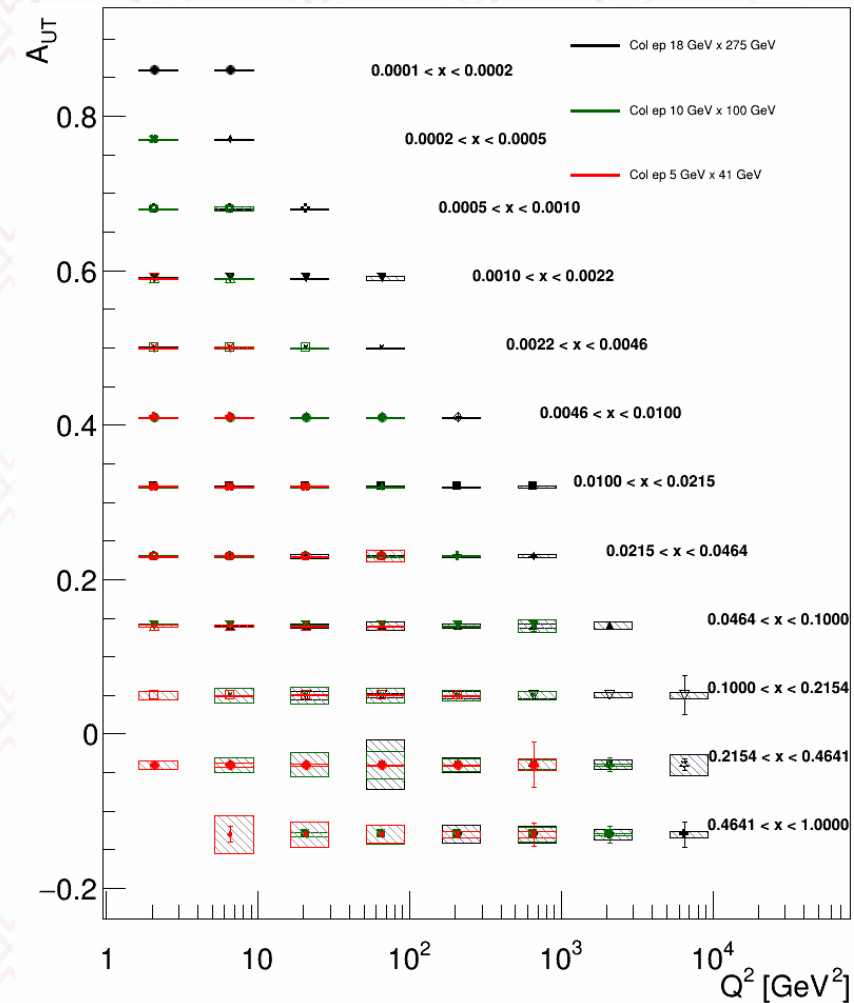
# Projections to $10\text{fb}^{-1}$

- Systematic uncertainties estimated from differences between true and reconstructed asymmetries  $\rightarrow$  they are likely largely overestimated since most of the kinematic smearing would be unfolded, but give a sense of where uncertainties still might be larger due to that unfolding



# Scale dependence (and interplay of collision energies)

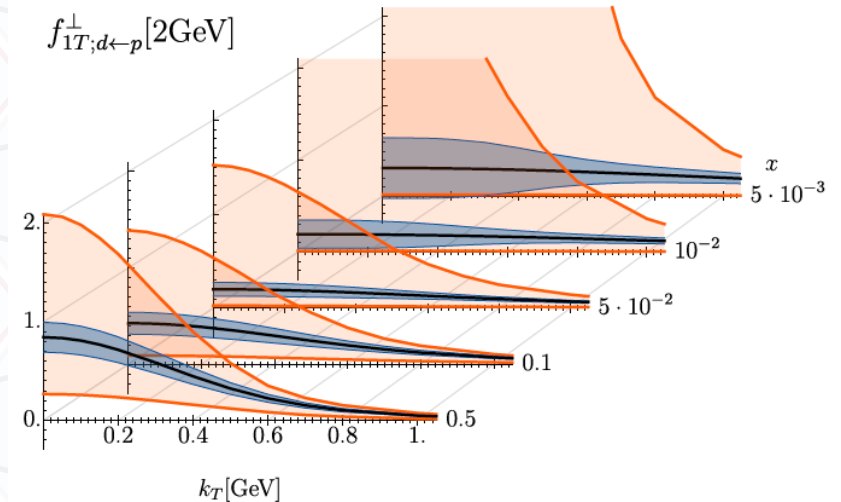
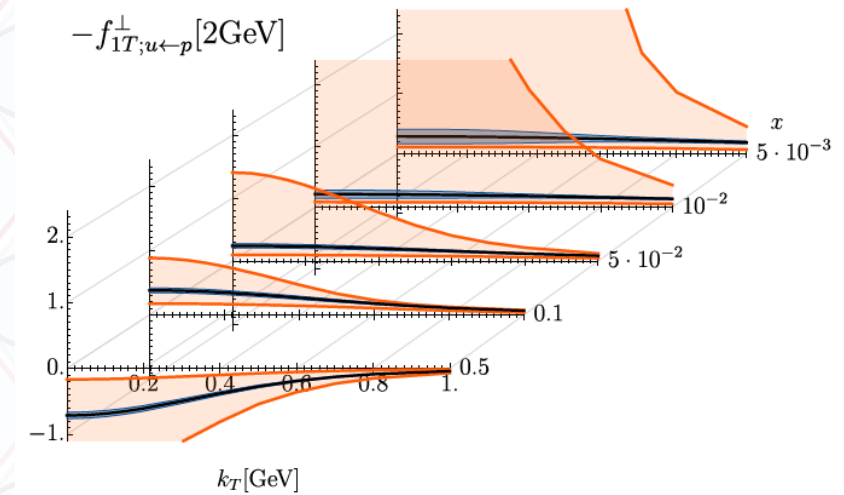
- An example of the expected uncertainties in  $x$  and  $Q^2$  to study the scale dependence of the Sivers/Collins asymmetries (as TMD evolution is not very well known/contains other nonperturbative pieces)
- Overlap of the different energies shows how they increase the lever arm
- Note: in future evolution analysis likely more  $Q^2$  bins and maybe not as fine  $x$  binning





# Impact for Sivers functions

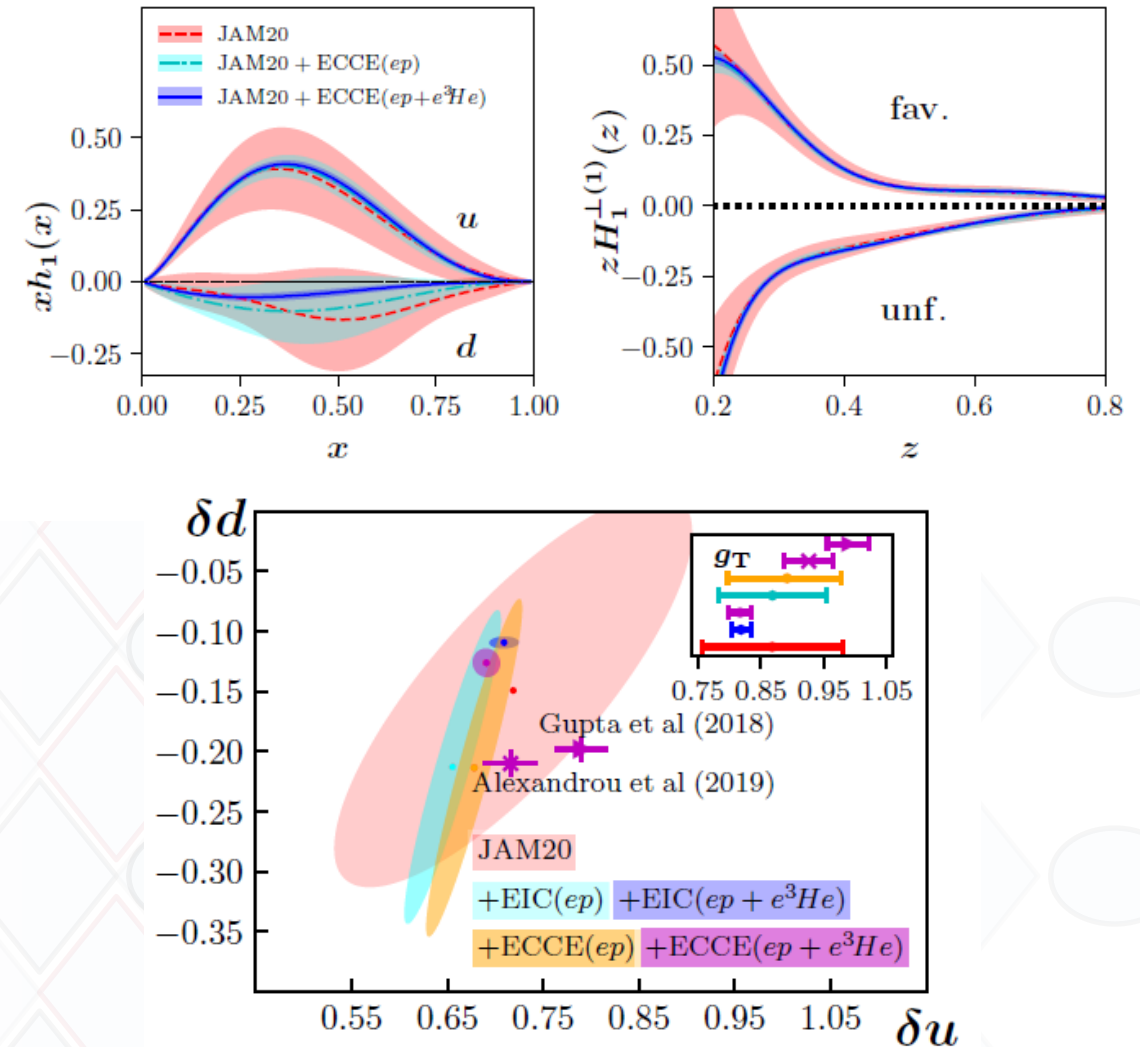
- Similar to YR impact studies following the latest BPV global fit (arXiv:2103.03270) for the Sivers function based on the existing SIDIS +DY data
- Uncertainties are shown for current level of knowledge on up/down Sivers functions at various  $x$  vs  $k_T$  and expected impact from ECCE



[hep-ex:2207.10890](https://arxiv.org/abs/hep-ex/2207.10890)

# Tensor charge impact

- Similar to [Gamberg et al Phys.Lett.B 816 \(2021\) 136255](#) (for YR) use fitting code from latest global fit Cammarota et al arXiv:2002.08384 to extract impact on Transversity, Collins functions and tensor charges
- Together with projected JLAB12 data precision to compare with Lattice results (and check for possible discrepancies)



# Summary

- TMDs provide input on the 3D momentum picture of the nucleon
- Closely related spin-spin (Transversity) and spin-orbit (Sivers function, Boer-Mulders function) effects
- Tensor charge as potential probe for BSM effects
- Full Geant studies show that ECCE/ePIC successfully addresses the TMD/SIDIS measurements of the EIC Yellow Report
- Continuation of evaluation as ePIC detector evolves, impact of kinematic reconstruction methods, prepare for unfolding (PID, tracking), understand radiative corrections, etc



