

# Heavy Quark Coalescence

Exotics and Exotic Phenomena  
in heavy ion collisions

October 1<sup>st</sup>, 2022

APCTP, Pohang



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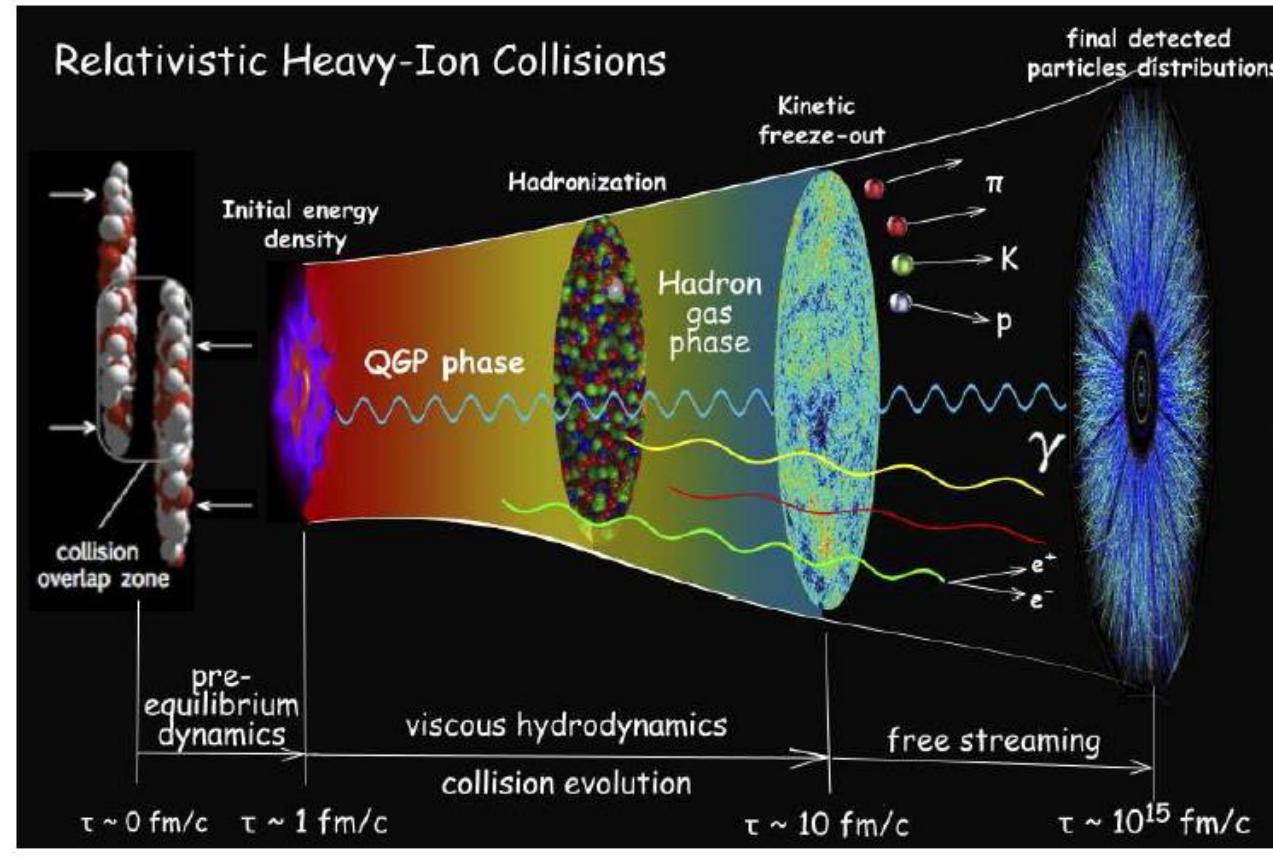


# Outline

- Introduction
- Charmed hadrons in heavy ion collisions
- Hadron production in heavy ion collisions
- Multicharmed and exotic hadron production
- Conclusion

# Introduction

## – Relativistic heavy ion collisions



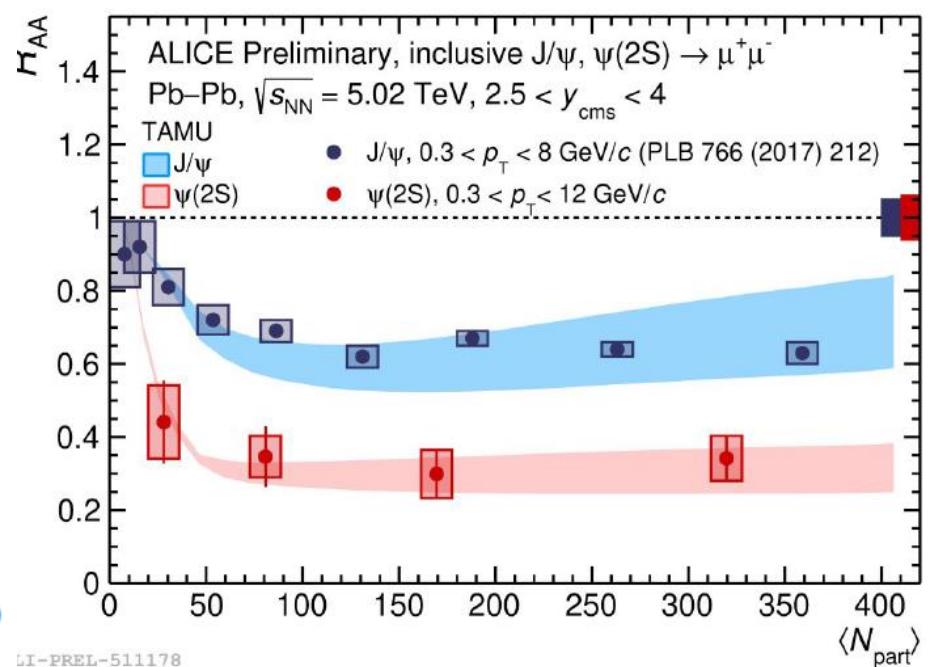
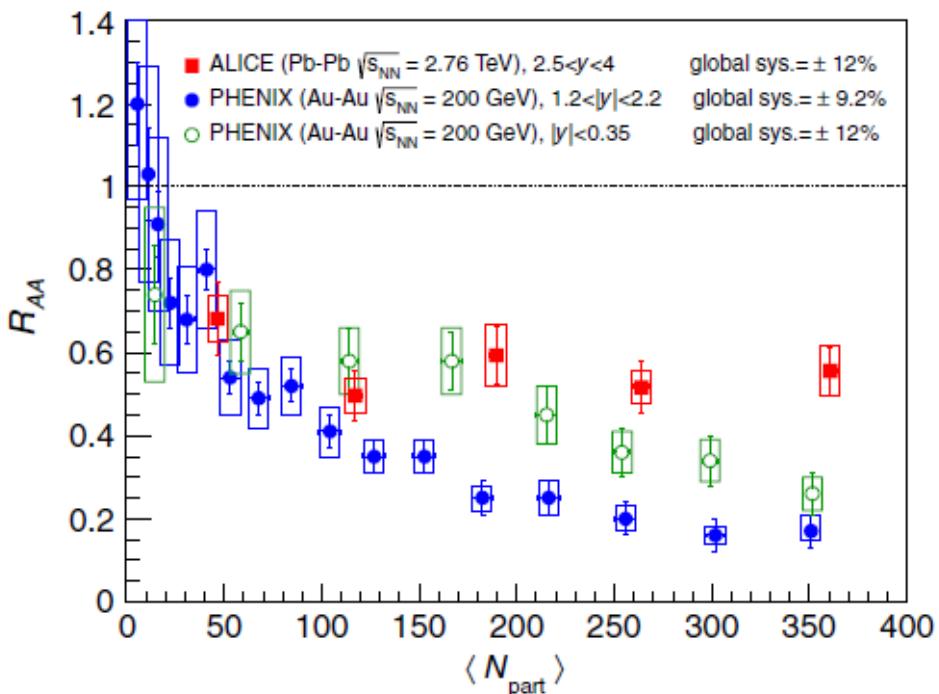
# Charmed hadrons in heavy ion collisions

## – Regeneration of charmonium states

### 1) The nuclear modification factor of charmonium states

B. Abelev et al, (ALICE Collaboration), Phys. Rev. Lett. **109**, 072301

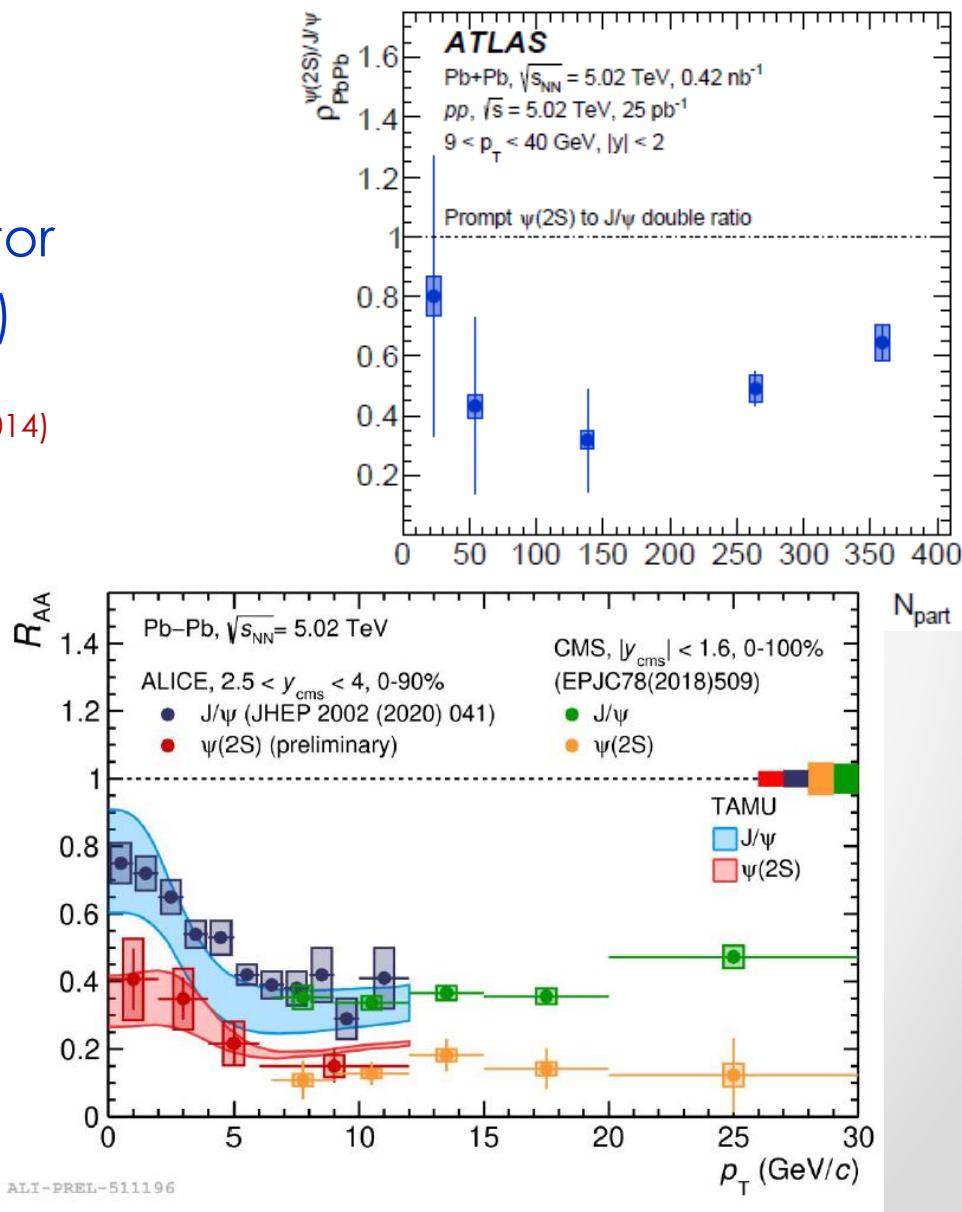
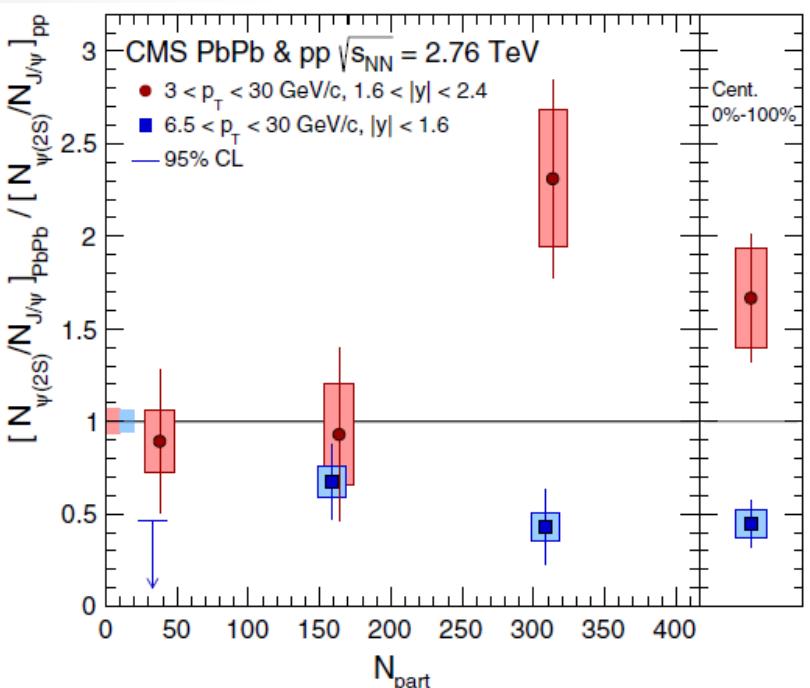
Jon-Are Saetre (Univ. of Bergen), Quark Matter 2022, Krakow, April 4-10



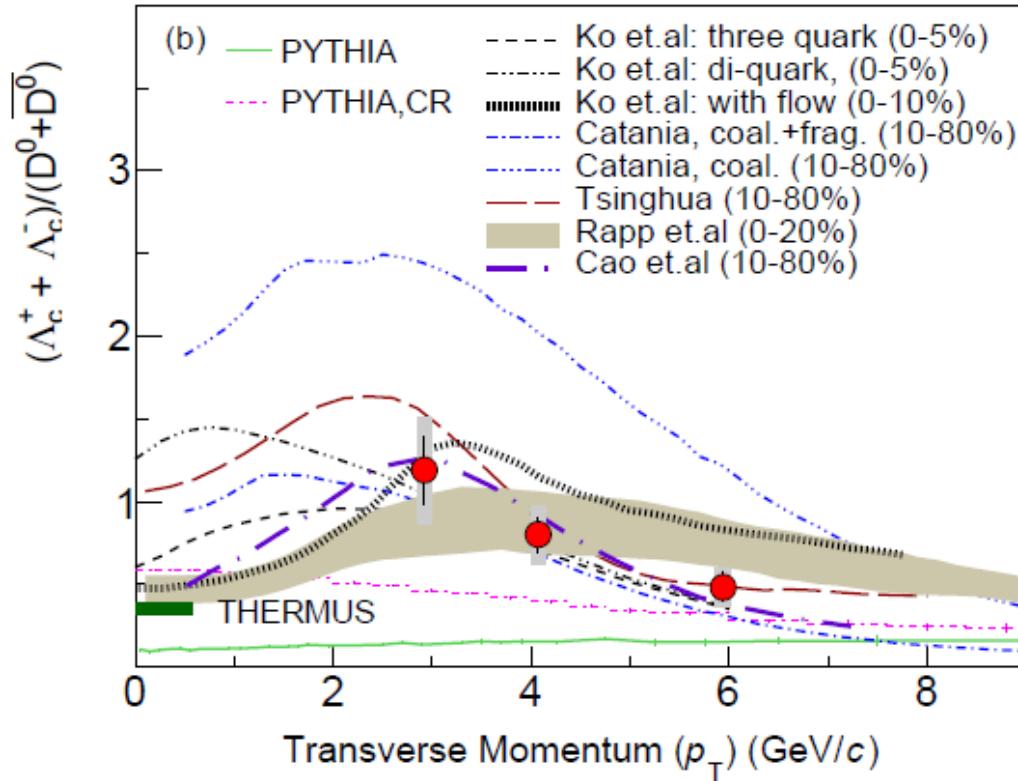
# - Nuclear modification factors of the $J/\psi$ and $\psi(2S)$

## 1) The nuclear modification factor ratio between the $J/\psi$ and $\psi(2S)$

V. Khachatryan et al, Phys. Rev. Lett. **113**, 262301 (2014)  
 M. Aaboud et al, Eur. Phys. J. C **78**, 762 (2018)



# – Regeneration of charmed hadrons : $\Lambda_c/D_0$

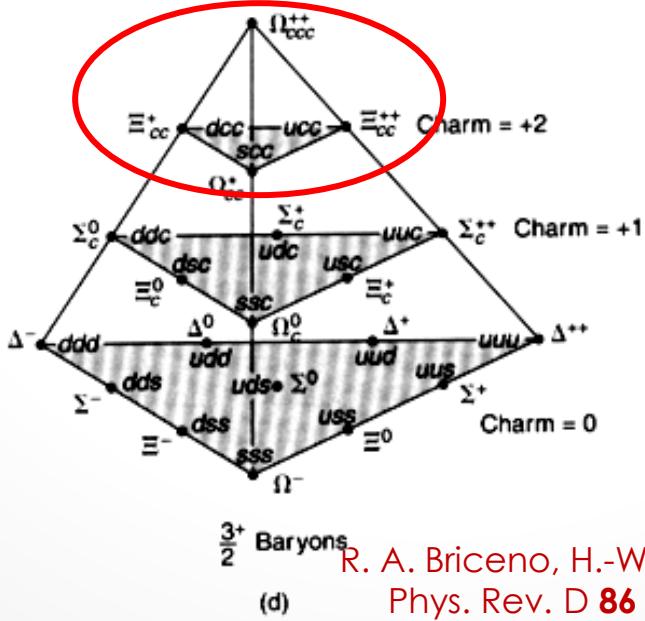
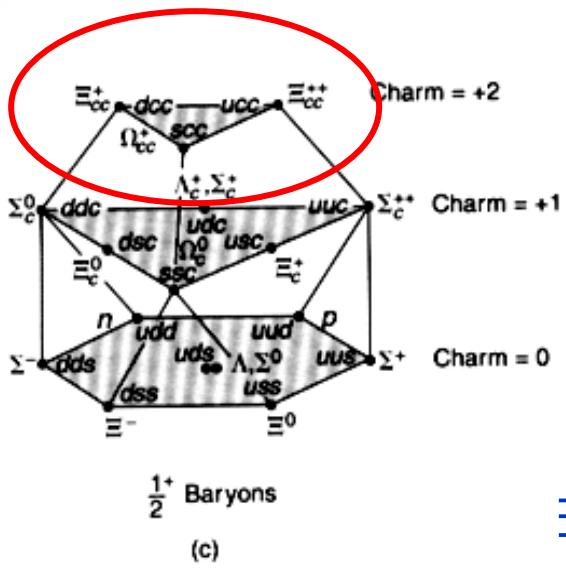
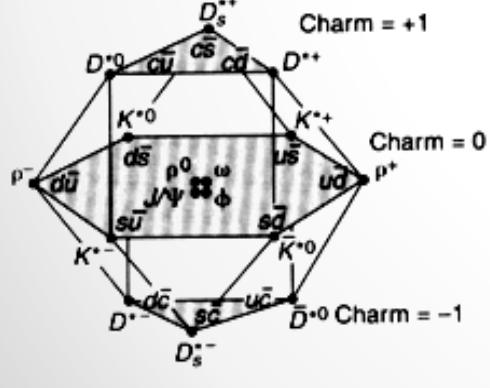
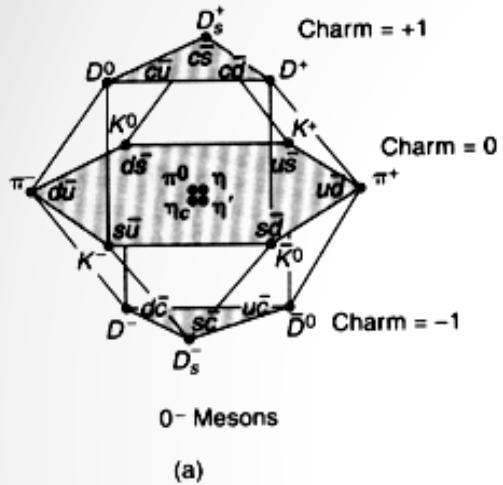


J. Adams et al, (STAR Collaboration), Phys. Rev. Lett. **124**, 172301 (2021)

Y. Oh, C. M. Ko, S. H. Lee, and S. Yasui, Phys. Rev. C **79**, 044905 (2009)

S. Cho, K-J. Sun, C. M. Ko, S. H. Lee, and Y. Oh, Phys. Rev. C **101**, 024909 (2020)

## – Charmed hadrons, SU(4)



## 1) Charmed mesons: $D, D^*, D_s, D_s^*$

2) Singly charmed baryons:  $\Lambda_c(2286)$ ,  
 $\Lambda_c(2595)$ ,  $\Lambda_c(2625)$ ,  
 $\Sigma_c(2455)$ ,  $\Sigma_c(2520)$ ,  
 $(2470)$ ,  $\Xi_c(2578)$ ,  $\Xi_c(2645)$ ,  
 $\Omega_c(2695)$ ,  $\Omega_c(2770)$

### 3) Doubly and triply charmed hadrons, $\Xi_{cc}$ , $\Xi^*_{cc}$ , $\Omega_{cc}$ , $\Omega^*_{cc}$ , $\Omega_{ccc}$

## 4) Exotic hadrons: $T_{cc}$ , X(3872)

## - X(3872) mesons

X(3872)

$I^G(J^{PC}) = 0^+(1^{++})$

J. Beringer *et al.* (PDG), Phys. Rev. D**86**, 010001 (2012)

Mass  $m = 3871.68 \pm 0.17$  MeV

$m_{X(3872)} - m_{J/\psi} = 775 \pm 4$  MeV

$m_{X(3872)} - m_{\psi(2S)}$

Full width  $\Gamma < 1.2$  MeV, CL = 90%

S.K. Choi *et al.* [Belle Collaboration], Phys. Rev. Lett. **90**, 242001 (2003)  $B^\pm \rightarrow K^\pm \pi^+ \pi^- J/\psi$

## - T<sub>cc</sub> (ccqq) mesons

Particle	$m$ [MeV]	$(I, J^P)$
$T_{cc}^1$	3797	(0, 1 <sup>+</sup> )

S. Cho *et al.* (EXHIC Collaboration), Prog. Part. Nucl. Phys. **95**, 279 (2017)

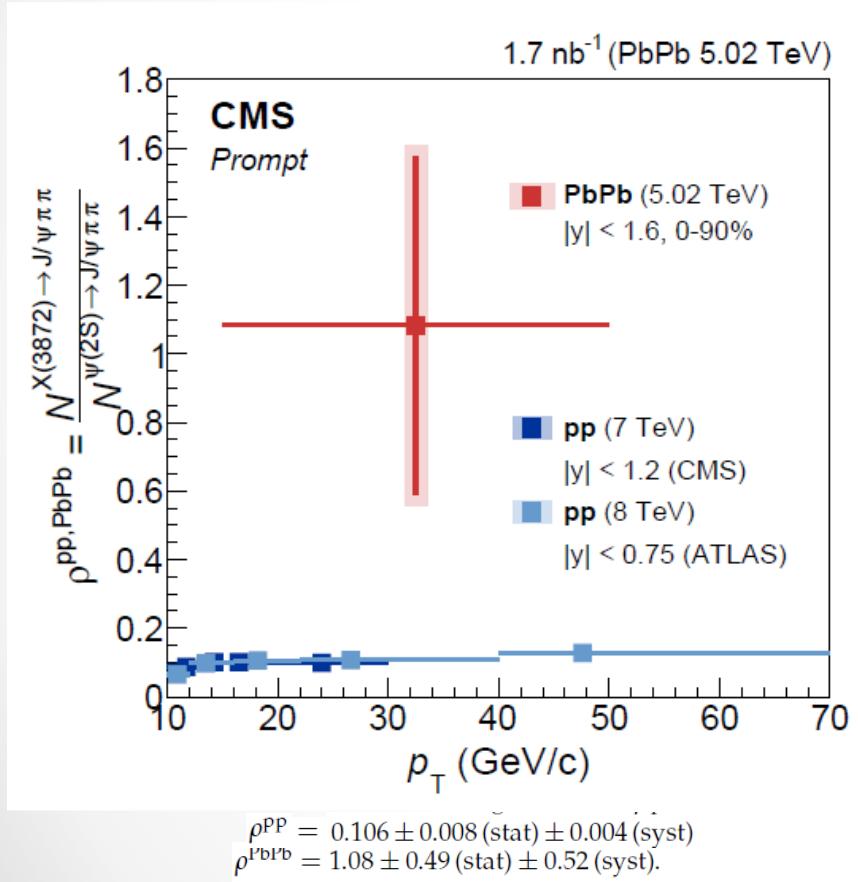
## - Estimated yields of X(3872) and T<sub>cc</sub> mesons

RHIC				LHC				
	$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.	$2q/3q/6q$	$4q/5q/8q$	Mol.	Stat.
$T_{cc}^1$ <sup>a</sup>	—	$4.0 \times 10^{-5}$	$2.4 \times 10^{-5}$	$4.3 \times 10^{-4}$	—	$6.6 \times 10^{-4}$	$4.1 \times 10^{-4}$	$7.1 \times 10^{-3}$
X(3872)	$1.0 \times 10^{-4}$	$4.0 \times 10^{-5}$	$7.8 \times 10^{-4}$	$2.9 \times 10^{-4}$	$1.7 \times 10^{-3}$	$6.6 \times 10^{-4}$	$1.3 \times 10^{-2}$	$4.7 \times 10^{-3}$

<sup>a</sup>Particles that are newly predicted by theoretical model.

S. Cho *et al.* (EXHIC Collaboration), Phys. Rev. C **84**, 064910 (2011)

- Recent measurements of X(3872) in Pb+Pb collisions and an exotic doubly charmed tetraquark, T<sub>cc</sub> in p+p collisions



CERN-EP-2021-165  
LHCb-PAPER-2021-031  
September 2, 2021

## Observation of an exotic narrow doubly charmed tetraquark

LHCb collaboration<sup>†</sup>

### Abstract

Conventional hadronic matter consists of baryons and mesons made of three quarks and quark-antiquark pairs, respectively. The observation of a new type of hadronic state, a doubly charmed tetraquark containing two charm quarks, an anti-u and an anti-d quark, is reported using data collected by the LHCb experiment at the Large Hadron Collider. This exotic state with a mass of about 3875 MeV/c<sup>2</sup> manifests itself as a narrow peak in the mass spectrum of D<sup>0</sup>D<sup>0</sup>π<sup>+</sup> mesons just below the D<sup>+</sup>D<sup>0</sup> mass threshold. The near-threshold mass together with a strikingly narrow width reveals the resonance nature of the state.

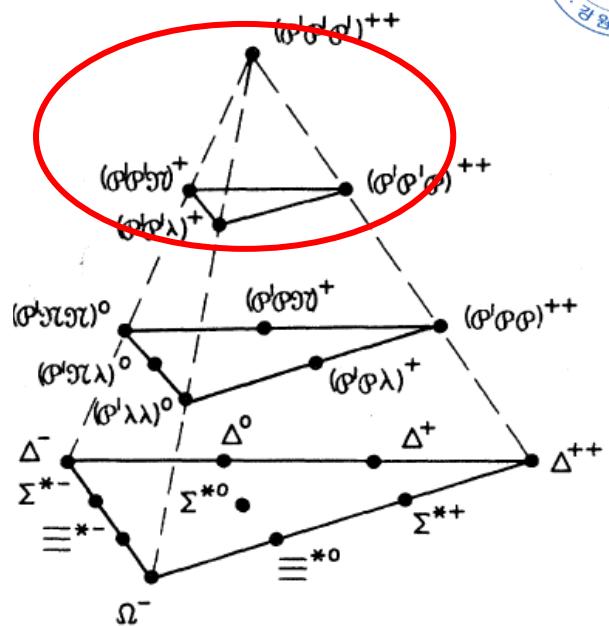
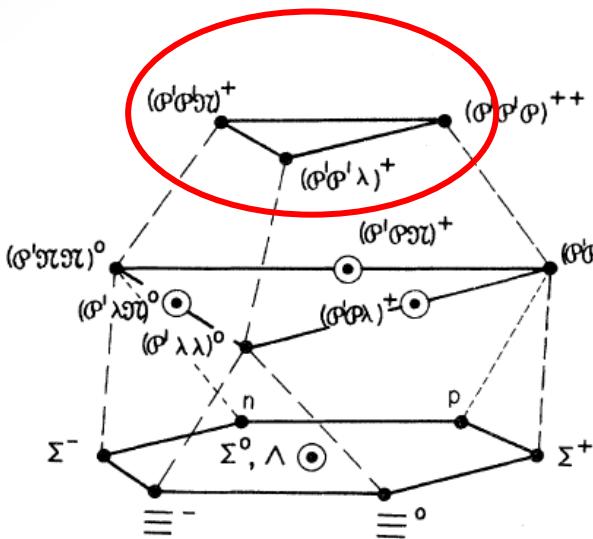
R. Aaij et al. (LHCb Collaboration),  
arXiv:2109.01038

Albert M. Sirunyan et al. [CMS Collaboration],

arXiv: 2102.13048

## - Multicharmed hadrons

A. De Rujula, H. Georgi,  
and S. Glashow  
Phys. Rev. D **12**, 147 (1975)



1) Doubly and triply charmed hadrons,  $\Xi_{cc}$ ,  $\Xi^*_{cc}$ ,  $\Omega_{cc}$ ,  $\Omega^*_{cc}$ ,  $\Omega_{ccc}$

- Observation of the doubly charmed baryon in  
2017

PRL **119**, 112001 (2017)

PHYSICAL REVIEW LETTERS

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15 SEPTEMBER 2017



### Observation of the Doubly Charmed Baryon $\Xi_{cc}^{++}$

R. Aaij *et al.*<sup>\*</sup>

(LHCb Collaboration)

(Received 6 July 2017; revised manuscript received 2 August 2017; published 11 September 2017)

# Hadron production in heavy ion collisions

## – Quark coalescence

V. Greco, C. M. Ko, and P. Levai, Phys. Rev. C **68**, 034904 (2003)

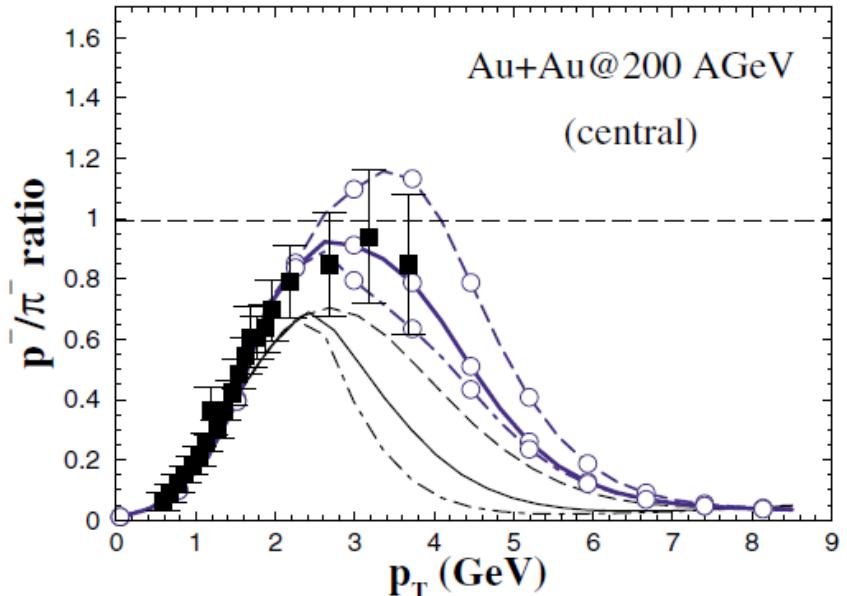
R. J. Freis, B. Muller, C. Nonaka, and S. Bass, Phys. Rev. C **68**, 044902 (2003)

$$N^{Coal} = g \int \left[ \prod_{i=1}^n \frac{1}{g_i} \frac{p_i \cdot d\sigma_i}{(2\pi)^3} \frac{d^3 p_i}{E_i} f(x_i, p_i) \right] f^W(x_1, \dots, x_n : p_1, \dots, p_n)$$

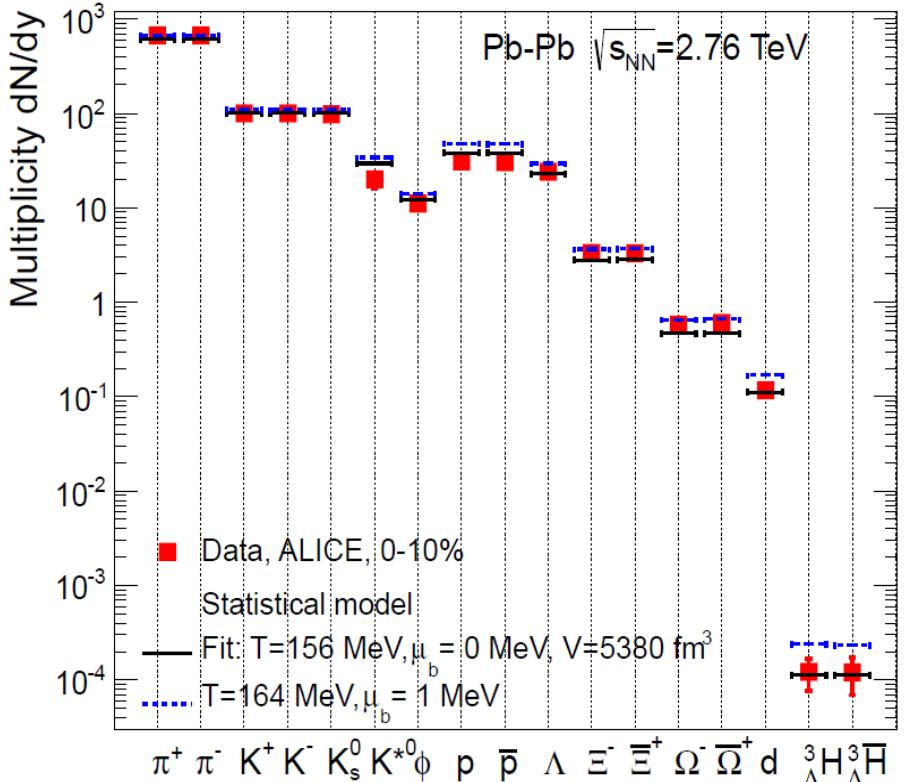
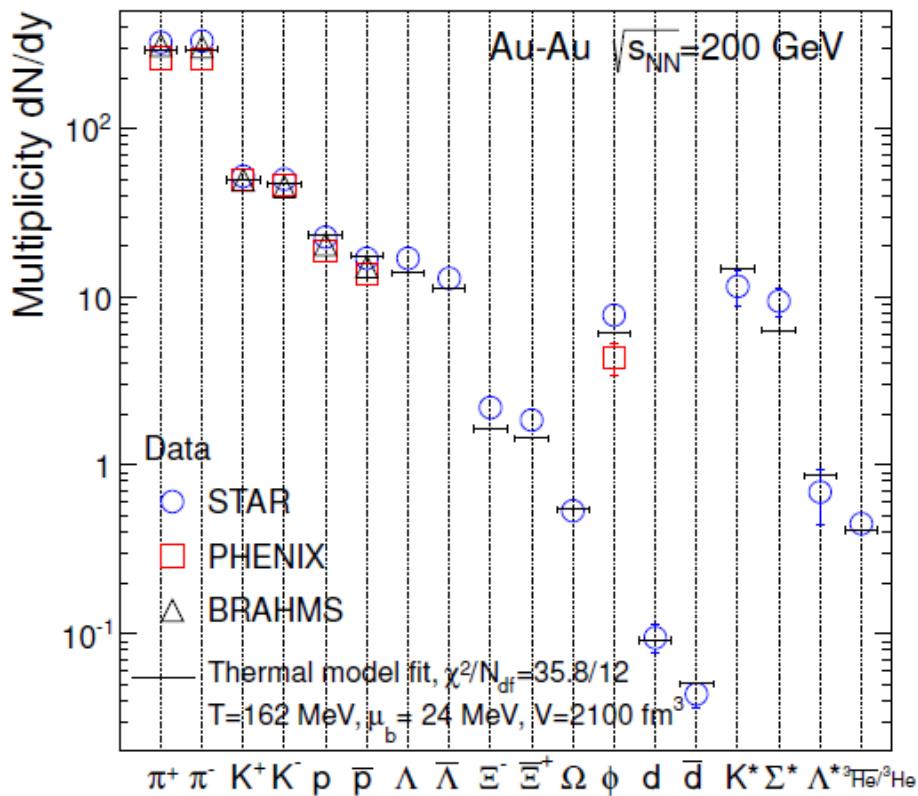
1) The coalescence probability function, the Wigner function

2) Constraints on constituents in the system

$$\int p_i \cdot d\sigma_i \frac{d^3 p_i}{(2\pi)^3 E_i} f(x_i, p_i) = N_i$$



### – Statistical hadronization



A. Andronic, P. Braun-Munzinger, K. Redlich and J. Stachel, Nucl. Phys. A **904-905**, 535c (2013)  
J. Stachel, A. Andronic, P. Braun-Munzinger, and K. Redlich, J. Phys. Conf. Ser. **509**, 012019 (2014)

# Multicharmed and exotic hadron production

- Transverse momentum distribution of multi-charmed hadrons

S. Cho and S. H. Lee, Phys. Rev. C **101**, 024902 (2020)

## 1) Charmed hadron yields in the coalescence model

$$N_{\Xi_{cc}} = g_{\Xi_{cc}} \int p_l \cdot d\sigma_l p_{c_1} \cdot d\sigma_{c_1} p_{c_2} \cdot d\sigma_{c_2} \frac{d^3 \vec{p}_l}{(2\pi)^3 E_l} \frac{d^3 \vec{p}_{c_1}}{(2\pi)^3 E_{c_1}} \frac{d^3 \vec{p}_{c_2}}{(2\pi)^3 E_{c_2}} f_l(r_l, p_l) f_{c_1}(r_{c_1}, p_{c_1}) \\ \times f_{c_2}(r_{c_2}, p_{c_2}) W_{\Xi_{cc}}(r_l, r_{c_1}, r_{c_2}; p_l, p_{c_1}, p_{c_2})$$

$$N_X = g_X \int p_l \cdot d\sigma_l p_{\bar{l}} \cdot d\sigma_{\bar{l}} p_c \cdot d\sigma_c p_{\bar{c}} \cdot d\sigma_{\bar{c}} \frac{d^3 \vec{p}_l}{(2\pi)^3 E_l} \frac{d^3 \vec{p}_{\bar{l}}}{(2\pi)^3 E_{\bar{l}}} \frac{d^3 \vec{p}_c}{(2\pi)^3 E_c} \frac{d^3 \vec{p}_{\bar{c}}}{(2\pi)^3 E_{\bar{c}}} \\ \times f_l(r_l, p_l) f_{\bar{l}}(r_{\bar{l}}, p_{\bar{l}}) f_c(r_c, p_c) f_{\bar{c}}(r_{\bar{c}}, p_{\bar{c}}) W_X(r_l, r_{\bar{l}}, r_c, r_{\bar{c}}; p_l, p_{\bar{l}}, p_c, p_{\bar{c}})$$

## 2) Transverse momentum distributions

$$\frac{d^2 N_{\Xi_{cc}}}{d^2 \vec{p}_T} = \frac{g_{\Xi_{cc}}}{V^2} (2\sqrt{\pi})^6 (\sigma_1 \sigma_2)^3 \int d^2 \vec{p}_{lT} d^2 \vec{p}_{c_1 T} d^2 \vec{p}_{c_2 T} \delta^{(2)}(\vec{p}_T - \vec{p}_{lT} - \vec{p}_{c_1 T} - \vec{p}_{c_2 T}) \frac{d^2 N_l}{d^2 \vec{p}_{lT}} \frac{d^2 N_{c_1}}{d^2 \vec{p}_{c_1 T}} \frac{d^2 N_{c_2}}{d^2 \vec{p}_{c_2 T}} \exp(-\sigma_1^2 k_1^2 - \sigma_2^2 k_2^2).$$

$$\frac{d^2 N_X}{d^2 \vec{p}_T} = \frac{g_X}{V^3} (2\sqrt{\pi})^9 (\sigma_1 \sigma_2 \sigma_3)^3 \int d^2 \vec{p}_{lT} d^2 \vec{p}_{cT} d^2 \vec{p}_{\bar{c}T} d^2 \vec{p}_{\bar{c}T} \delta^{(2)}(\vec{p}_T - \vec{p}_{lT} - \vec{p}_{cT} - \vec{p}_{\bar{c}T} - \vec{p}_{\bar{c}T}) \frac{d^2 N_l}{d^2 \vec{p}_{lT}} \frac{d^2 N_{\bar{l}}}{d^2 \vec{p}_{\bar{l}T}} \\ \times \frac{d^2 N_c}{d^2 \vec{p}_{cT}} \frac{d^2 N_{\bar{c}}}{d^2 \vec{p}_{\bar{c}T}} \exp(-\sigma_1^2 k_1^2 - \sigma_2^2 k_2^2 - \sigma_3^2 k_3^2).$$

## 2) Transverse momentum distributions of charm and light quarks

$$\frac{dN_c}{d^2 p_T} = \begin{cases} a_0 \exp[-a_1 p_T^{a_2}] & p_T \leq p_0 \\ a_0 \exp[-a_1 p_T^{a_2}] + a_3 (1 + p_T^{a_4})^{-a_5} & p_T \geq p_0 \end{cases}$$

$$\frac{d^2 N_l}{d^2 p_T} = g_l \frac{V}{(2\pi)^3} m_T e^{-m_T/T_{eff}},$$

RHIC	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$
$p_T \leq p_0$	0.69	1.22	1.57			
$p_T \geq p_0$	1.08	3.04	0.71	3.79	2.02	3.48
LHC	$a_0$	$a_1$	$a_2$	$a_3$	$a_4$	$a_5$
$p_T \leq p_0$	1.97	0.35	2.47			
$p_T \geq p_0$	7.95	3.49	3.59	87335	0.5	14.31

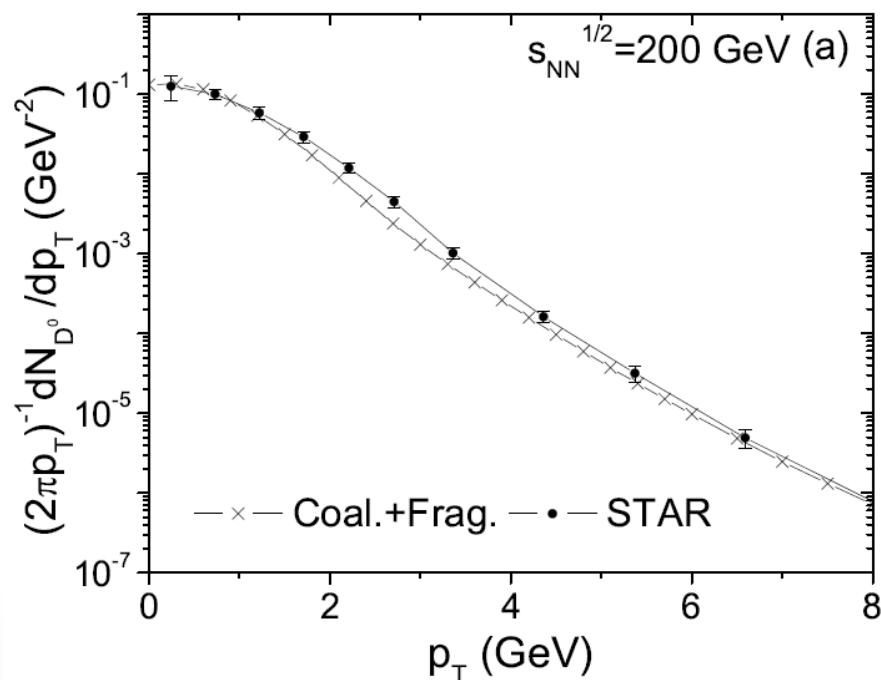
S. Plumari, V. Minissale, S. K. Das, G. Coci and V. Greco, Eur. Phys. J. C **78**:348 (2017)

Y. Oh, C. M. Ko, S.-H. Lee, and S. Yasui, Phys. Rev. C **79** 044905 (2009)

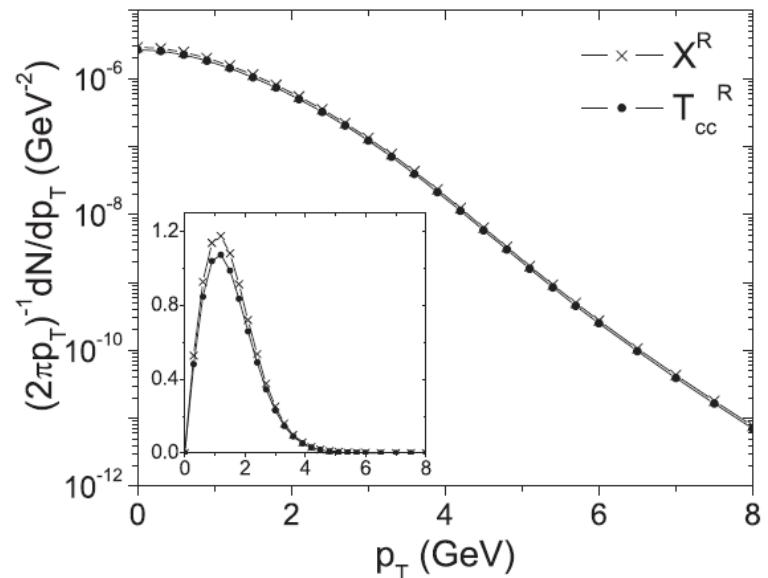
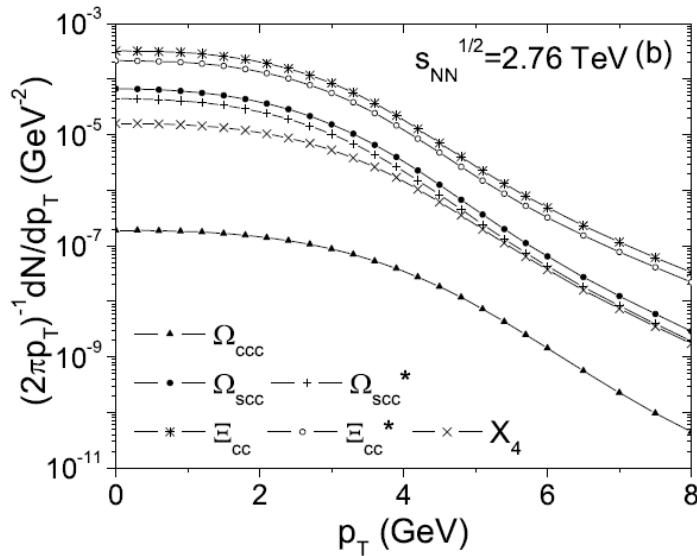
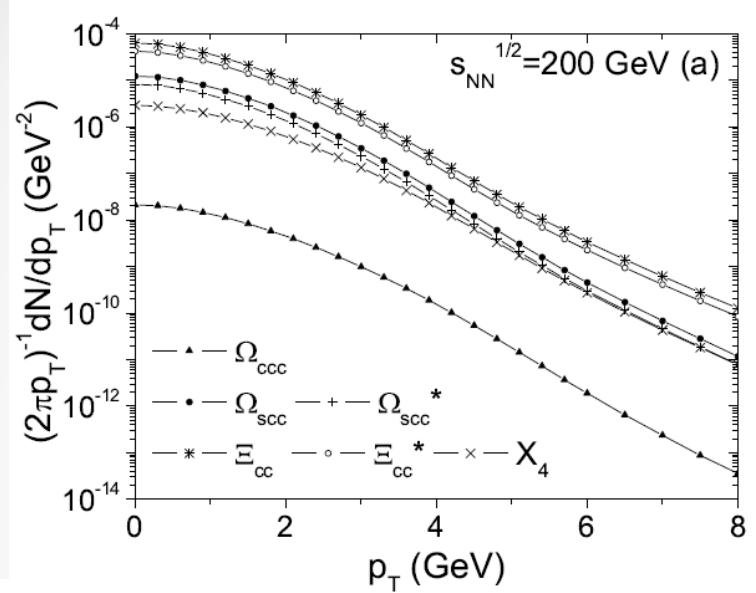
S. Cho et al. (EXHIC Collaboration), Prog. Part. Nucl. Phys. **95**, 279 (2017)

J. Adam et al. [STAR Collaboration], Phys. Rev. C **99**, no. 3, 034908 (2019)

	RHIC		LHC (2.76 TeV)	
	Sc. 1	Sc. 2	Sc. 1	Sc. 2
$T_H$ (MeV)		162		156
$V_H$ (fm <sup>3</sup> )		2100		5380
$\mu_B$ (MeV)		24		0
$\mu_s$ (MeV)		10		0
$\gamma_c$		22		39
$\gamma_b$		$4.0 \times 10^7$		$8.6 \times 10^8$
$T_C$ (MeV)	162	166	156	166
$V_C$ (fm <sup>3</sup> )	2100	1791	5380	3533
$N_u = N_d$	320	302	700	593
$N_s = N_{\bar{s}}$	183	176	386	347
$N_c = N_{\bar{c}}$		4.1		11
$N_b = N_{\bar{b}}$		0.03		0.44



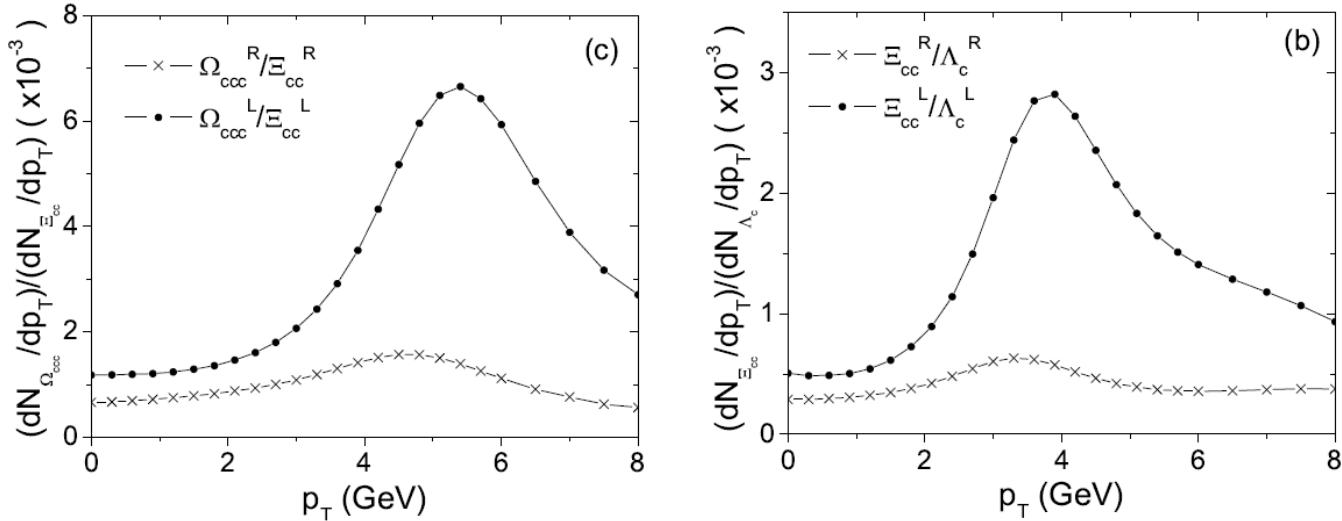
### 3) Transverse momentum distributions of charmed hadrons



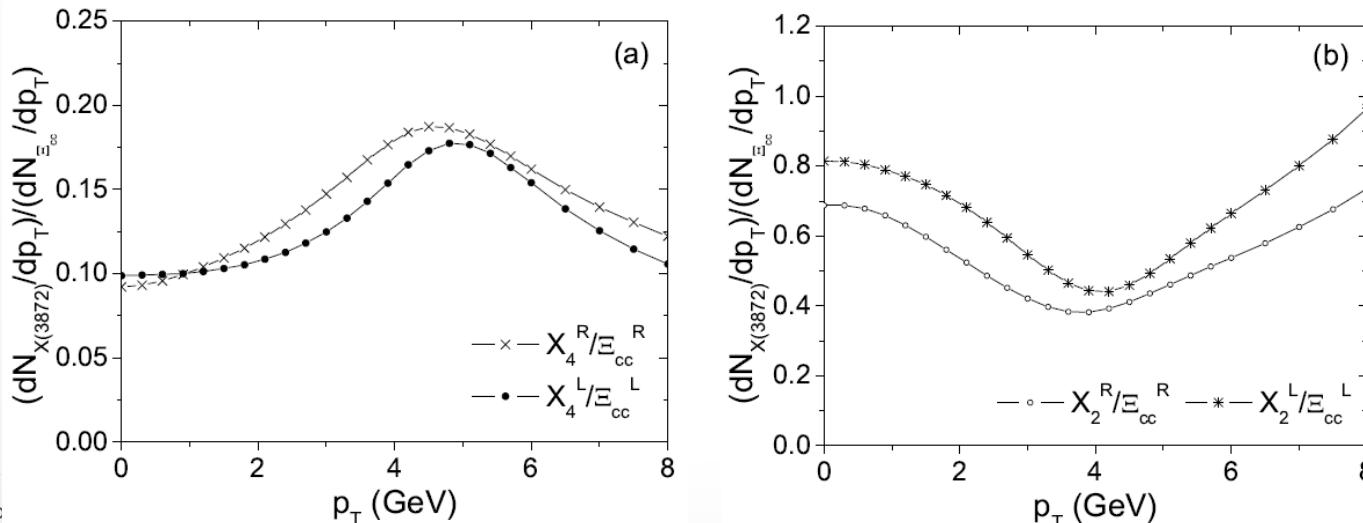
	RHIC	LHC
$\Xi_{cc}$	$4.4 \times 10^{-4}$	$6.7 \times 10^{-3}$
$\Xi_{cc}^*$	$2.9 \times 10^{-4}$	$4.5 \times 10^{-3}$
$\Omega_{scc}$	$8.6 \times 10^{-5}$	$1.3 \times 10^{-3}$
$\Omega_{scc}^*$	$5.7 \times 10^{-5}$	$8.5 \times 10^{-4}$
$\Omega_{ccc}$	$1.7 \times 10^{-7}$	$5.9 \times 10^{-6}$
$T_{cc}$	$2.2 \times 10^{-5}$	$3.8 \times 10^{-4}$
$X_4$	$2.4 \times 10^{-5}$	$3.8 \times 10^{-4}$
$X_2$	$2.6 \times 10^{-4}$	$4.5 \times 10^{-3}$
$D^0$	0.71	6.0
$\Lambda_c$	0.63	4.0

## - Transverse momentum distribution ratios

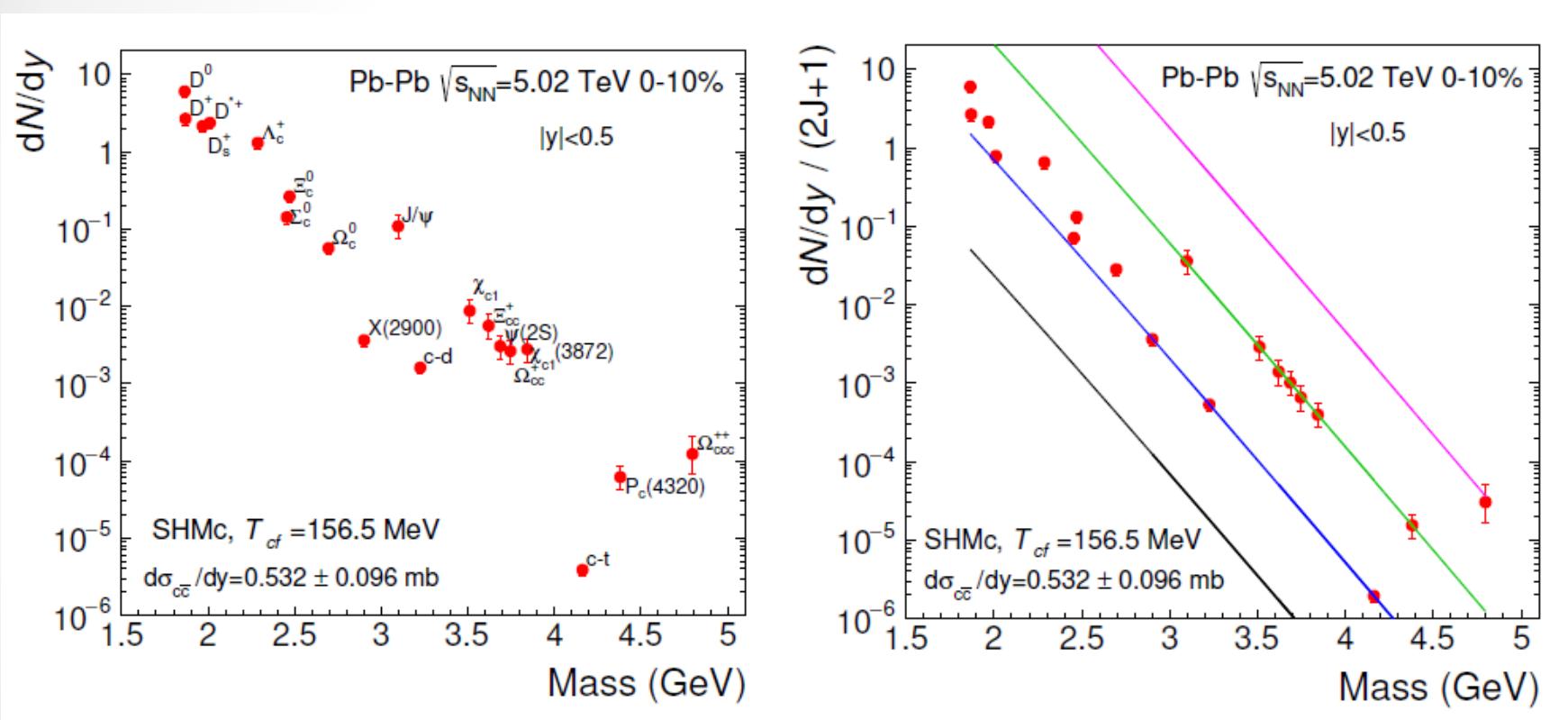
### 1) Baryon/baryon ( $ccc/cca$ , or $ccq/cqq$ )



### 2) Meson/baryon ( $ccqq/cca$ , or $cc/ccb$ )

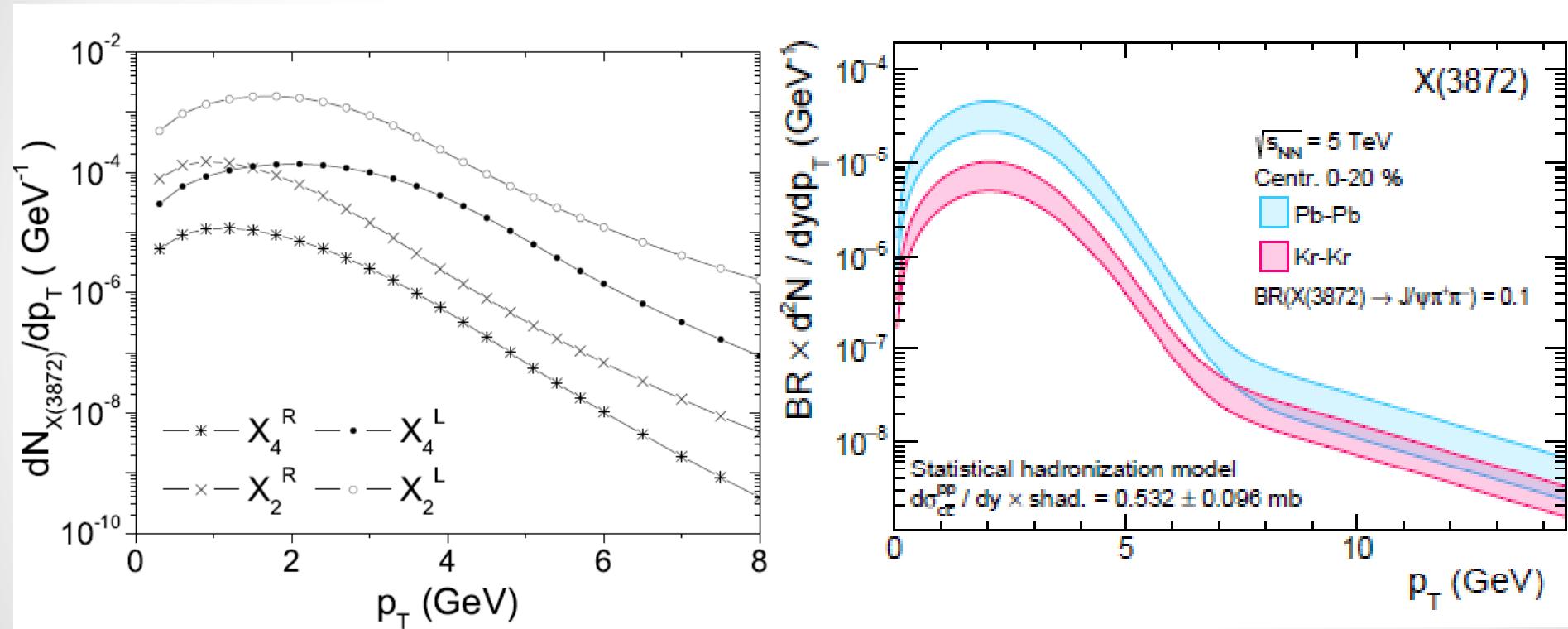


## - The 1<sup>st</sup> comparison with results from the statistical hadronization model



A. Andronic, P. Braun-Munzinger, M. K. Kohler, A. Mazeliauskas, K. Redlich, J. Stachel, and V. Vislavicius, J. High Energy Phys. **2021**, 35 (2021).

- The 2<sup>nd</sup> comparison with results from the statistical hadronization model



A. Andronic, P. Braun-Munzinger, M. K. Kohler, K. Redlich and J. Stachel, Phys. Lett. B **797**, 134836 (2019).

# Conclusions

## – Heavy Quark Coalescence

- 1) Studying production of hadrons in heavy ion collisions can help us to understand hadron production mechanism
- 2) Heavy ion collision experiments provide better chances to study production of multicharm hadrons as well as exotic hadrons
- 3) Transverse momentum distributions are dependent on the internal structure of the hadron
- 4) Transverse momentum distribution ratios between multi-charm hadrons and exotic hadrons, or other combinations between charmed hadrons reflect the internal structure of the exotic hadron



# Thank you for your attention!