

## Long-range structure of $T_{cc}^+$ state

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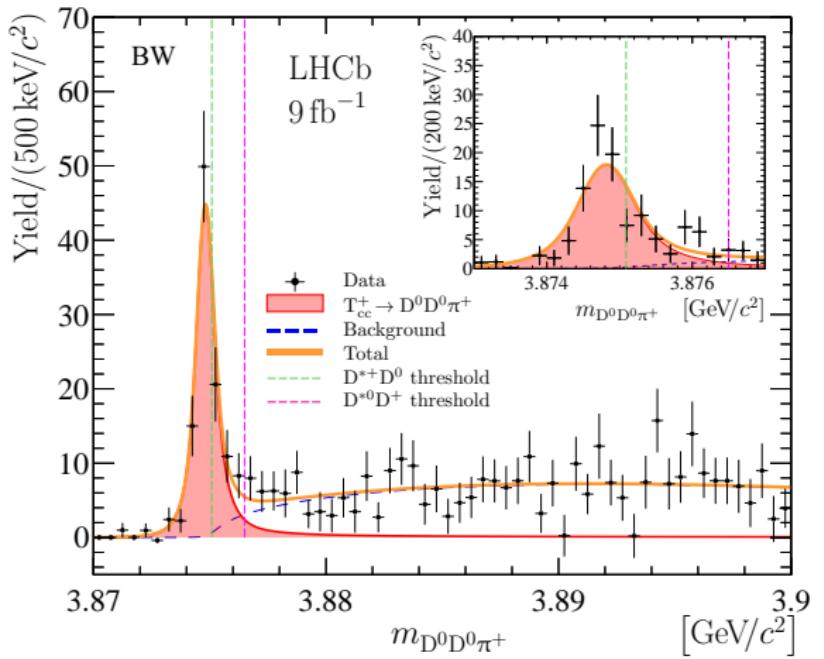
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# Background

# Amazing results in LHCb: observation of $T_{cc}^+$



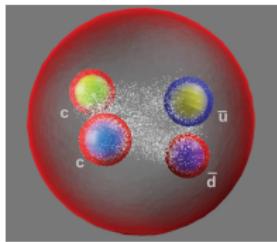
EPS-HEP conference, Ivan Polyakov's talk, 29/07/2021; Nature Physics, 22'

- Prompt production of 3-BODY final states:  
 $D^0\bar{D}^0\pi^+$
- Fitting with Breit-Wigner function
  - $\delta m_{\text{BW}} \equiv m_{T_{cc}} - m_{D^{*+}\bar{D}^0} = -273 \pm 61 \text{ keV}$ ,
  - $\Gamma_{\text{BW}} = 410 \pm 165 \text{ keV}$
  - $\Rightarrow$  Very close to  $D^{*+}\bar{D}^0$  threshold
  - $\Rightarrow$  Very narrow resonance
- The statistical significance of the hypothesis  $\delta m_{\text{BW}} < 0 : 4.3\sigma$

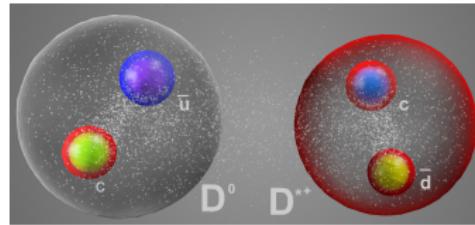
- The second doubly charmed hadron  $\Rightarrow$  manifestly exotic ( $cc\bar{u}\bar{d}$ ), tetraquark !
  - $\Rightarrow QQ\bar{q}\bar{q}$  anticipated and debated for 40 yrs !!!

## Two threads of theoretical works

- Before the observations, there were many theoretical predictions.
- In principle, there are two scenarios (or their hybrid)



Compact tetraquark



Hadronic molecule

- Two threads of history:

⇒ Motivation 1:  $QQ\bar{q}\bar{q}$  is potential STABLE tetraquark state

⇒ Motivation 2: In molecular picture, analog of  $X(3872)$  in the double heavy sector

# History: $QQ\bar{q}\bar{q}$ is potential STABLE tetraquark state

- The potential stable  $QQ\bar{q}\bar{q}$  was first proposed in 1980s

J.P. Ader, J.M. Richard, P. Taxi, PRD25(1982) 2370

*“...On the other hand, the genuine exotic  $QQ\bar{Q}'\bar{Q}'$  can be stable against dissociation if the ratio of the quark masses is large enough.”*

- Further developments

J. Carlson et al, PRD37,744; B. Silvestre-Brac et al,Z.Phys.C57,273-282; Valcarce et al, PLB393,119-123...

- In 2017, the observation of  $\Xi_{cc}^{++}$  in LHCb incited a new round discussions on  $QQ\bar{q}\bar{q}$

⇒ Quark model

Luo et al,EPJC7710,709; Karliner et al,PRL119,202001; Eichten et al,PRL119,202002; W.Park et al,NPA983,1-19,...

⇒ Lattice QCD

A. Francis et al,PRL118,142001; P. Junnarkar et al PRD99,034507; Hadron Spectrum Collaboration, JHEP11,033,...

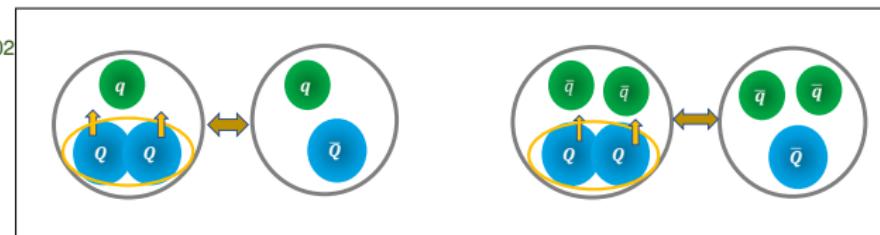
⇒ ...

- E.g: when  $M_Q/m_q \sim \infty$

Eichten et al, PRL119,202002

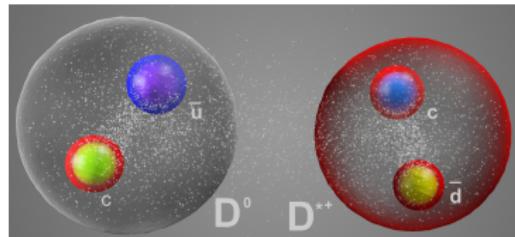
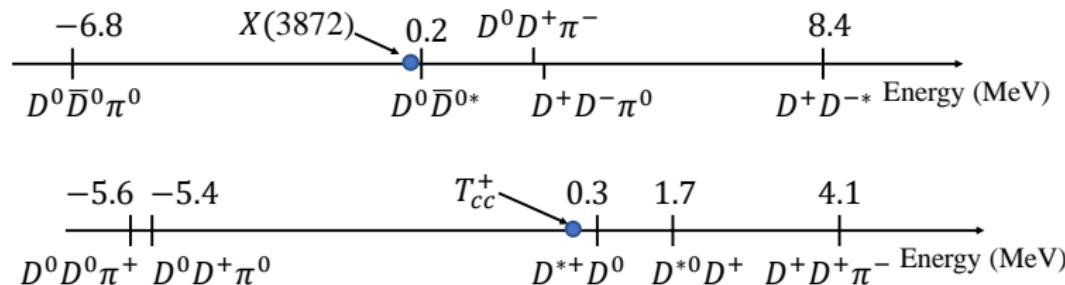
heavy-diquark-heavy-antiquark symmetry

$$(QQ\bar{q}\bar{q}) = (QQq) + (Qqq) - (Q\bar{q})$$



## Molecular scenario: $X(3872)$ and $T_{cc}^+$

- The molecule picture: (1) near-threshold state (2)  $r = \frac{1}{\sqrt{2\mu\delta m_{BW}}} \sim 8\text{fm}$



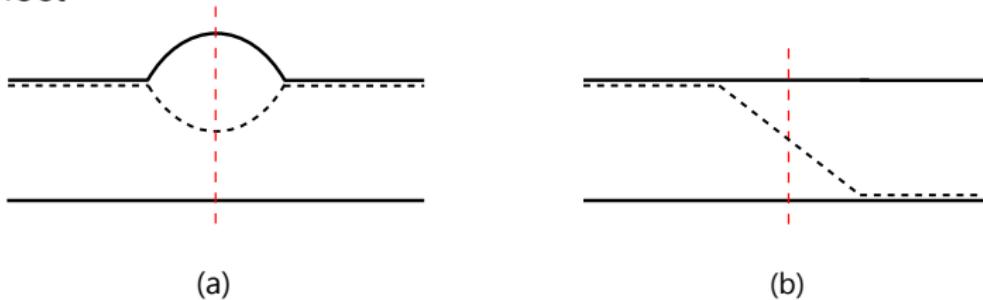
	$X(3872)$	$T_{cc}^+$
Thresh./channels	$\bar{D}^{*0}D^0/\bar{D}^0D^{*0}, \delta m = (0.00 \pm 180) \text{ keV}$ $D^{*-}D^+/D^-D^{*+}$ $J/\psi\rho, J/\psi\omega$	$D^{*+}D^0 : \delta m_{BW} = -273 \pm 61 \text{ keV}$ , $D^{*0}D^+$ None
Possible core	$\chi_{c1}(2P), (c\bar{c}\bar{u}\bar{d})$	$(cc\bar{u}\bar{d})$
Narrow	$\Gamma = (1.19 \pm 0.21) \text{ MeV}$	$\Gamma_{BW} = 410 \pm 165 \text{ keV}$
Isospin violation	$\frac{\mathcal{B}[X \rightarrow J/\psi\omega(\omega \rightarrow 3\pi)]}{\mathcal{B}[X \rightarrow J/\psi\pi^+\pi^-]} \sim 1$	?

- In the isospin symmetry: same one-pion exchange interaction!!!

$$V[\bar{D}^* D / \bar{D} D^*; I(J^{PC}) = 0(1^{++})] = V[D^* D; I(J^P) = 0(1^+)]$$

- Three-body effect

Du:2021zzh,Lin:2022wmj



- Same puzzles for  $X(3872)$  and  $T_{cc}$

⇒ Why they are close to the  $\bar{D}^{*0} D^0$  and  $D^{*0} D^+$  threshold? Fine-tuning?

⇒ Prompt production VS molecular picture?

Bignamini:2009sk,Artoisenet:2009wk,Albaladejo:2017blx,Braaten:2018eov

\*  $T_{cc}$ : Prompt production of 3-BODY final states:  $D^0 D^0 \pi^+$

## History: analog of $X(3872)$

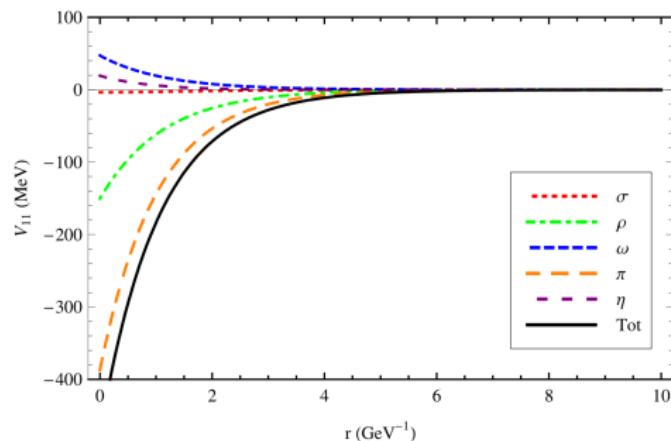
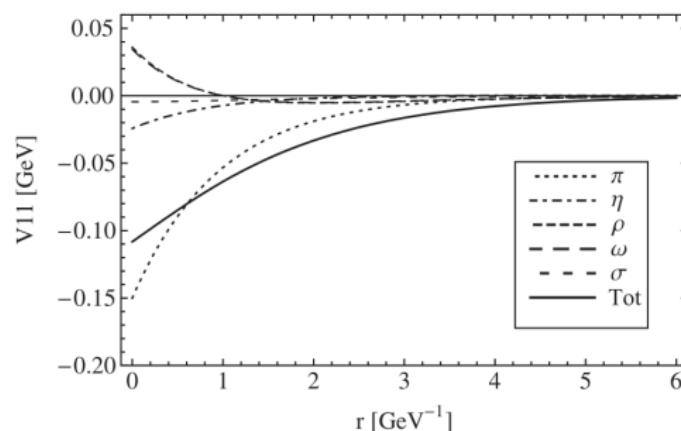
- E.g 1: QCD sum rules: almost degenerate  $T_{cc}$  and  $X(3872)$

J.M.Dias, S.Narison et al, PLB703(2011)274-280

- E.g 2: One-boson-exchange potential  $\pi, \eta, \rho, \omega, \sigma$

N.Li, S.-L.Zhu et al, PRD86(2012)074022, PRD88(2013)114008

⇒ Reproduce the  $X(3872)$  first and predict an  $D^*D$  molecule with  $E_b \sim 400$  keV



- These predictions should be attached more importance.

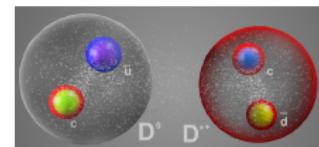
⇒ Experimental similarities between  $X(3872)$  and  $T_{cc}$

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# Strong and radiative decays

# Long-range properties of $T_{cc}$

- Theoretical frameworks for  $X(3872)$  could be immigrated to  $T_{cc}$
- $T_{cc}$  as very loosely bound states:  $\delta m_{BW} \sim 200$  keV,  $r \sim 8$  fm
- Phase-space allowed decays  $T_{cc} \rightarrow DD\gamma$ ,  $T_{cc} \rightarrow DD\pi$ : long-range properties
  - ⇒ Insensitive to the short-range structure
  - ⇒ **Bound information** (e.g.  $\psi$  or  $g_{T_{cc}D^*D}$ ) + **properties of its components**
  - ⇒ Effective field theory (EFT): framework make use of separated scales
- Coupled channels :  $|1\rangle \equiv |D^{*+}D^0\rangle$ ,  $|2\rangle \equiv |D^{*0}D^+\rangle$ 
  - ⇒ Isospin violation effect



- Our work: The BW width ( $410 \pm 165$  keV) is over-estimated.

arXiv:2107.14784, Release in 30/07/2021

- ⇒ Long-range properties can be determined with little uncertainty in NREFT

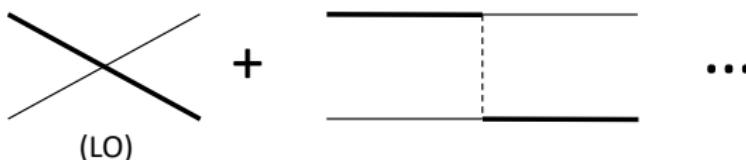
# Effective field theory: scales and power counting

- Power counting: Naive dimensional analysis

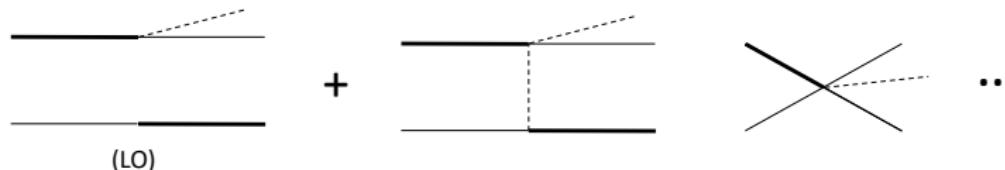
S. Weinberg

⇒ Small scale:  $Q \sim \sqrt{2\delta m_{T_{cc}} \mu_{DD^*}} \sim 20 - 60$  MeV, large scale  $m_\pi$

- Diagram:  $D^* D \rightarrow D^* D$ : LO: contact terms, OPE subleading order

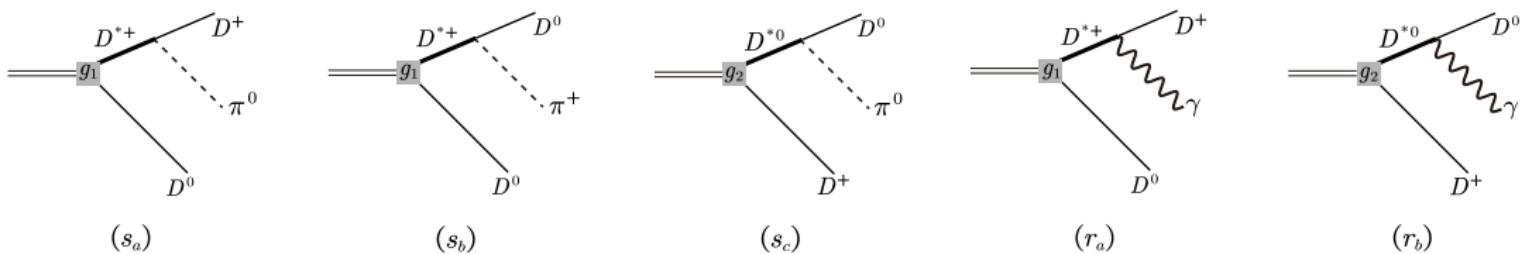


- Diagram:  $D^* D \rightarrow DD\pi$ : LO: One-body operator



- $v_D \sim 0.075$ : Non-relativistic dynamics

# Strong and radiative decays



- Parameters:  $g_1, g_2$  (bound information),  $g_\pi, g_\gamma$  (properties of components)

$\Rightarrow g_\pi$  extracted from  $D^{*+} \rightarrow D^+ \pi^0$  and  $D^{*+} \rightarrow D^0 \pi^+$

$\Rightarrow g_\gamma$  extracted from the partial decay widths of  $D^{*,0} \rightarrow D^{+,0} \gamma$ , take  $\Gamma_{D^{*0}} = 40\text{-}80 \text{ keV}$

$\Rightarrow g_1$  and  $g_2$  extract from the  $D^* D$  scattering or bound state wave function

- Calculation

Similar calculation for  $X(3872)$ : M.B. Voloshin,...

$$\mathcal{A}[D^{*+} \rightarrow D^+ \pi^0] = g_\pi q_\pi \cdot \epsilon_{D^*}, \quad \mathcal{A}[T_{cc}^+ \rightarrow D^+ D^0 \pi^0] = \frac{g_1 \epsilon_T^\mu (g_{\mu\nu} - \frac{p_{12\mu} p_{12\nu}}{m_{D^*}^2}) g_\pi p_2^\nu}{p_{12}^2 - m_{D^*}^2 + i m_{D^*} \Gamma_{D^*}}$$

- Coupled-channel Lippmann-Schwinger equation

$$T = V + VGT,$$

- Extracting  $g_1$  and  $g_2$  from residues of  $T$ -matrix:

$$\lim_{E \rightarrow E_0} (E - E_0) t_{ij} \sim g_j$$

- Contact interaction with cutoff regulator

$$V(\mathbf{p}, \mathbf{p}') = \begin{bmatrix} v_{11}(\Lambda) & v_{12}(\Lambda) \\ v_{12}(\Lambda) & v_{11}(\Lambda) \end{bmatrix} \Theta(\Lambda - p)\Theta(\Lambda - p'),$$

- For 2-channel problem,  $\Lambda$ -dependence of  $v_{ij}(\Lambda)$  can be fixed explicitly make the  $T$ -matrix free of cutoff

⇒ Coupled-channel EFT

Phys.Lett.B 588 (2004) 57-66

## Lippman-Schwinger formalism

$$t = v + vGt,$$

$$G_i(E) = \int^\Lambda \frac{d^3 q}{(2\pi)^3} \frac{1}{E - E_{i,q} + i\epsilon}, \quad E_{i,q} = \delta_i + \frac{q^2}{2\mu}$$

Pole :  $E_0, \kappa_i \equiv \sqrt{2\mu(-E_0 + \delta_i)}$

## Schrodinger formalism

$$(H_0 + V)|\psi\rangle = E_0|\psi\rangle$$

$$\langle \mathbf{p} | \psi \rangle = \cos \theta \phi_1(p) |1\rangle + \sin \theta \phi_2(p) |2\rangle,$$

$$\phi_i(p) \sim \Theta(\Lambda - p)(E_0 - \frac{p^2}{2\mu} - \delta_i)^{-1}$$

- Three equivalent sets of parameters

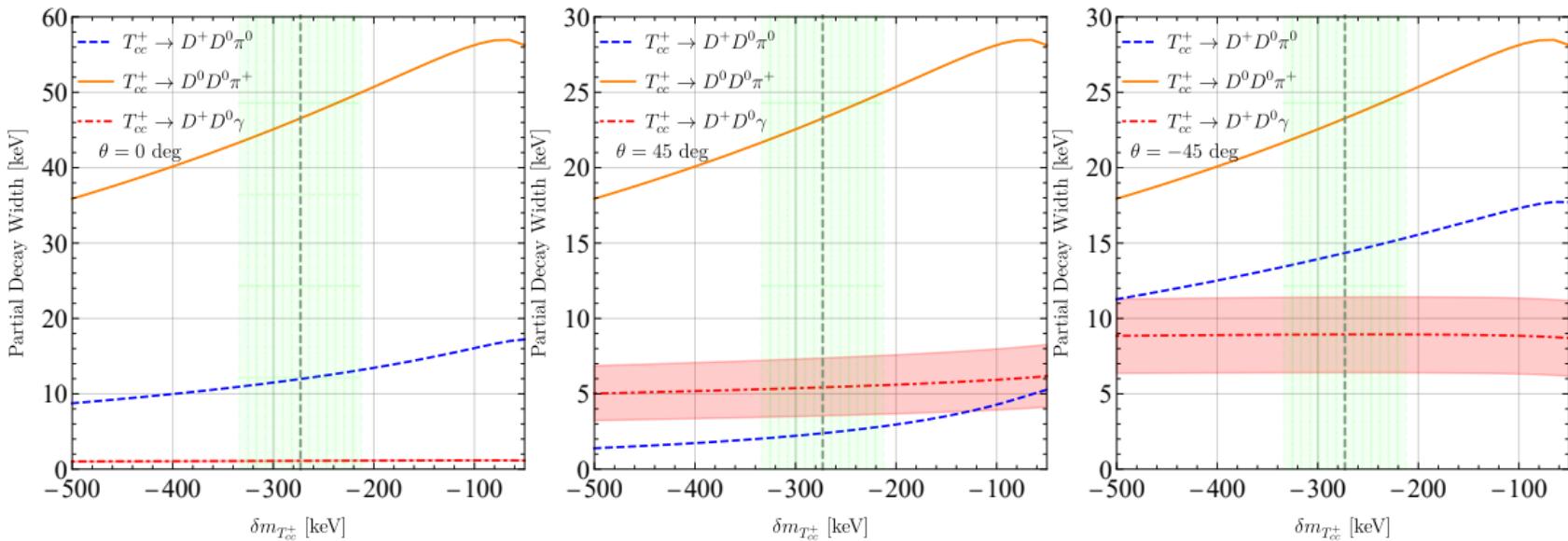
$$\{v_{11}, v_{12}\} \leftrightarrow \{E_0, \theta\} \leftrightarrow \{g_1, g_2\}$$

$\theta$  is mixing angle of the two channel

$$g_1 \sim \sqrt{\kappa_1} \cos \theta, \quad g_2 \sim \sqrt{\kappa_2} \sin \theta.$$

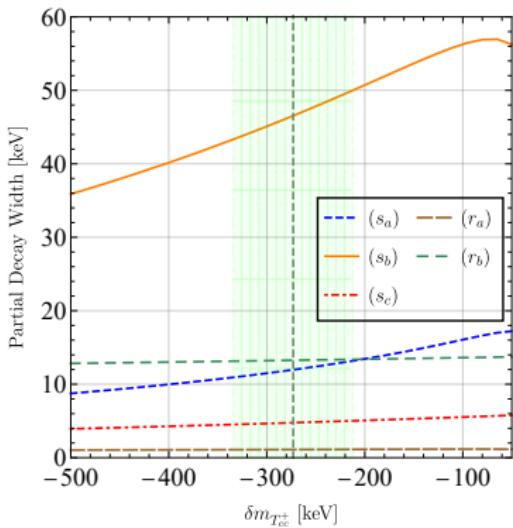
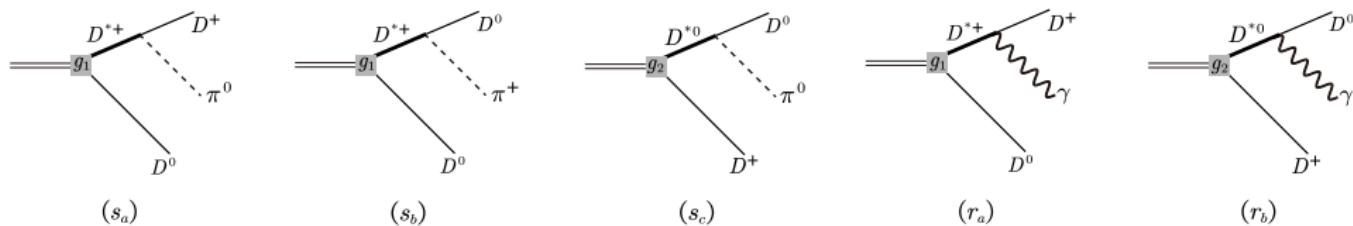
- 1) Renormalization group invariant 2) coupled-channels 3) explicit isospin violation  $\delta_i$

# Numerical results



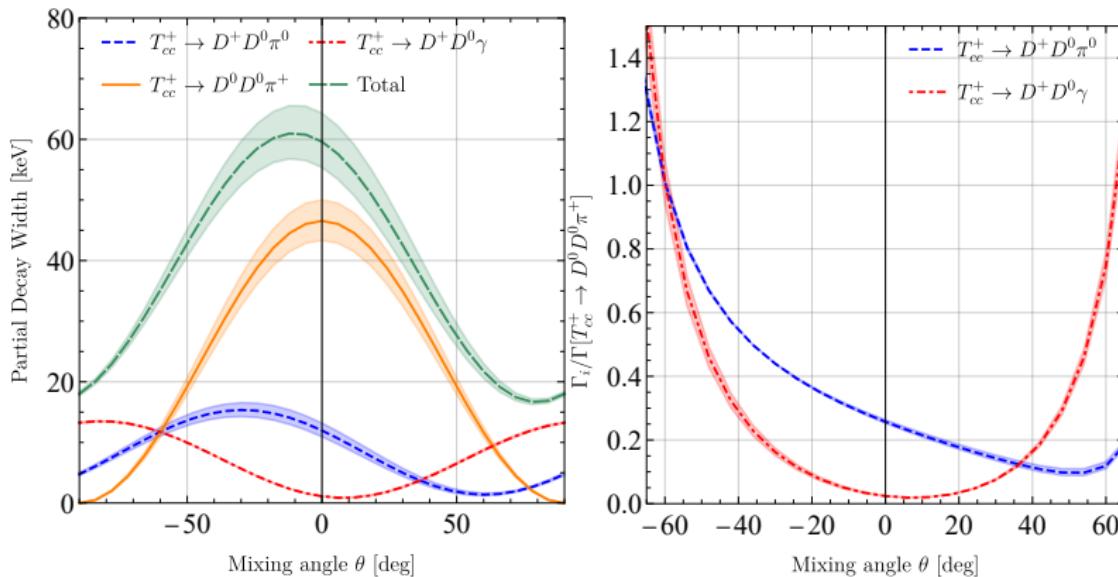
- $\theta = 0$ :  $D^{*+} D^0$  single channel (Left) ;  $\theta = 45$ ,  $I = 1$ (Middle);  $\theta = -45$ :  $I = 0$  (Right).
- The uncertainties:  $\delta m_{T_{cc}^+}$ ,  $\Gamma[D^{*0} \rightarrow D^0 \gamma]$
- The dominant decay mode is  $T_{cc}^+ \rightarrow D^0 D^0 \pi^+$  (observation channel in experiment)

# Amplitude analysis



- Dominant diagrams to the strong interaction ( $s_b$ ):
  - ⇒ Extra isospin factor  $\sqrt{2}$  and constructive interference effect
- Dominant diagrams to the radiative interaction: ( $r_b$ )
  - ⇒ M1 radiative transition roughly proportional to the electric charge of the light quarks

# Final results



- Our results are inconsistent with the BW fitting
- The ratio of partial decay widths is sensitive to the mixing angle

$$\Gamma_{\text{str}} + \Gamma_{\text{EM}} = \begin{cases} 46.7^{+2.7}_{-2.9} \text{ keV} & I = 0 \\ 59.7^{+4.6}_{-4.4} \text{ keV} & I = 1 \end{cases} \quad \text{VS} \quad \Gamma_{\text{BW}} = 410 \pm 165 \text{ keV}$$

$$31.2^{+2.2}_{-2.4} \text{ keV} \quad D^*+D^0$$

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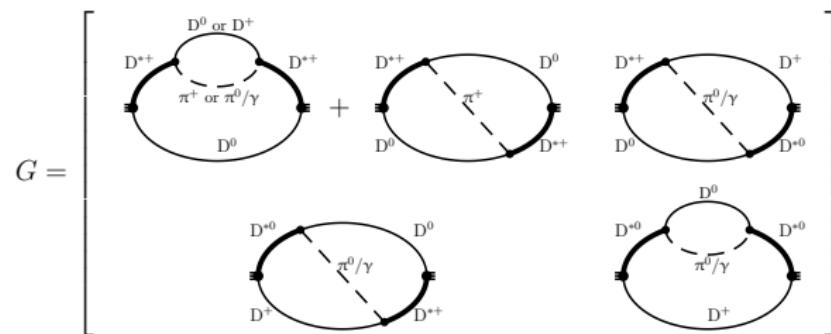
# Discussions

- Similar calculations: assuming  $I = 0$  of  $T_{cc}^+$ ; relativistic framework PLB826,136897;PRD104,116010
- Subleading effects: 2-body operator,  $DD$  FSI, compact tetraquark effect M.-J Yan et al, PRD105,014007
- Coupled-channel approach including 3-body effect:  $\Gamma = 56 \pm 2$  keV Du:2021zzh
- The 2nd analysis from LHCb considering unitary:  $\mathfrak{F}_f^U(s) = \rho_f(s) |[m_U^2 - s - |g|^2 \Sigma(s)]^{-1}|^2$

where  $f \in \{D^0 D^0 \pi^+, D^0 D^+ \pi^0, D^0 D^+ \gamma\}$      $\rho_f(s)$  : 3-body phase space,

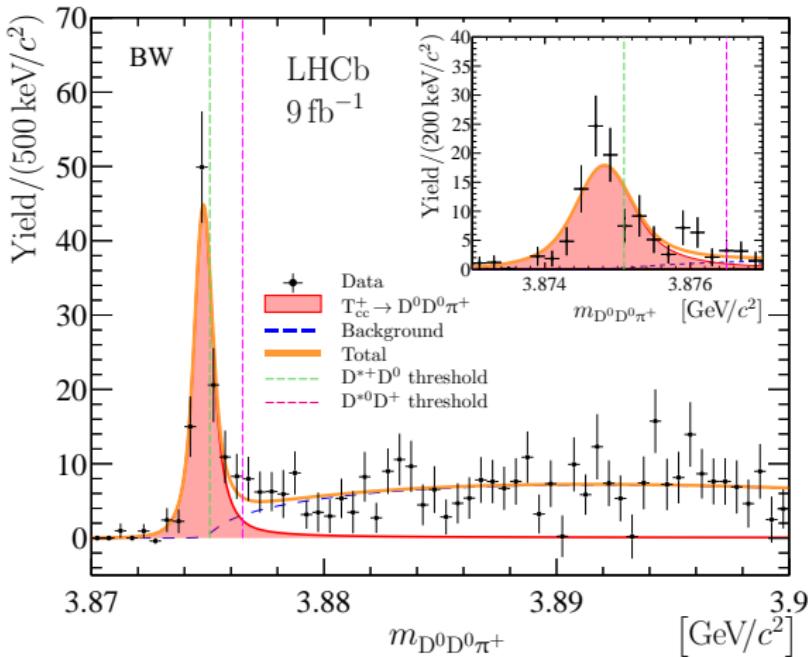
LHCb, Nature Commun. 13 (2022) 1, 3351

$$|g|^2 \Sigma(s) = (g^* - g^*) G \begin{pmatrix} g \\ -g \end{pmatrix}$$



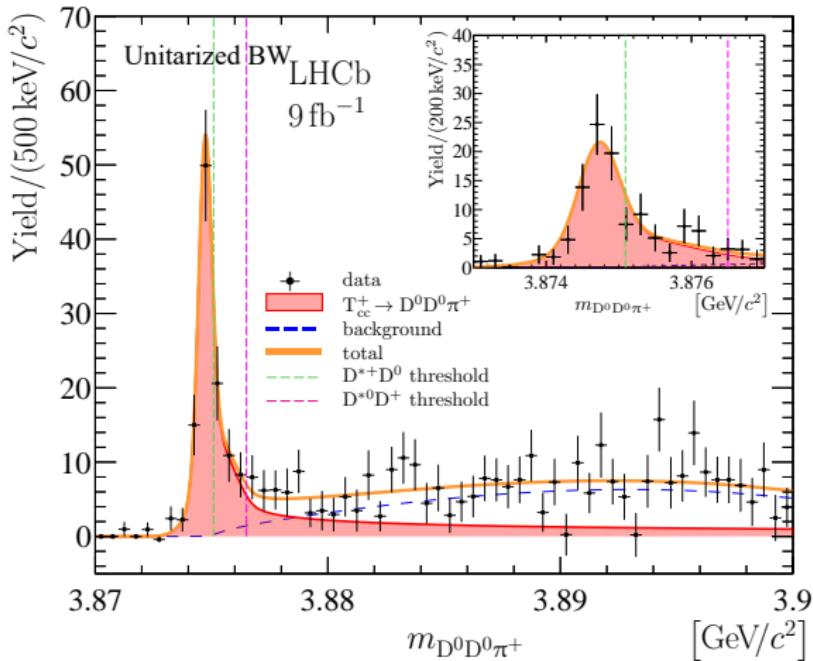
$$\delta m_{pole}^U = -360 \pm 40^{+4}_{-0} \text{ keV}, \Gamma_{pole}^U = 48 \pm 2^{+0}_{-14} \text{ keV}$$

# Related works



EPS-HEP conference, Ivan Polyakov's talk, 29/07/2021; Nature Physics '22

$$\Gamma_{BW} = 410 \pm 165 \text{ keV} \quad \text{VS} \quad \Gamma_{pole}^U = 48 \pm 2^{+0}_{-14} \text{ keV} \quad \text{VS} \quad \Gamma^{I=0} = 46.7^{+2.7}_{-2.9} \text{ keV}$$



LHCb, Nature Commun. 13 (2022) 1, 3351

## Molecular state VS compact tetraquark state

- The present result supports the molecular interpretation
- The closeness to thresholds ( $\sim 200$  keV) need fine-tuning mechanisms Discussions for X(3872):PRD69,074005
  - ⇒ Mechanism 1: fine-tuning of  $D^*D$  potential
  - ⇒ Mechanism 2: fine-tuning of the mass of compact core
- The low-energy properties can not reflect the short structures
  - ⇒ E.g. universal low energy properties for system ( $\frac{1}{a_s} \sim \sqrt{2\mu E_B} \ll m_\pi$ ) PRD69,074005
- The proportion of the compact core could be small (decreasing with mass approaching threshold), but it could be important to generate the bound state PRD105,116024
- To uncover the short-range structure → processes associated with higher energy scale
  - ⇒ Prompt production ( pp collision, heavy ion collision)
  - ⇒ ...

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# Summary

- In the molecular scheme, the strong and radiative decays of  $T_{cc}^+$  are investigated

$$\Gamma_{BW} = 410 \pm 165 \text{ keV} \quad \text{VS} \quad \Gamma_{pole}^U = 48 \pm 2^{+0}_{-14} \text{ keV} \quad \text{VS} \quad \Gamma^{I=0} = 46.7^{+2.7}_{-2.9} \text{ keV}$$

- ⇒ Inconsistent with the original experimental analysis (even considering the uncertainties)
- ⇒ Coincide with the unitarized analysis
- Coupled channel EFT: 1)  $\Lambda$ -independent 2) coupled-channels 3) explicit isospin violation
- The separation of the long-range dynamics and short-range dynamics
  - ⇒ The long-range dynamics can be determined by only two parameters  $E_b$  and  $\theta$
  - ⇒ Two edge sword: the short-range structure is hard to detect
- Remaining puzzles
  - ⇒ Prompt production, relation of X(3872) and  $T_{cc}$ , fine-tuning mechanisms, short range interaction and structures,...

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# Thanks for your attention!