

Hadron induced Charmonium production

Reimei workshop "Hadrons in dense matter at J-PARC"

21-23 Feb. 2022, KEK Tokai.

Gy. Wolf

Wigner RCP

in collaboration with G. Balassa, P. Kovács, M. Zétényi, Wigner RCP
Su Houn Lee, Yonsei University, Korea

- Motivation
- Transport
- hadron(\bar{p}, π, p)A reaction (PANDA, JPARC?)

Gy. Wolf, G. Balassa, P. Kovács, M. Zétényi, S.H. Lee,

Act. Phys. Pol. B10 (2017) 1177, arxiv:1711.10372

Phys. Lett. B780 (2018) 25, arXiv:1712.06537

Act. Phys. Pol. B11 (2018) 531

Gluon condensate in matter

Quark and gluon condensates are known in vacuum, in matter:

$$\langle n.m. | O | n.m. \rangle = \langle 0 | O | 0 \rangle + \int d^3p/p_0 f_N(p, \mu) \langle N | O | N \rangle$$

we need to know $\langle N | \bar{q}q | N \rangle$ and $\langle N | \alpha_s G^2 | N \rangle$

Trace anomaly:

$$T_{\mu}^{QCD\mu} = \frac{\beta}{2g} G_{\mu\nu}^a G^{a\mu\nu} + m\bar{q}q$$

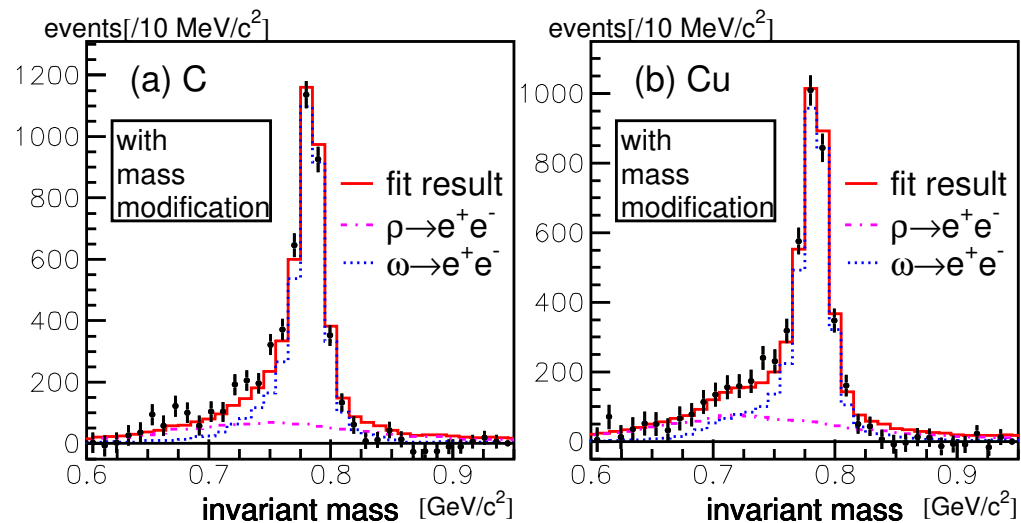
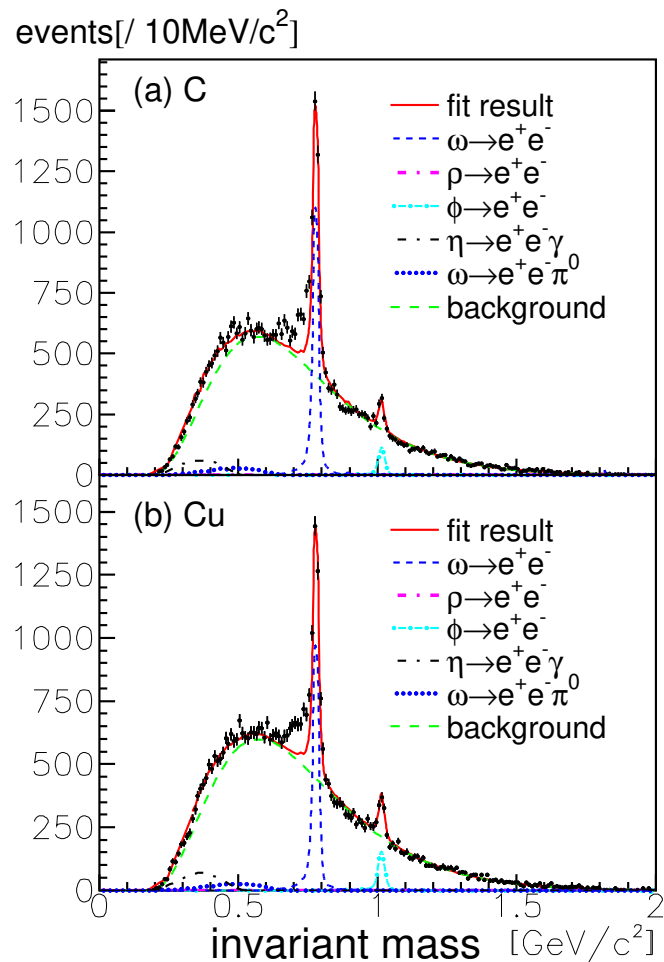
Between vacuum states: energy of the vacuum. Between nucleons

$$m_N \bar{u}(p)u(p) = \langle N(p) | \frac{\beta}{2g} G_{\mu\nu}^a G^{a\mu\nu} + m\bar{q}q | N(p) \rangle$$

contribution of light quarks (πN scattering, σ -term): ≈ 50 MeV,

gluons contribution to the mass of the proton: ≈ 750 MeV

KEK E325 12 GeV pA data ρ and ω



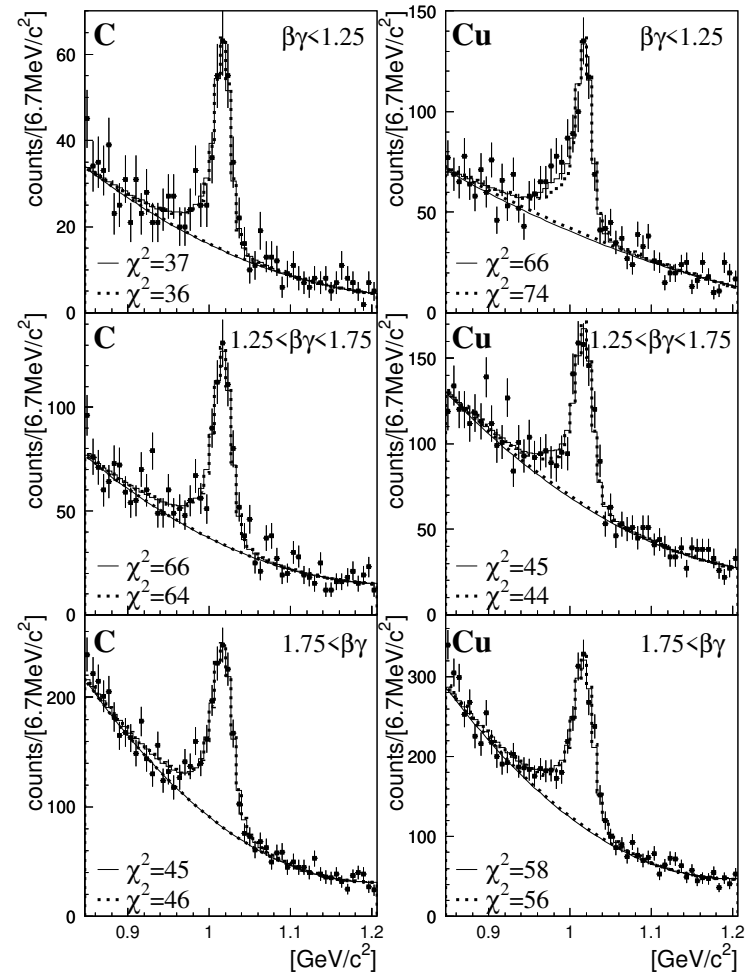
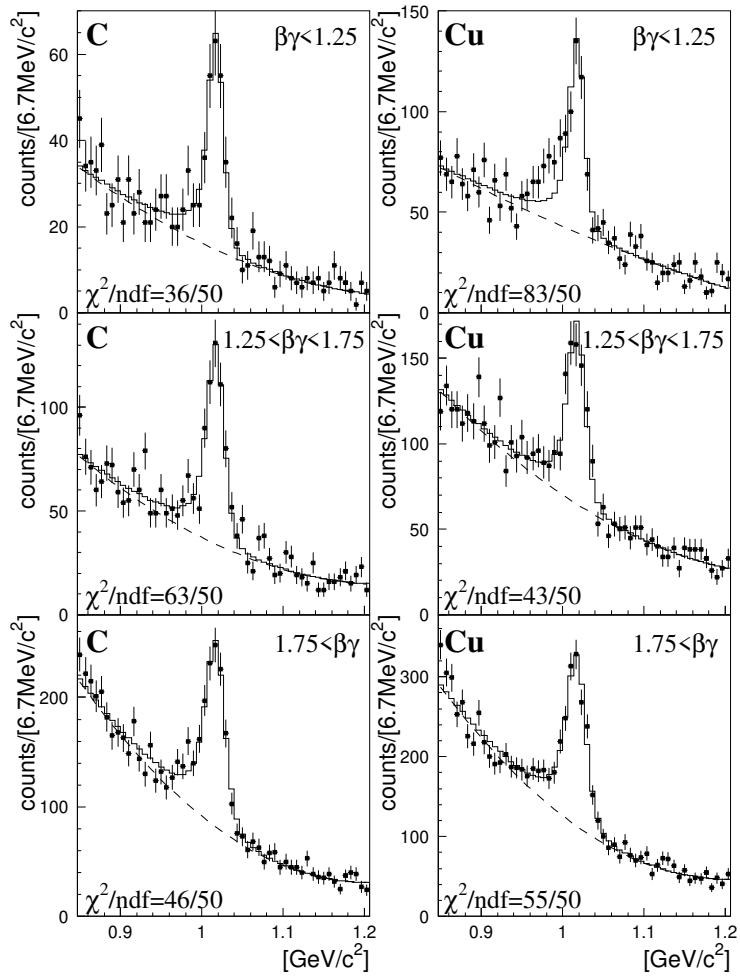
$$m(\rho)/m(0) = 1 - 0.09(\rho/\rho_0)$$

no broadening

M. Naruki *et al.*

Phys. Rev. Lett. 96 (2006) 092301

KEK E325 12 GeV pA data for ϕ



$$m(\rho)/m(0) = 1 - 0.033(\rho/\rho_0)$$

$$\Gamma(\rho)/\Gamma(0) = 3.6(\rho/\rho_0)$$

R. Muto *et al.*

Phys. Rev. Lett. 98 (2007) 042501



$$\frac{\partial F}{\partial t} + \frac{\partial H}{\partial \mathbf{p}} \frac{\partial F}{\partial \mathbf{x}} - \frac{\partial H}{\partial \mathbf{x}} \frac{\partial F}{\partial \mathbf{p}} = \mathcal{C}, \quad H = \sqrt{(m_0 + U(\mathbf{p}, \mathbf{x}))^2 + \mathbf{p}^2}$$

- potential: momentum dependent, soft: K=215 MeV

$$U^{nr} = A \frac{n}{n_0} + B \left(\frac{n}{n_0} \right)^\tau + C \frac{2}{n_0} \int \frac{d^3 p'}{(2\pi)^3} \frac{f_N(x, p')}{1 + \left(\frac{\mathbf{p} - \mathbf{p}'}{\Lambda} \right)^2},$$

- testparticle method

$$F = \sum_{i=1}^{N_{test}} \delta^{(3)}(\mathbf{x} - \mathbf{x}_i(t)) \delta^{(4)}(p - p_i(t)).$$

- Unknown cross sections: Statistical bootstrap:

G. Balassa, P. Kovács, Gy. Wolf, Eur. Phys. J. A54 (2018) 25,

Gy. Wolf et al., Phys.Atom.Nucl. 75 (2012) 718-720

Gy. Wolf, M. Zetenyi, Eur.Phys.J. A52 (2016) 258

M. Zetenyi, Gy. Wolf, Phys.Lett. B785 (2018) 226

Spectral equilibration

- medium effects on the spectrum of hadrons (vector mesons)
- how they get on-shell (energy-momentum conservation)
- Field theoretical method (Kadanoff-Baym equation)
B. Schenke, C. Greiner, Phys.Rev.C73:034909,2006
- Off-shell transport
W. Cassing, S. Juchem, Nucl.Phys. A672 (2000) 417
S. Leupold, Nucl.Phys. A672 (2000) 475
- Spectral equilibration: Markov or memory effect

Off-shell transport

- Kadanoff-Baym equation for retarded Green-function
Wigner-transformation, gradient expansion

- transport equation for $F_\alpha = f_\alpha(x, p, t)A_\alpha$

$$A(p) = -2ImG^{ret} = \frac{\hat{\Gamma}}{(E^2 - \mathbf{p}^2 - m_0^2 - \text{Re}\Sigma^{ret})^2 + \frac{1}{4}\hat{\Gamma}^2},$$

W. Cassing, S. Juchem, Nucl.Phys. A672 (2000) 417

S. Leupold, Nucl.Phys. A672 (2000) 475

- testparticle approximation

Transport equations

- $$\frac{d\vec{X}_i}{dt} = \frac{1}{1-C_{(i)}} \frac{1}{2\epsilon_i} \left[2\vec{P}_i + \vec{\nabla}_{P_i} \text{Re}\Sigma_{(i)}^{\text{ret}} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\text{Im}\Sigma_{(i)}^{\text{ret}}} \vec{\nabla}_{P_i} \text{Im}\Sigma_{(i)}^{\text{ret}} \right]$$

$$\frac{d\vec{P}_i}{dt} = -\frac{1}{1-C_{(i)}} \frac{1}{2\epsilon_i} \left[\vec{\nabla}_{X_i} \text{Re}\Sigma_{(i)}^{\text{ret}} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\text{Im}\Sigma_{(i)}^{\text{ret}}} \vec{\nabla}_{X_i} \text{Im}\Sigma_{(i)}^{\text{ret}} \right]$$

$$\frac{d\epsilon_i}{dt} = \frac{1}{1-C_{(i)}} \frac{1}{2\epsilon_i} \left[\frac{\partial \text{Re}\Sigma_{(i)}^{\text{ret}}}{\partial t} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\text{Im}\Sigma_{(i)}^{\text{ret}}} \frac{\partial \text{Im}\Sigma_{(i)}^{\text{ret}}}{\partial t} \right]$$

- where $C_{(i)}$ renormalization factor

$$C_{(i)} = \frac{1}{2\epsilon_i} \left[\frac{\partial}{\partial \epsilon_i} \text{Re}\Sigma_{(i)}^{\text{ret}} + \frac{\epsilon_i^2 - \vec{P}_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\text{Im}\Sigma_{(i)}^{\text{ret}}} \frac{\partial}{\partial \epsilon_i} \text{Im}\Sigma_{(i)}^{\text{ret}} \right]$$

- the last equation for homogenous system can be rewritten as

$$\frac{dM_i^2}{dt} = \frac{d(\epsilon_i^2 - P_i^2)}{dt} = \frac{d\text{Re}\Sigma_{(i)}^{\text{ret}}}{dt} + \frac{M_i^2 - M_0^2 - \text{Re}\Sigma_{(i)}^{\text{ret}}}{\text{Im}\Sigma_{(i)}^{\text{ret}}} \frac{d\text{Im}\Sigma_{(i)}^{\text{ret}}}{dt}$$

Charmonium in vacuum and in matter

- Charmonium: J/Ψ , $\Psi(3686)$, $\Psi(3770)$: colour dipoles in colour-electric field
- $\bar{D}(\bar{c}q)D(\bar{q}c)$ loops contribute to the charmonium selfenergies
- in matter the energy of the colour dipole is modified due to the modification of the gluon condensate **second order Stark-effect**
S.H. Lee, C.M. Ko Phys. Rev. C67 (2003) 038202

$$\Delta m_\psi = -\frac{\rho_N}{18m_N} \int dk^2 \left| \frac{\partial \psi(k)}{\partial k} \right|^2 \frac{k}{k^2/m_c + \epsilon} \left\langle \frac{\alpha_s}{\pi} E^2 \right\rangle_N \quad \epsilon = 2m_c - m_\Psi$$

- the effect of the $\bar{D}D$ loop modified, because the mass of D mesons also modified due to the change of the quark condensate
- The width of the charmonium increases due to the collisional broadening
- dilepton branching ratio in matter?
due to collisional broadening $\Gamma_{med}^{tot} \gg \Gamma_{vac}^{tot}$. What is Γ_{med}^{em} ? Br_{med}^{em} ?

hadron(\bar{p}, π, p) A around charmonium threshold energies

| Charmonium | Stark-effect+ $\bar{D}D$ loop |
|--------------|-------------------------------|
| J/ Ψ | -8+3 MeV ρ/ρ_0 |
| $\Psi(3686)$ | -100-30 MeV ρ/ρ_0 |
| $\Psi(3770)$ | -140+15 MeV ρ/ρ_0 |

collisional broadening at ρ_0 : 15 MeV, 26 MeV and 26 MeV (cross sections were fitted to charmonium suppression at SPS)

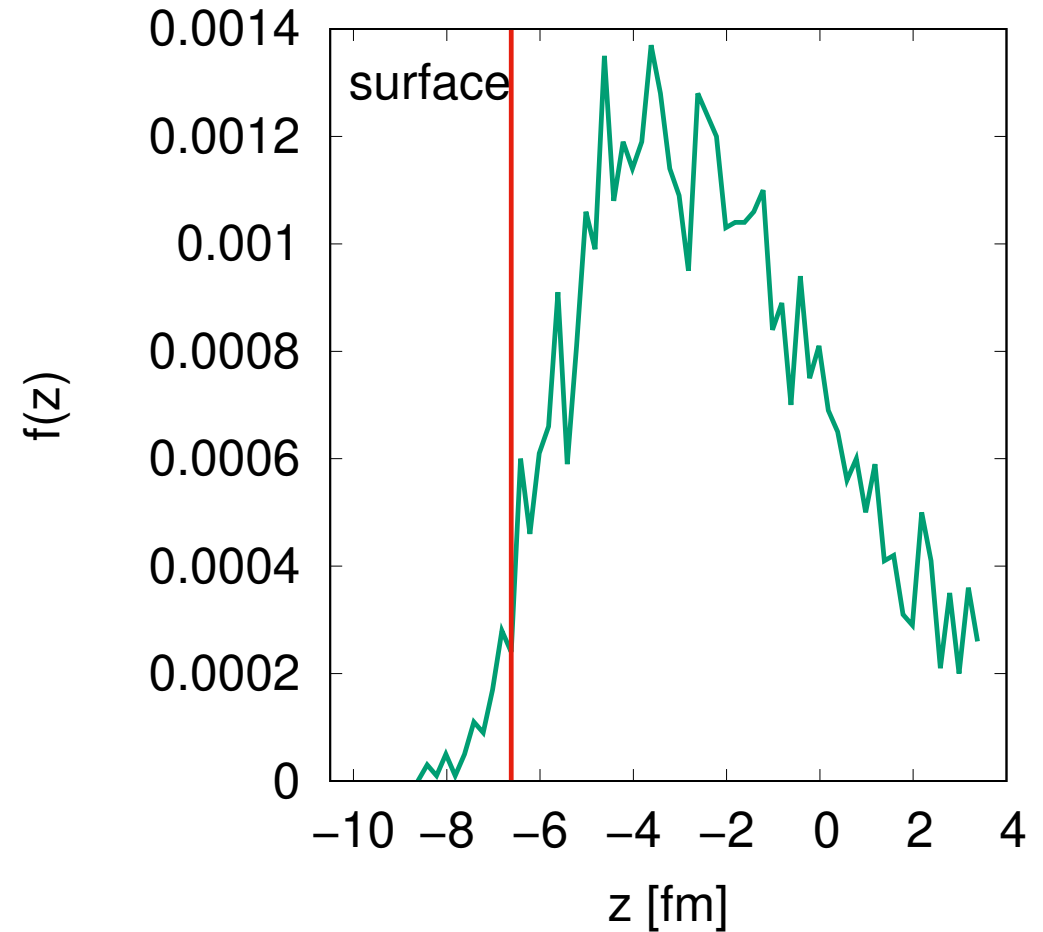
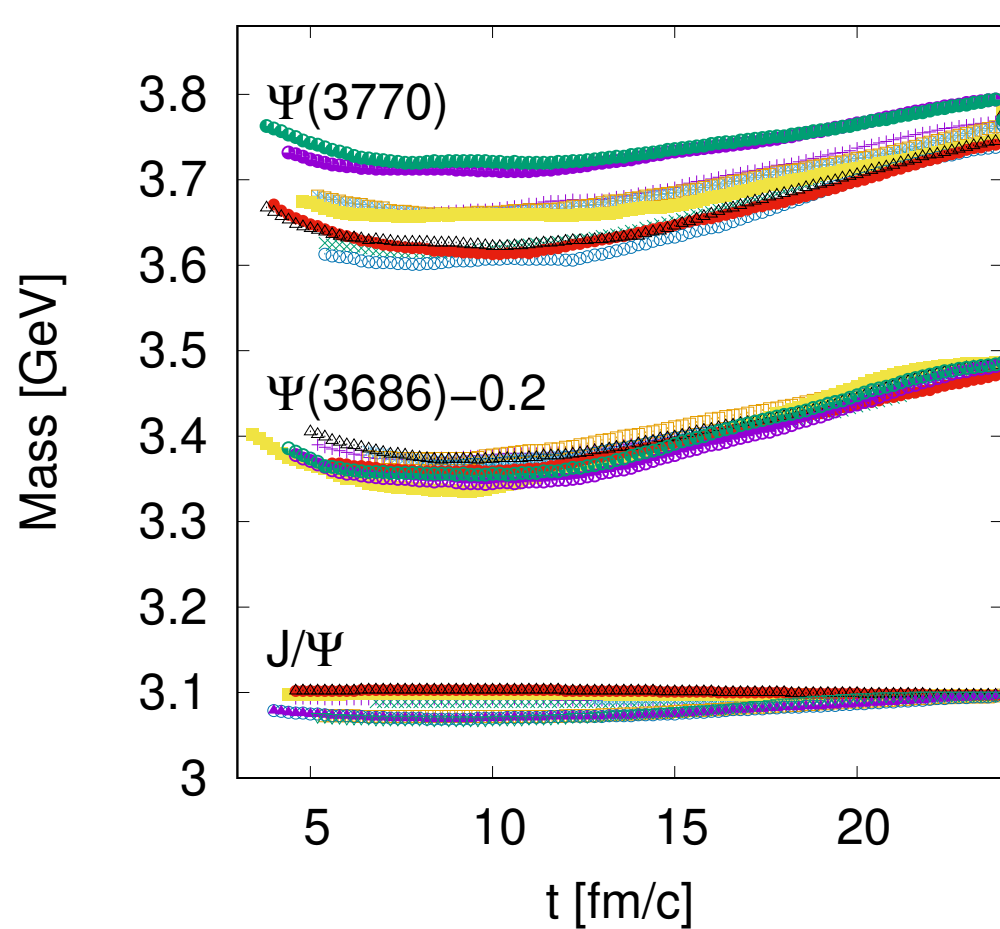
background:

Drell-Yan: small number of energetic hadron-hadron collisions

$\bar{D}D$ decay: c quark decays weakly to s quark, $D \rightarrow Ke\bar{\nu}_e$ and similarly for \bar{D} , close to the threshold due to the production of two kaons the available energy for dileptons are strongly reduced

up to moderate energies (< 8 GeV for \bar{p} , < 12 GeV for π , < 15 GeV for p) the background is low

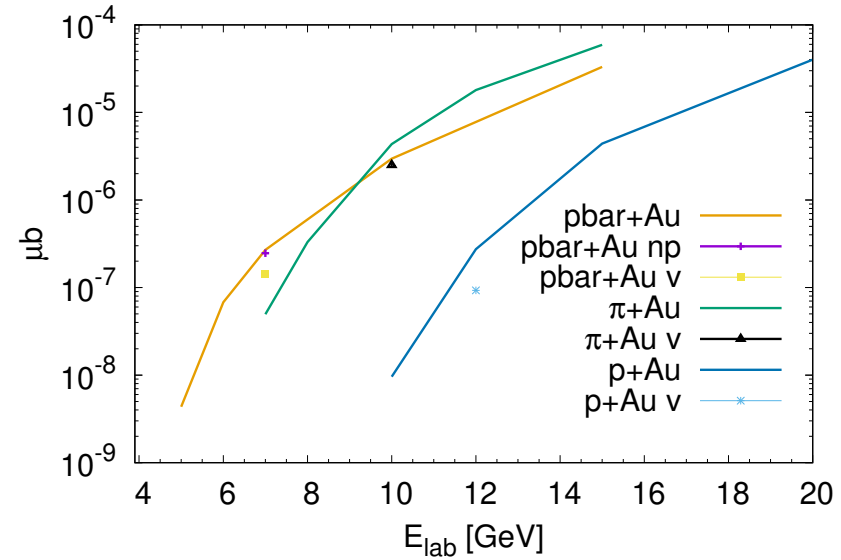
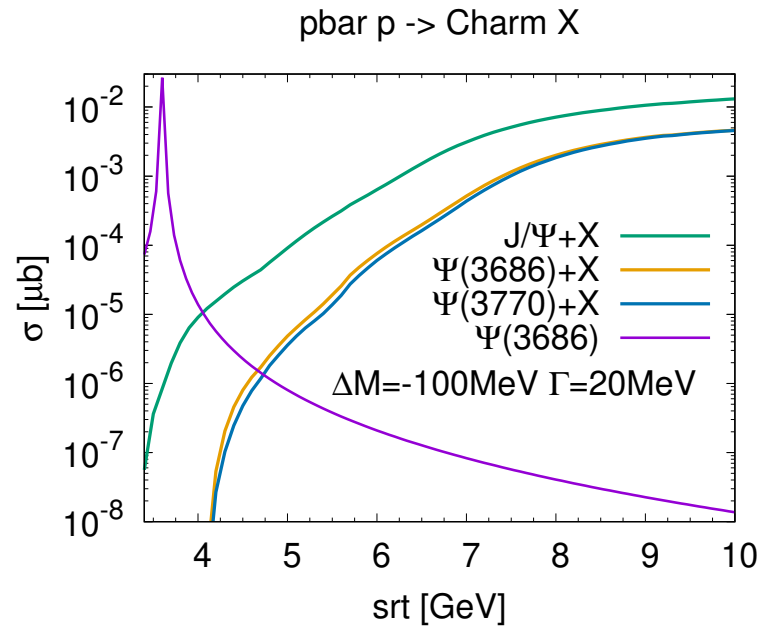
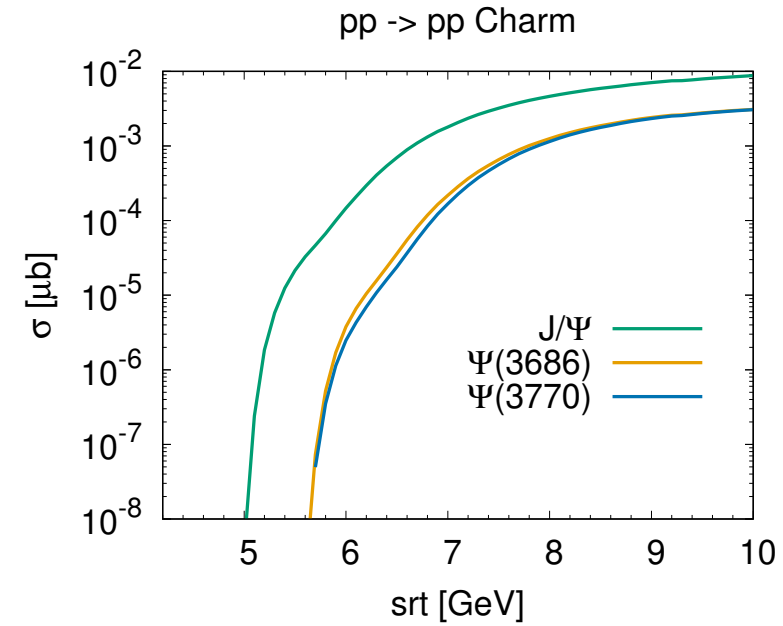
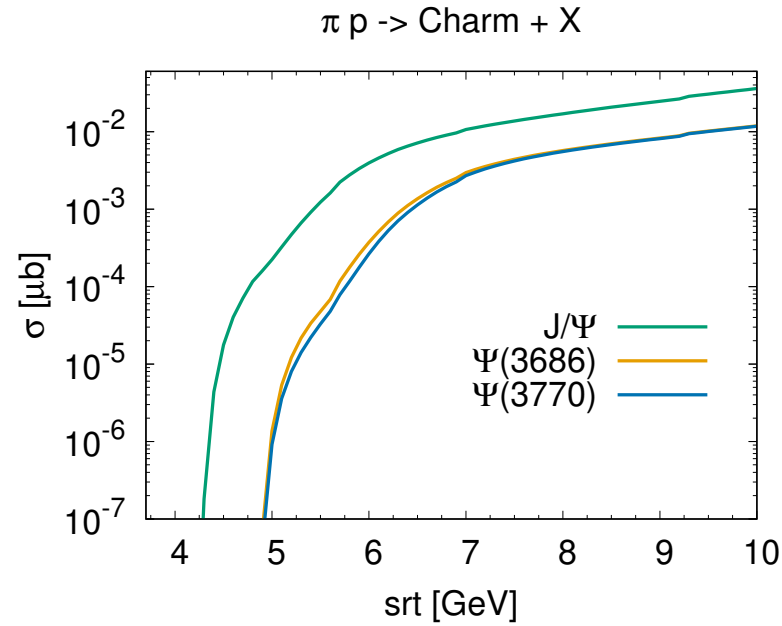
Time evolution of masses and pos. of creation in π Au 6.5 GeV



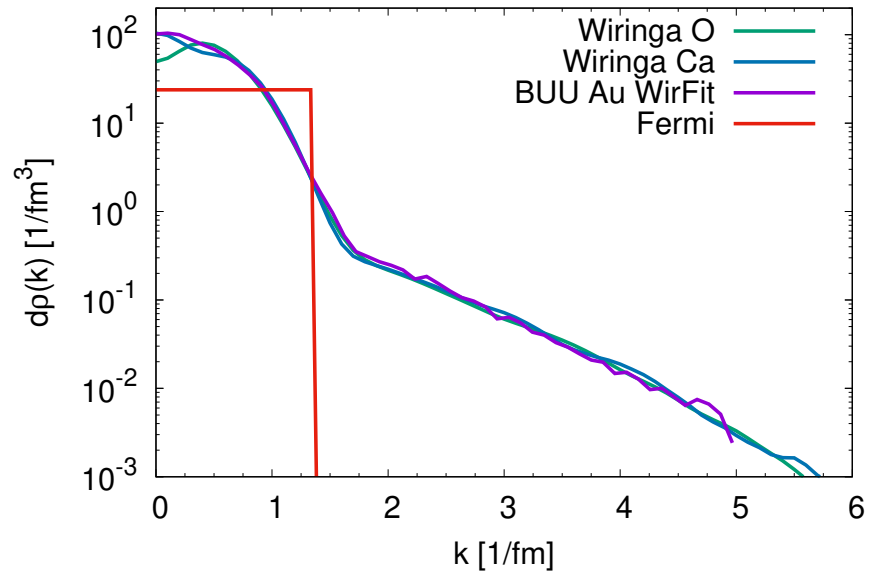
The charmonium states are created at the surface of the heavy nucleus, travel through the dense matter (decays with some probability), crosses the thin surface again and reaching the vacuum.

Major contribution to the dilepton channel are coming from the dense matter and from the vacuum. $t_{\rho > 0.8} \approx 9$ fm, $t_{0.8 > \rho > 0.2} \approx 4$ fm.

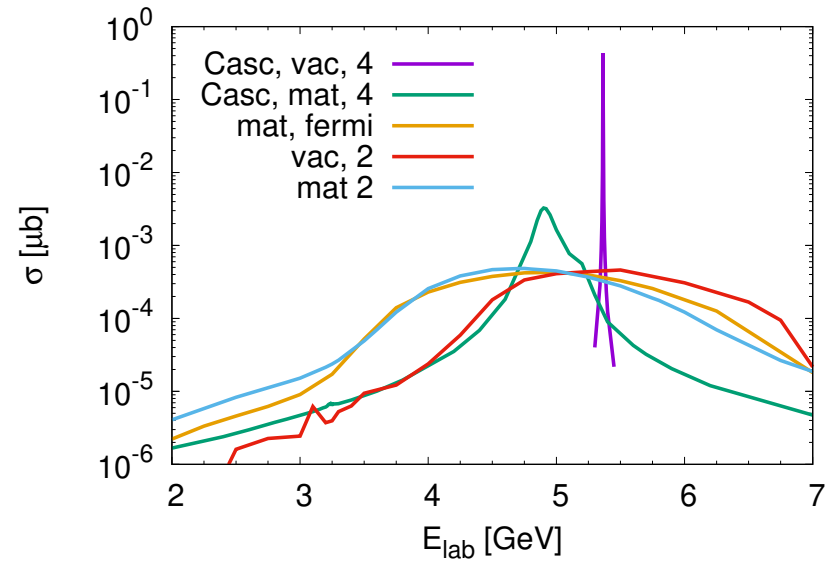
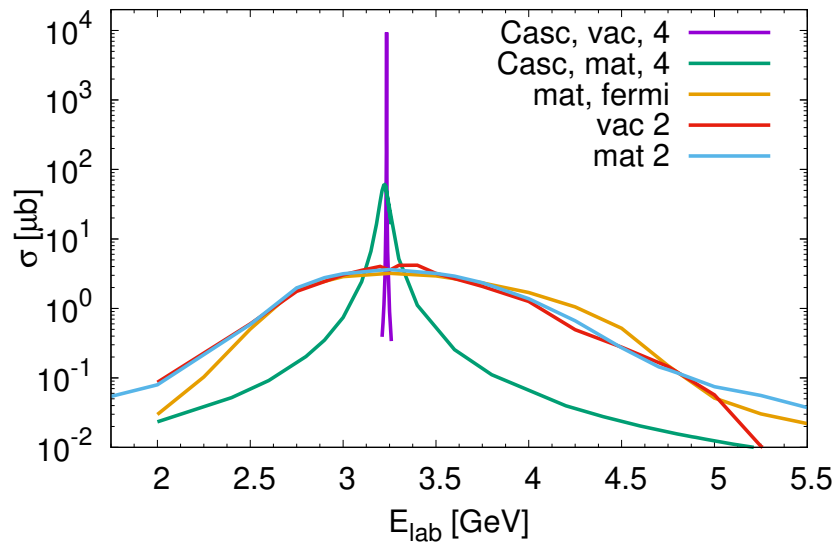
Cross sections



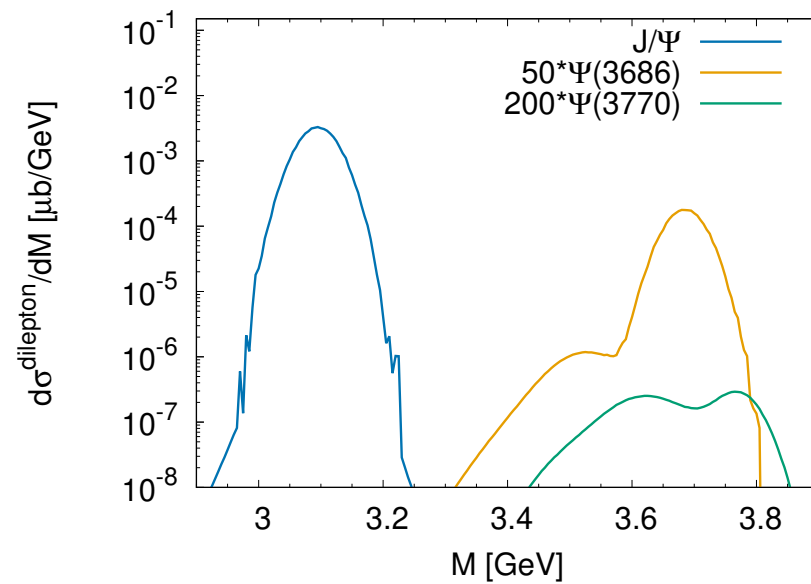
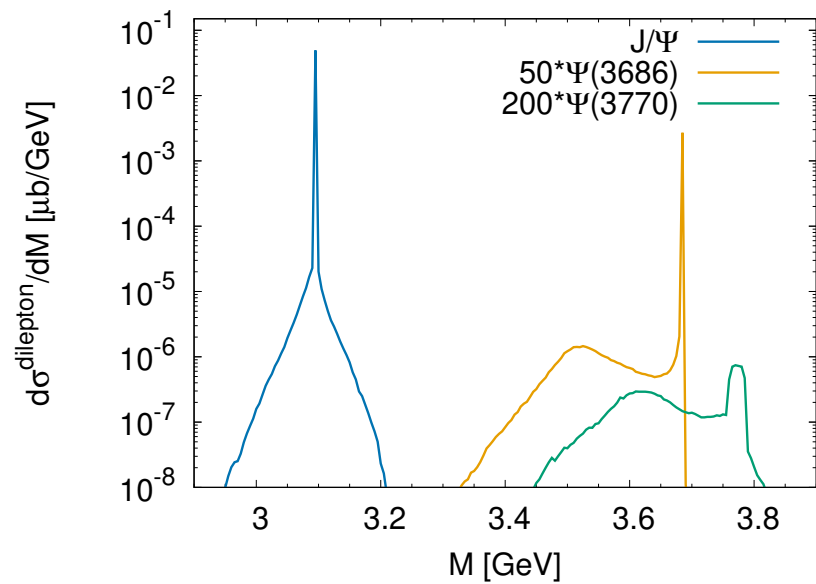
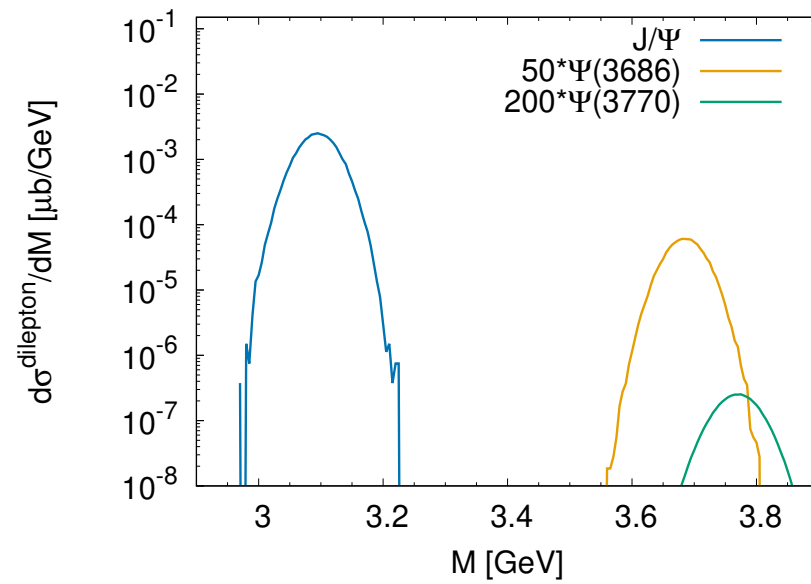
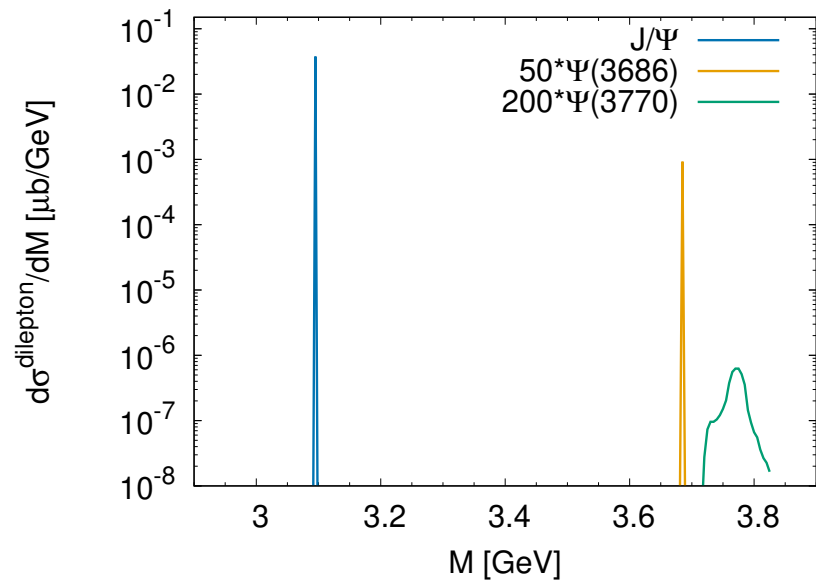
Excitation functions



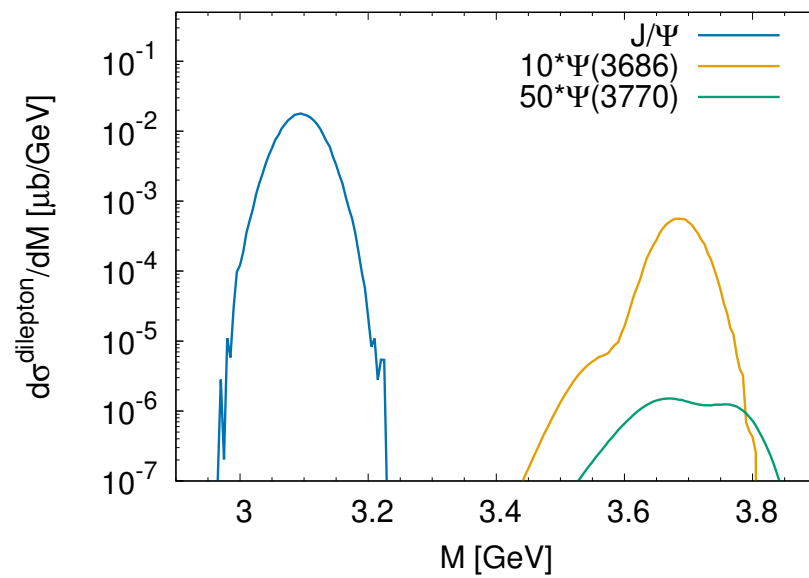
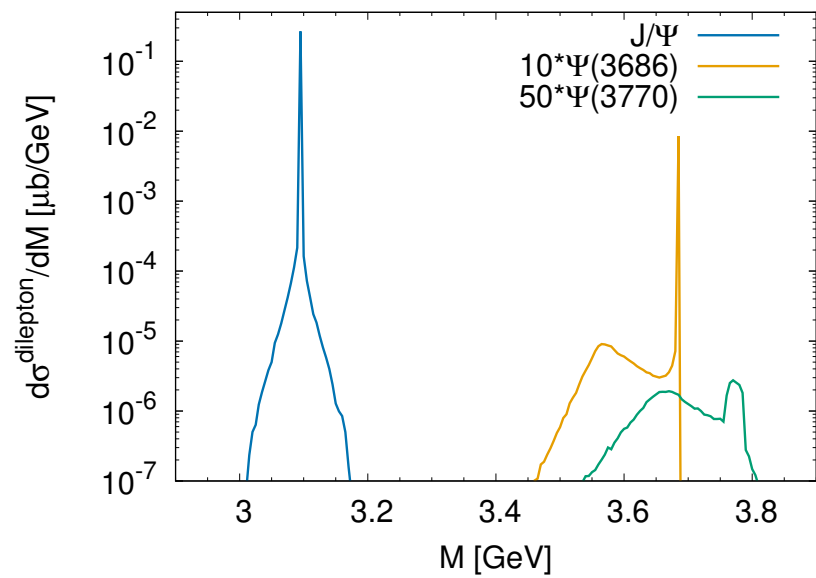
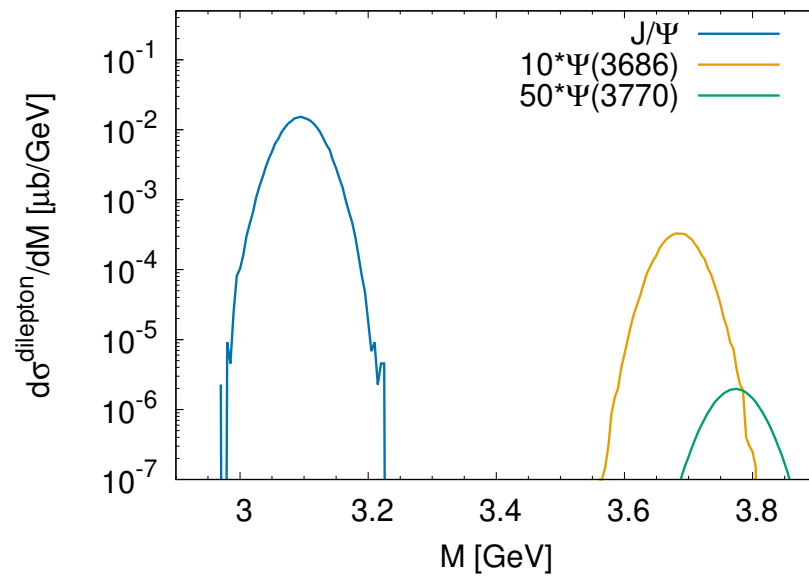
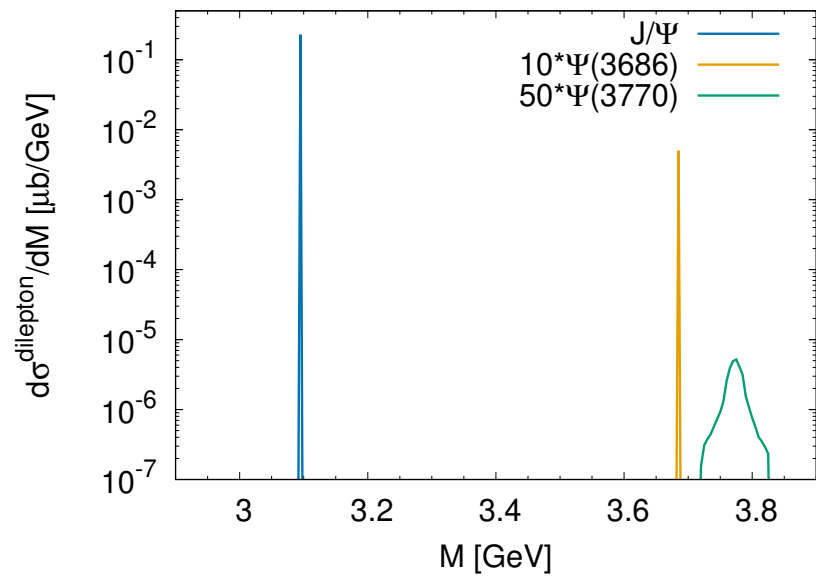
Initial momentum distribution
with short range correlation



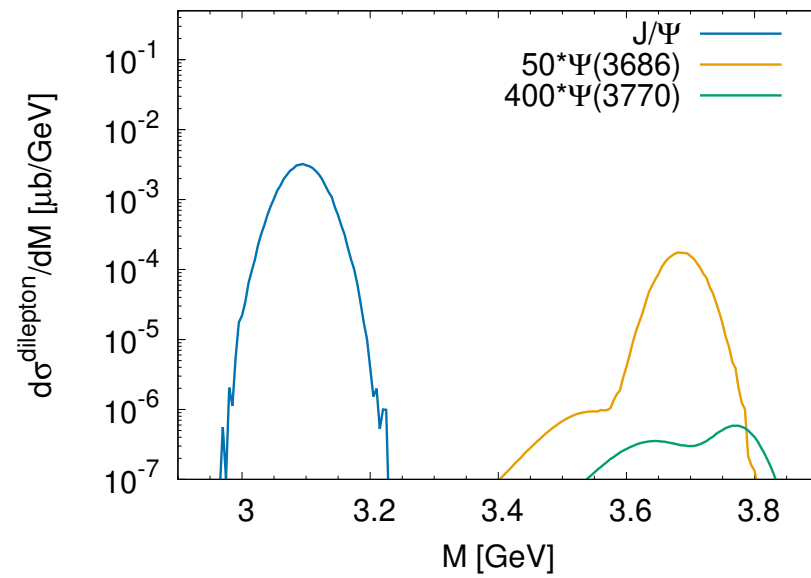
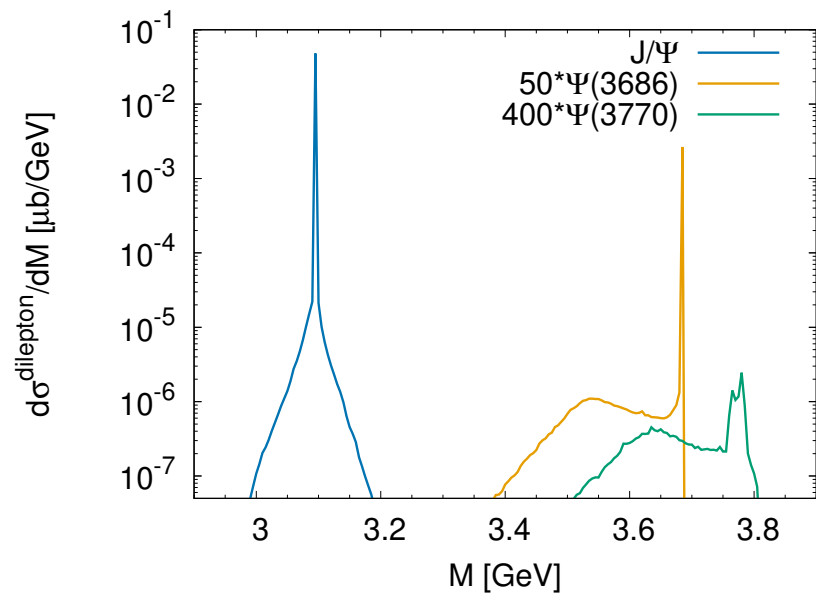
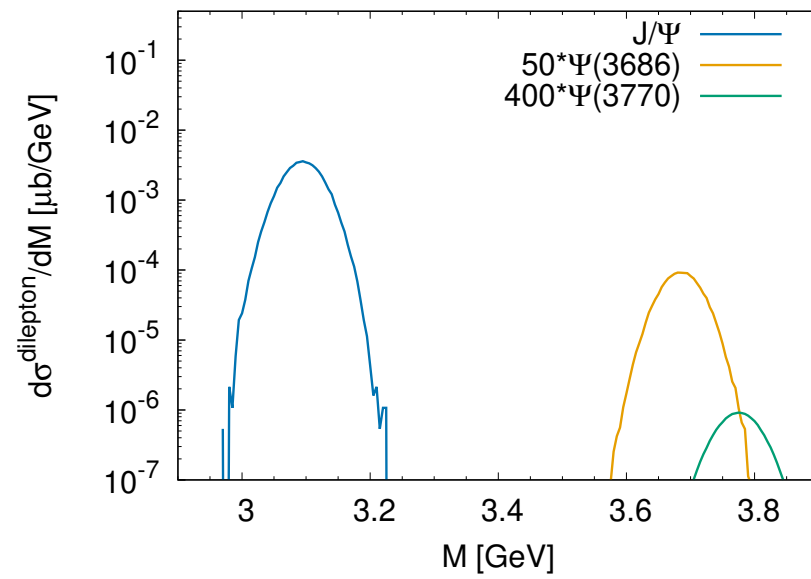
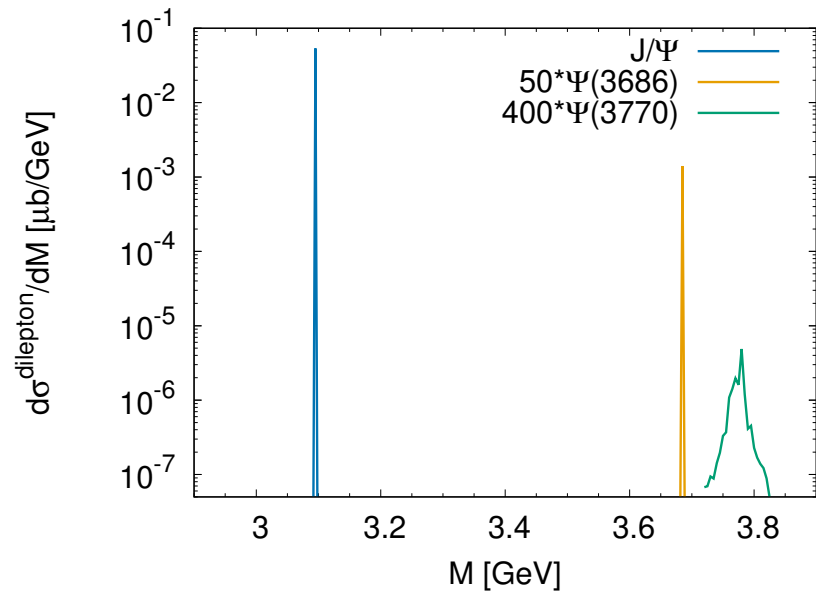
p Au at 12 GeV



π Au at 10 GeV



\bar{p} Au at 7 GeV



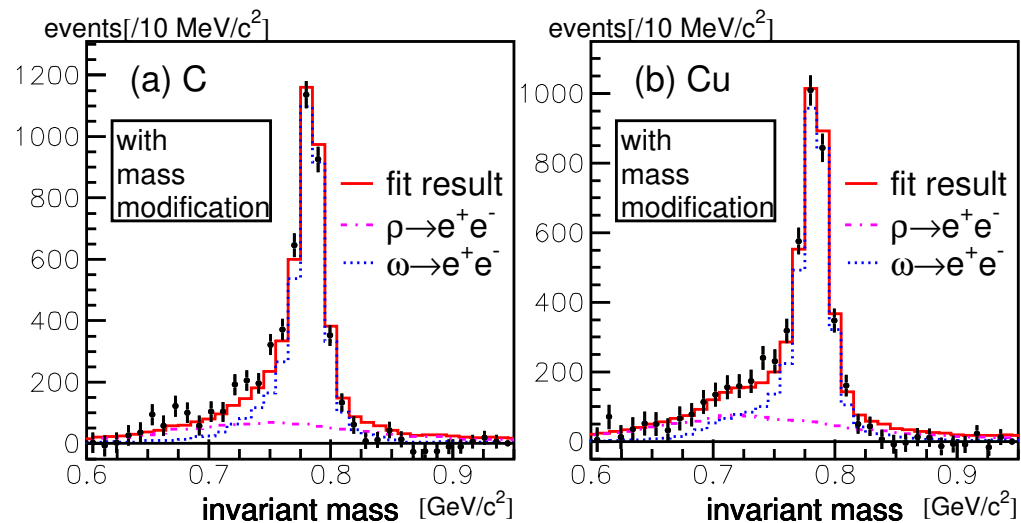
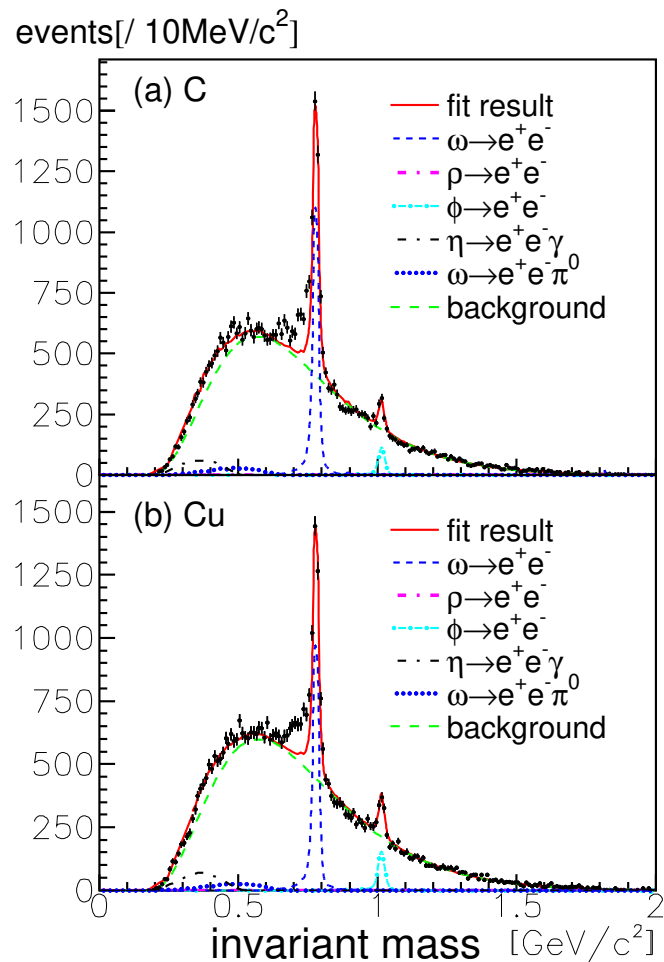
$\Psi(3686)$

- The distance between the peaks corresponds to a mass shift at $\rho \approx 0.9\rho_0$
- qualitatively the same picture if increase or reduce the mass shift by factor of 2
- measuring the peak distance, we obtain the mass shift at $\rho \approx 0.9\rho_0$
- measuring the mass shift, we obtain the gluon condensate at $\rho \approx 0.9\rho_0$
- the same picture in \bar{p}, π, p at and above thresholds
- measuring the $JP/\Psi, \Psi(3686)$ states allow to determine their mass shift if it is > 60 MeV
- key points: cross sections are not, background is several magnitude less than the signal
- em. width
- absorption cross sections 25 mb (40 mb for p)
- can the error of the experimental mass resolution from the vacuum peak overshadow the smaller, in-medium peak?

Summary

- Dilepton production in hadron-A provides us the possibility to study charmonium mass shift in matter. In all systems we found in-medium spikes for $\Psi(3686)$.
- We can measure the gluon condensate in nuclear matter.

KEK E325 12 GeV pA data ρ and ω



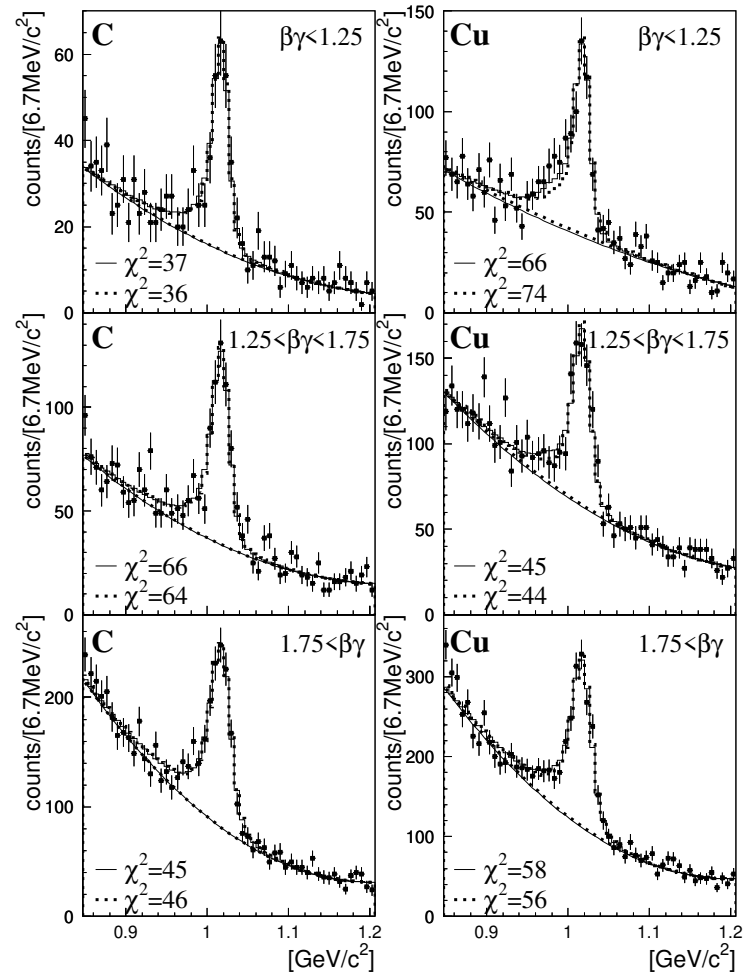
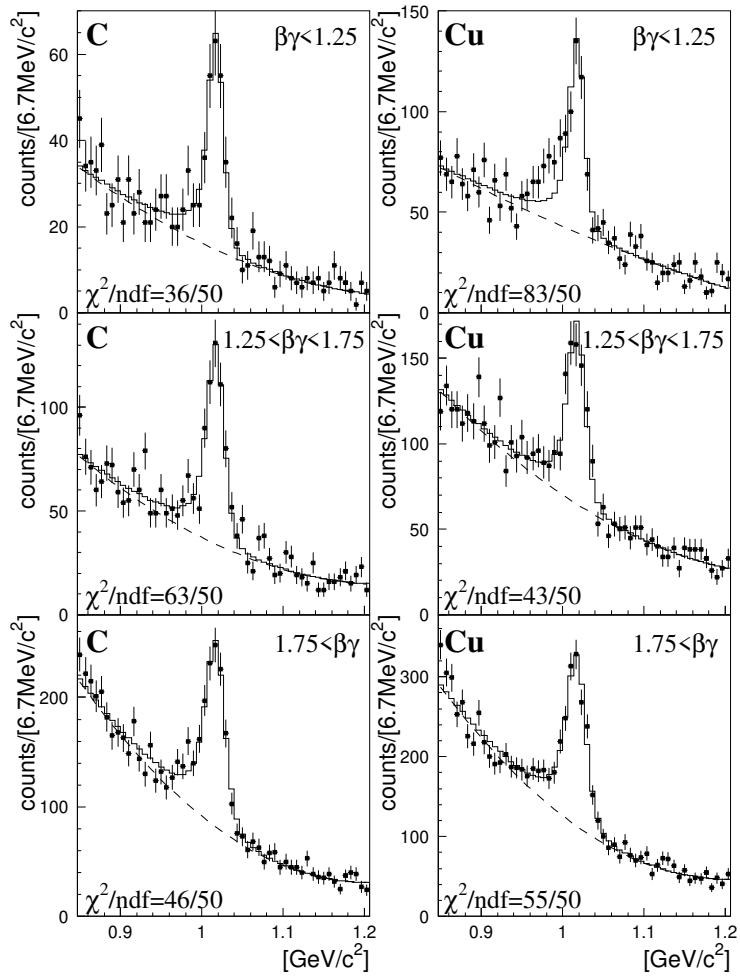
$$m(\rho)/m(0) = 1 - 0.09(\rho/\rho_0)$$

no broadening

M. Naruki *et al.*

Phys. Rev. Lett. 96 (2006) 092301

KEK E325 12 GeV pA data for ϕ



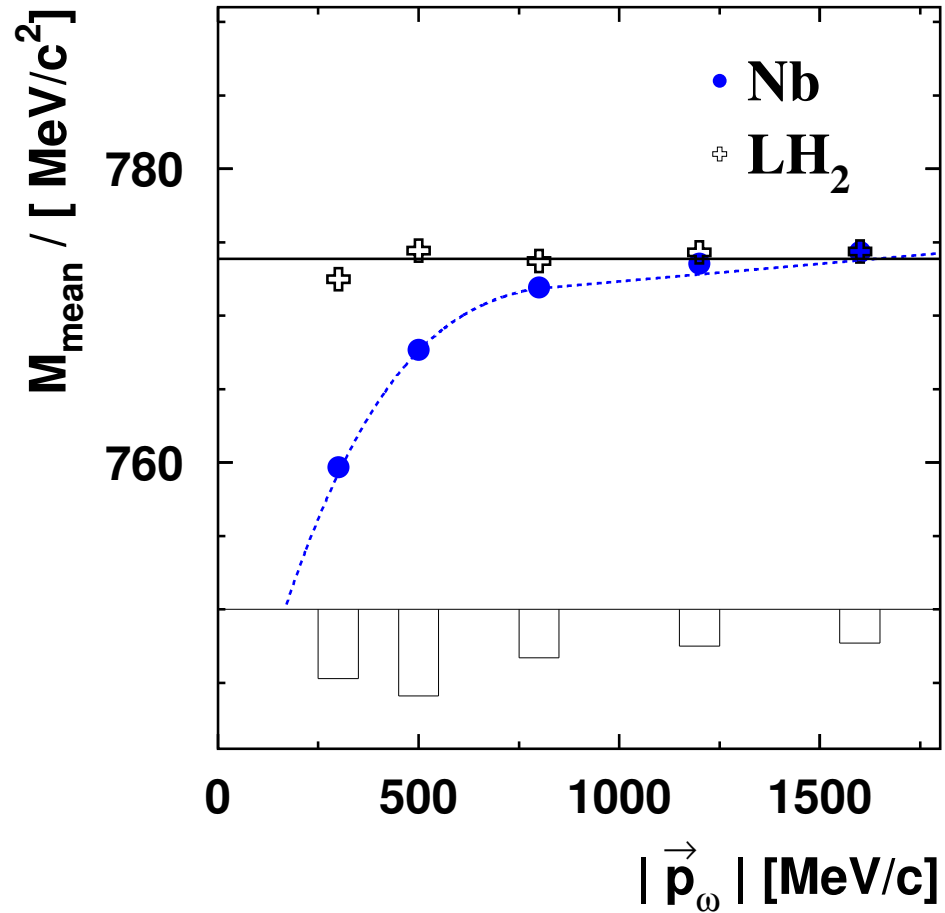
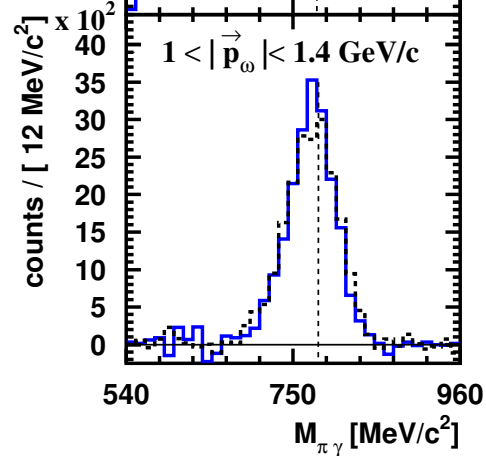
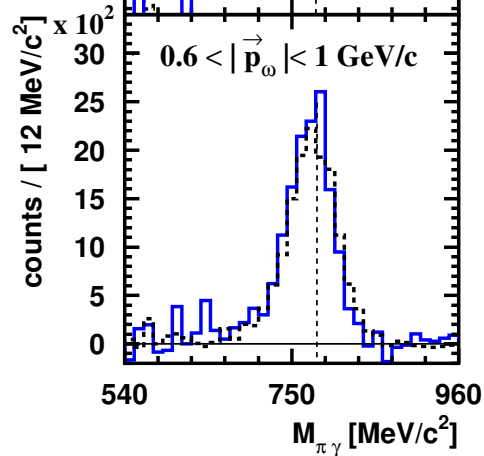
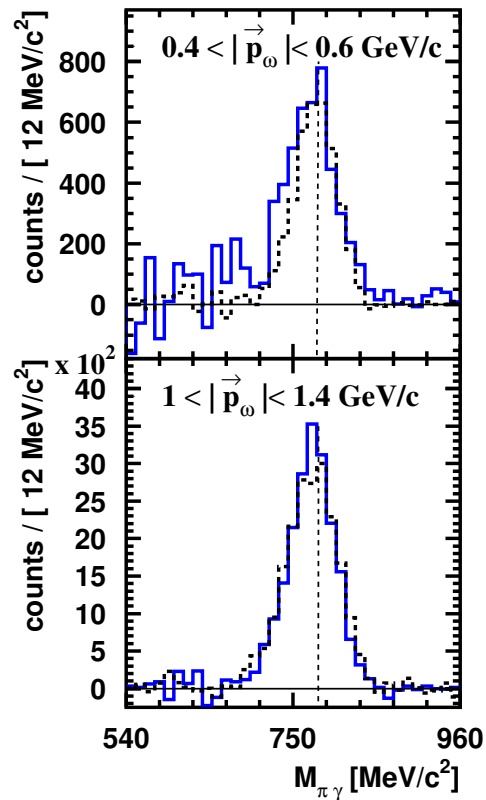
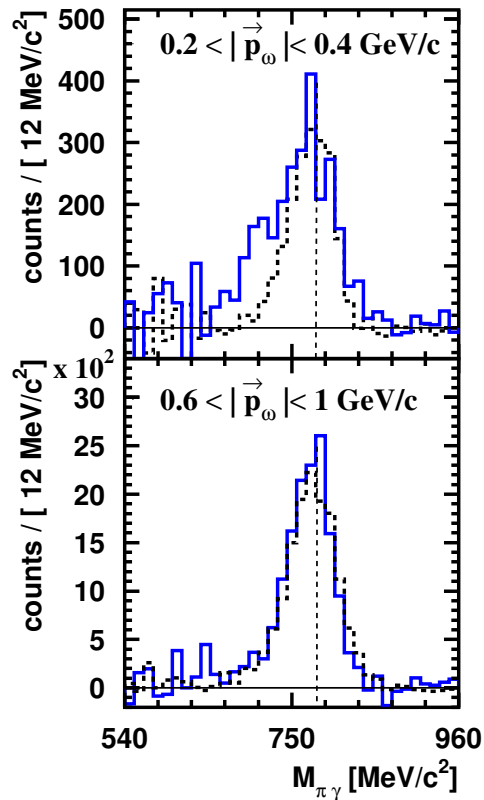
$$m(\rho)/m(0) = 1 - 0.033(\rho/\rho_0)$$

$$\Gamma(\rho)/\Gamma(0) = 3.6(\rho/\rho_0)$$

R. Muto *et al.*

Phys. Rev. Lett. 98 (2007) 042501

TAPS/ELSA data for $\gamma A \rightarrow \omega X$



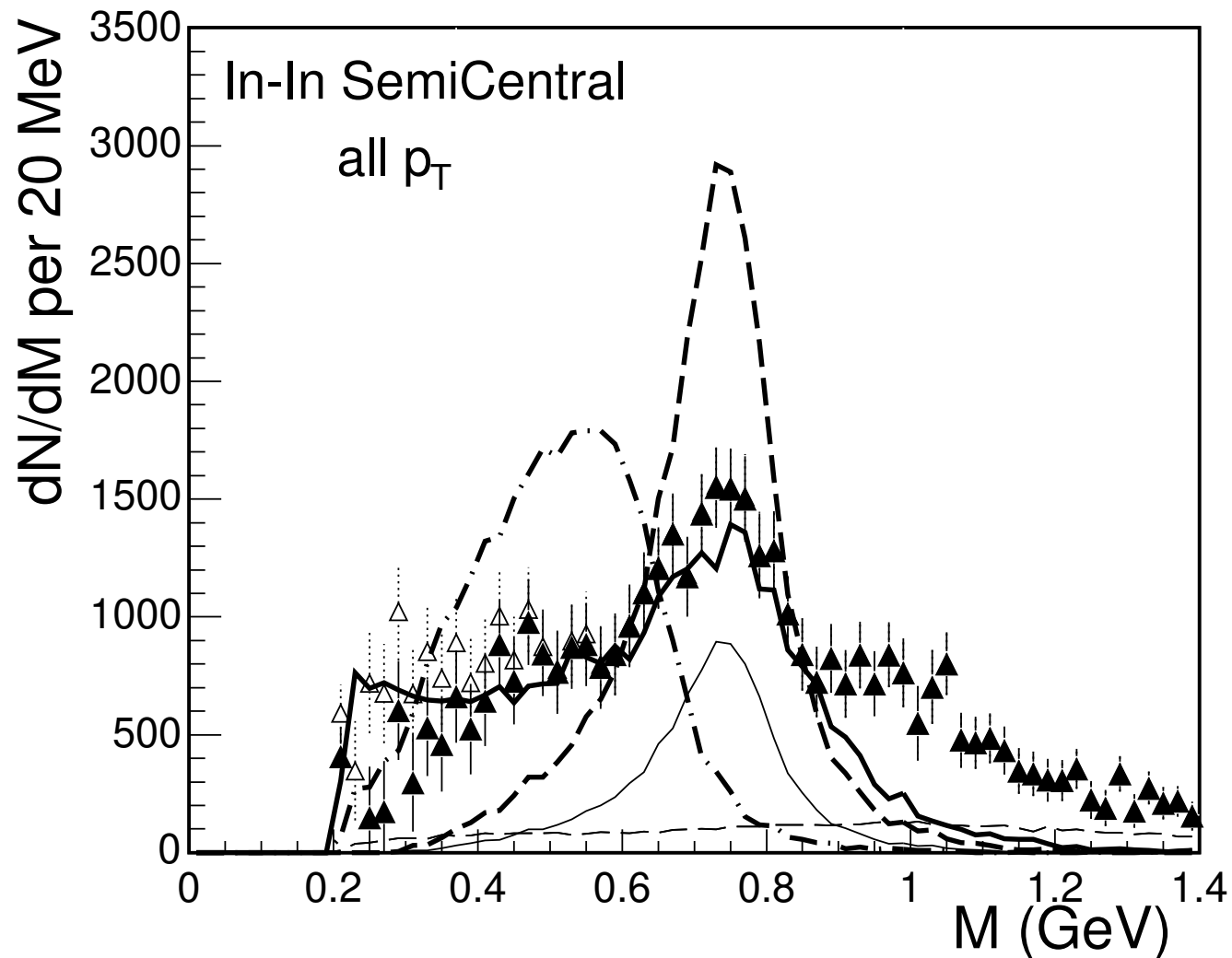
$$m(\rho)/m(0) = 1 - 0.14(\rho/\rho_0), \quad \bar{\rho} = 0.6\rho_0$$

$$\Gamma_{res} = 55 \text{ MeV}$$

D. Trnka *et al.*

Phys. Rev. Lett. 94 (2005) 192303

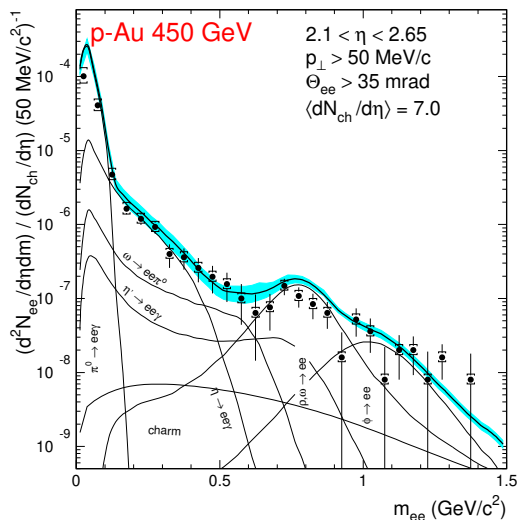
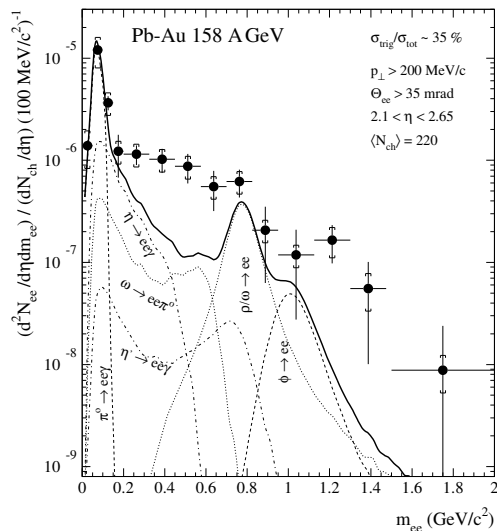
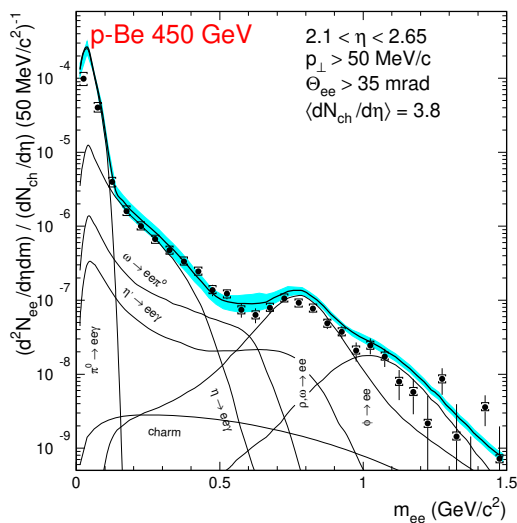
NA60 data for ρ



thick solid line: ρ -broadening
due to hadronic reactions
R. Rapp, J. Wambach
Adv. Nucl. Phys. 25, 1

S. Damjanovic *et al.*
Eur.Phys.J.C49:235-241,2007

CERES data



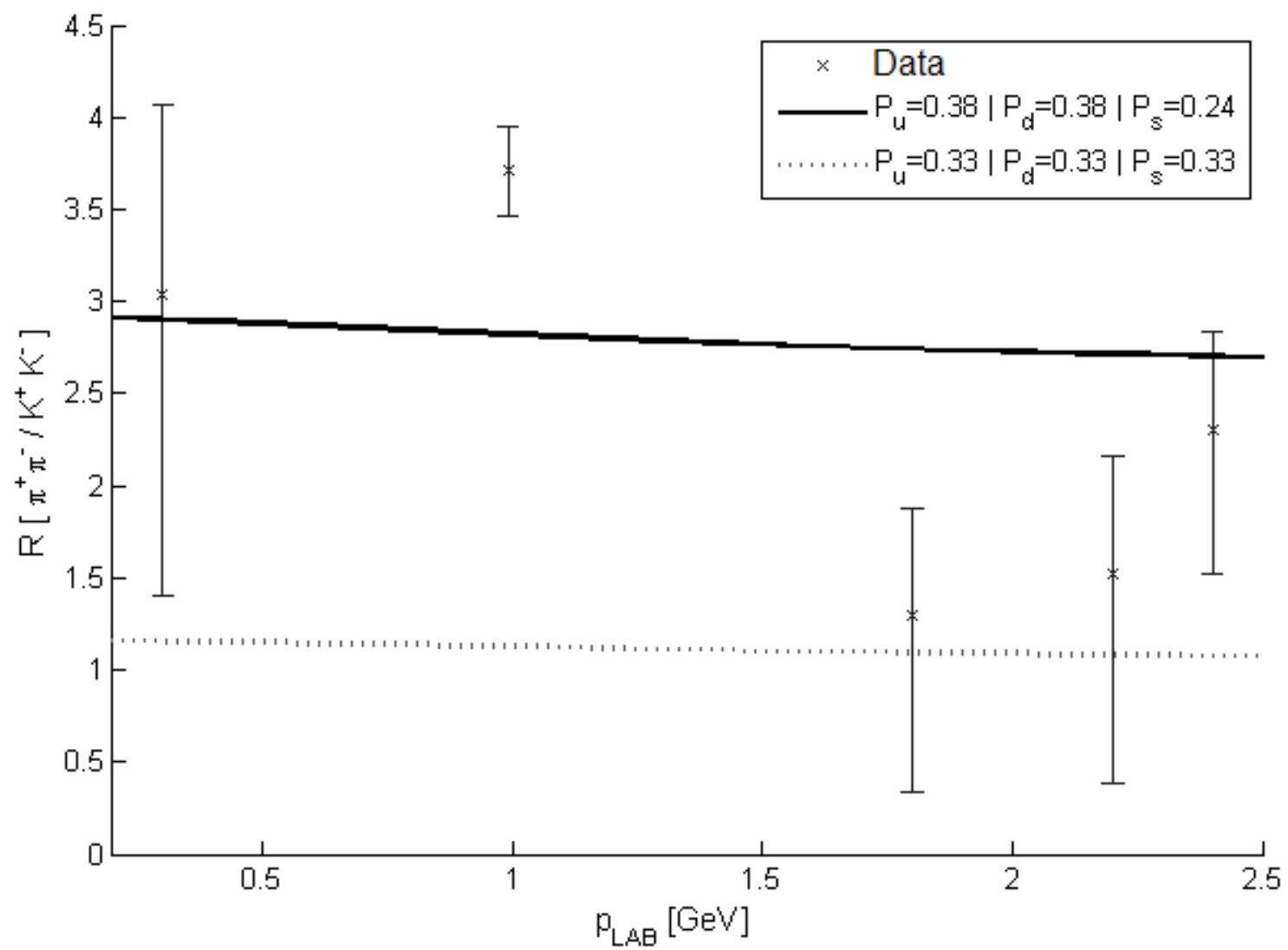
G. Agakichiev *et al.*
 Eur. Phys. J. C4 (1998) 231

G. Agakichiev *et al.*
 Phys. Lett. B422 (1998) 405

Statistical Bootstrap approach

G. Balassa, P. Kovács, Gy. Wolf, Eur. Phys. J. A54 (2018) 25

- Estimate unknown cross sections of different hadronic reactions up to a few GeV in c.m.s energy.
- Our method incorporate that during the collision a compound system, a fireball, is formed and, through possible production of subsequent fireballs, this system decays into a specific final state.
- The probability of the resulting final state can be calculated from the corresponding phase space, the quark content of the final state and from the density of states $\rho(m)$.



Predictions

