
Dense nuclear matter from HICs to NS

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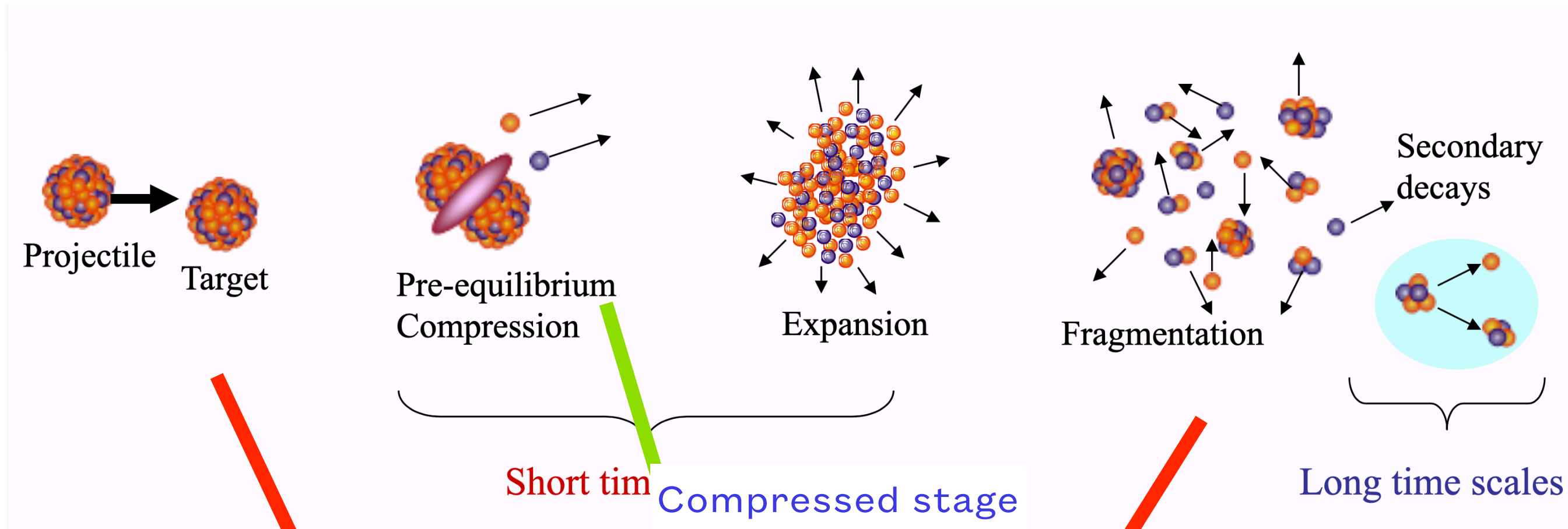
in collaboration with S. Jeon, C.-H. Lee, Y. Kim, Y.-M. Kim, and K. Kwak



Content

- Introduction
- Transport theory / DJBUU model
- Results comparison with TMEP
- Pion production and symmetry energy @ LAMPS/RAON
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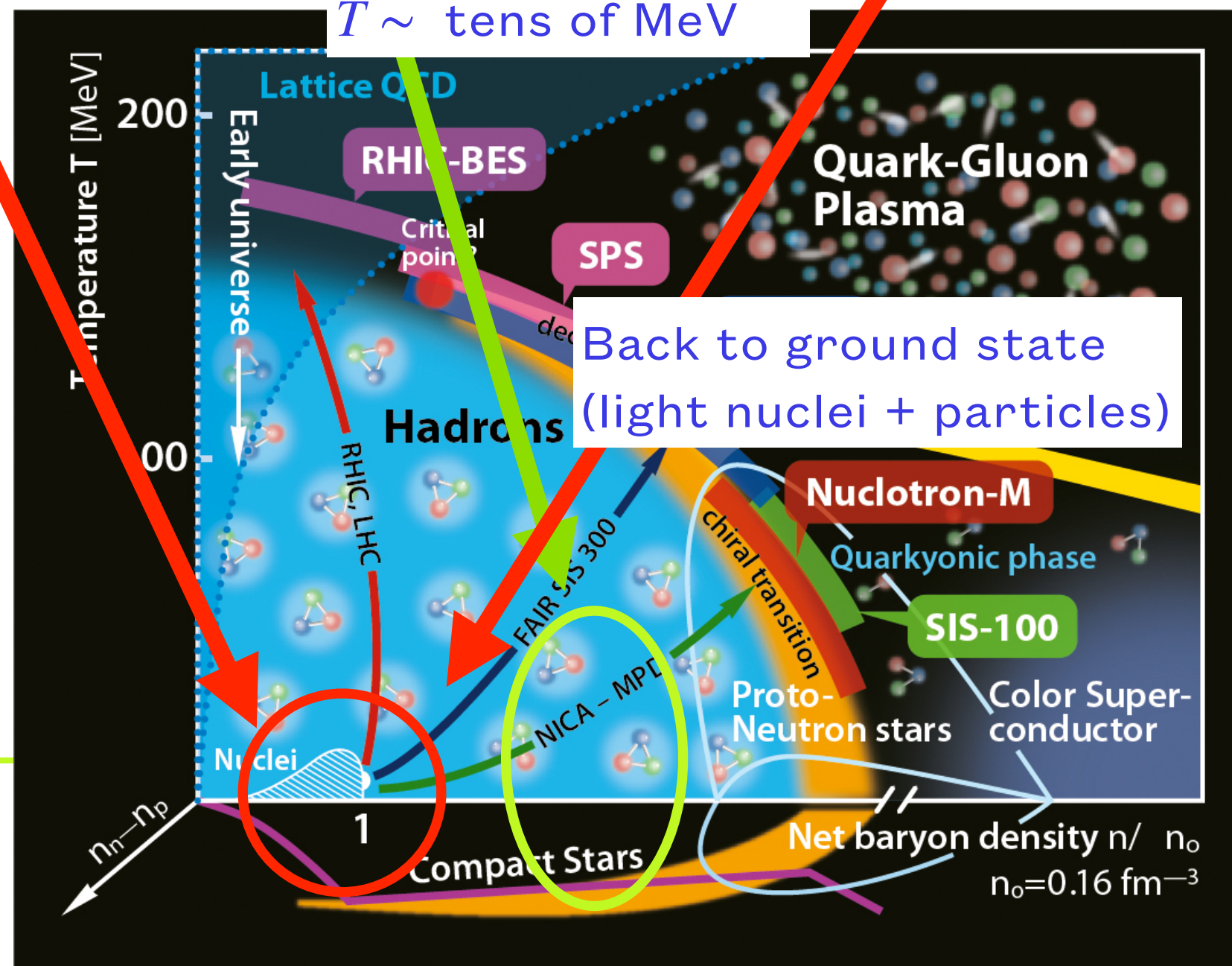
Heavy-ion collisions: why study?



Initial stage
 $\rho_0 = 0.16 \text{ fm}^{-3}$
 $T \sim 0 \text{ MeV}$

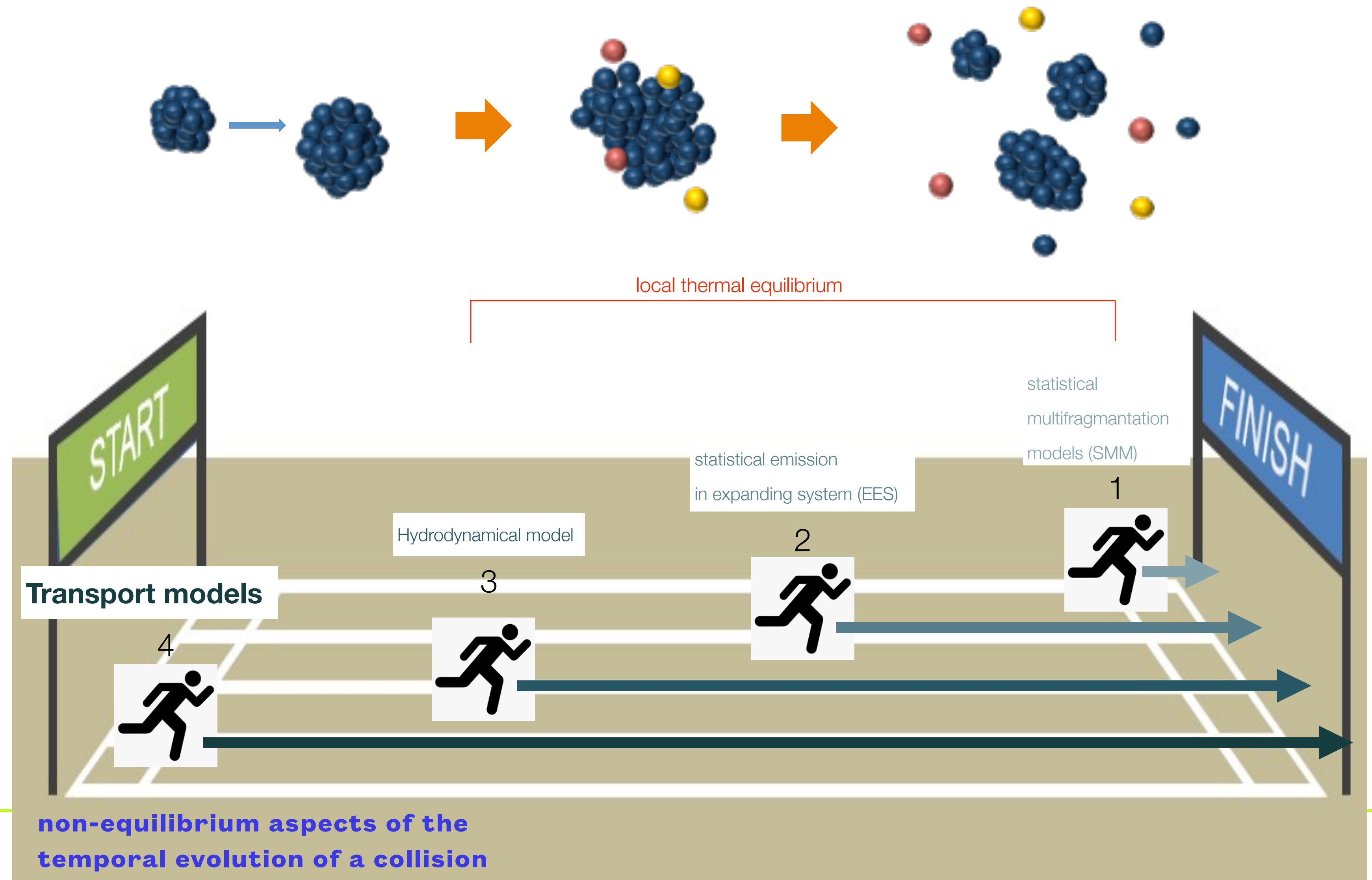
$\rho \sim \text{a few } \rho_0$

$T \sim \text{tens of MeV}$

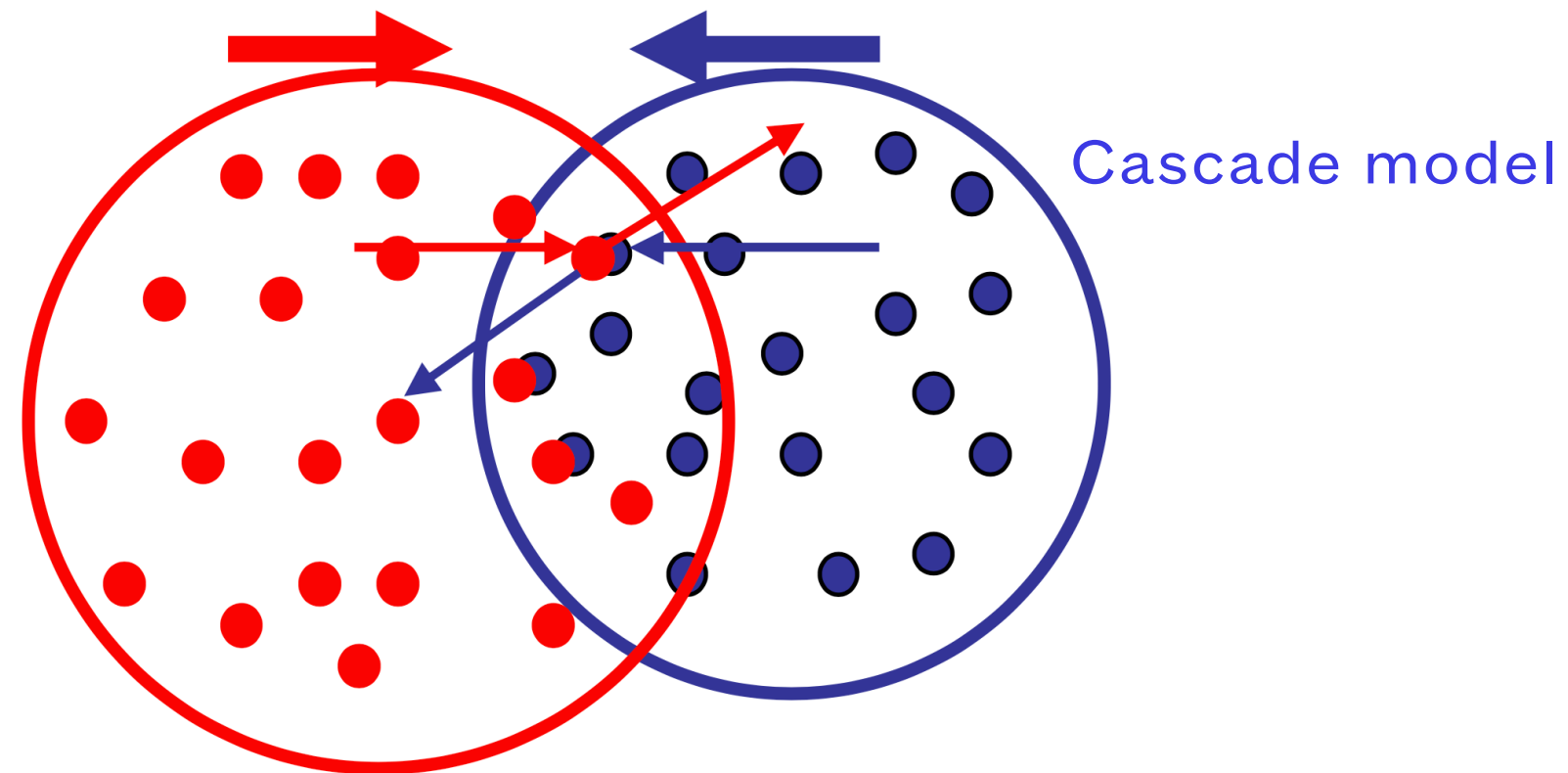


- explore phase diagram of strongly interacting matter in the hadronic sector
- nuclear matter above saturation: EOS & hadronic properties in dense medium
- importance for astrophysics: SN and NS

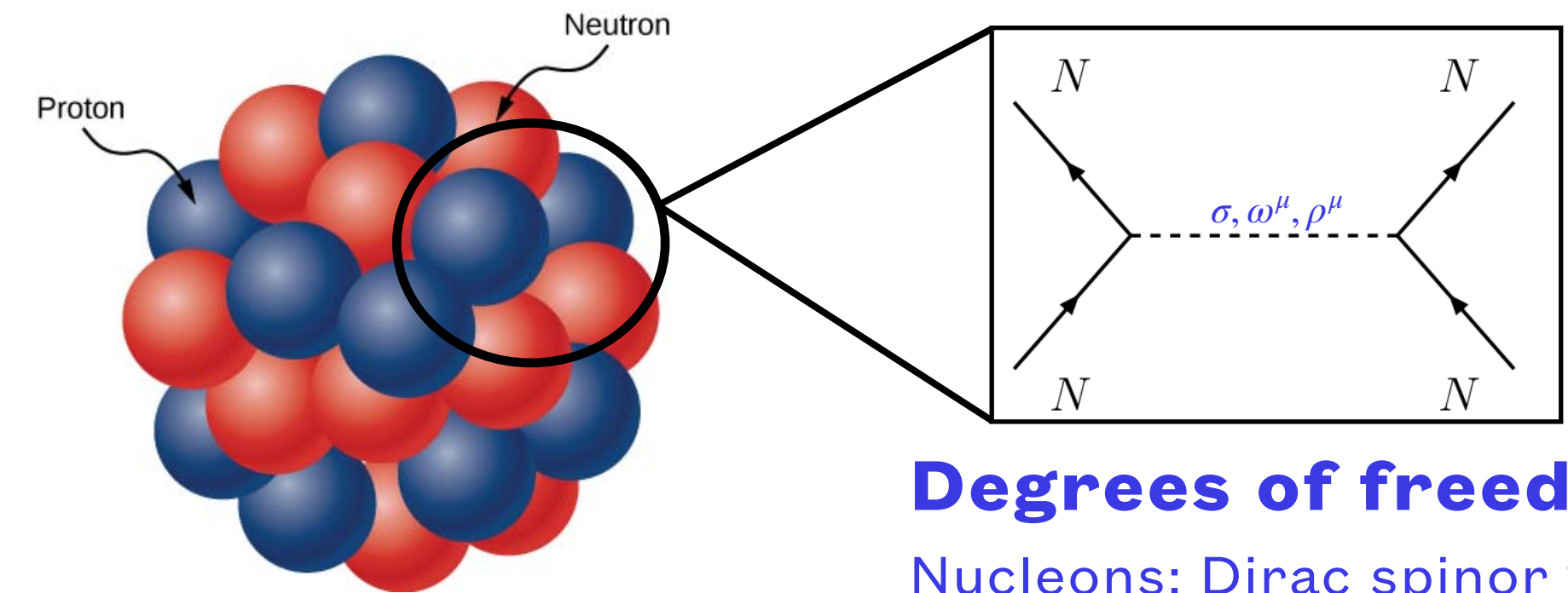
Levels of descriptions in HICs



Collisions and microscopic interactions



- simple and first model focusing only NN collisions (no interactions)
- collision criterion: point of closest approach (Bertsch prescription)
- scattering can be elastic or inelastic
- giving great insight of heavy-ion physics



Degrees of freedom
 Nucleons: Dirac spinor ψ
 Interaction: $\sigma, \omega^\mu, \rho^\mu$ mesons

- free Lagrangian for Dirac field + interaction
 Lagrangian for meson field

$$\left[i\gamma_\mu \partial^\mu - \underbrace{(m_N + g_\sigma \sigma)}_{\text{Dirac mass, effective mass, } m^*} - g_\omega \gamma_0 \omega^0 - g_\rho \gamma_0 \tau_3 \rho_3^0 - \frac{e}{2} \gamma_0 (1 + \tau^3) A^0 \right] \psi = 0$$

$$m_\sigma^2 \sigma + a\sigma^2 + b\sigma^3 = -g_\sigma \rho_S$$

$$m_\omega^2 \omega^0 = g_\omega \rho_B$$

$$m_\rho^2 \rho_3^0 = g_\rho \rho_{B,I3}$$

TABLE I. Parameter sets.

Parameter	Set I	Set II	NL3
f_σ (fm ²)	10.33	same	15.73
f_ω (fm ²)	5.42	same	10.53
f_ρ (fm ²)	0.95	3.15	1.34
f_δ (fm ²)	0.00	2.50	0.00
A (fm ⁻¹)	0.033	same	-0.01
B	-0.0048	same	-0.003

Relativistic transport equation (BUU eq.)

Aim: microscopic description of nucleus-nucleus collisions

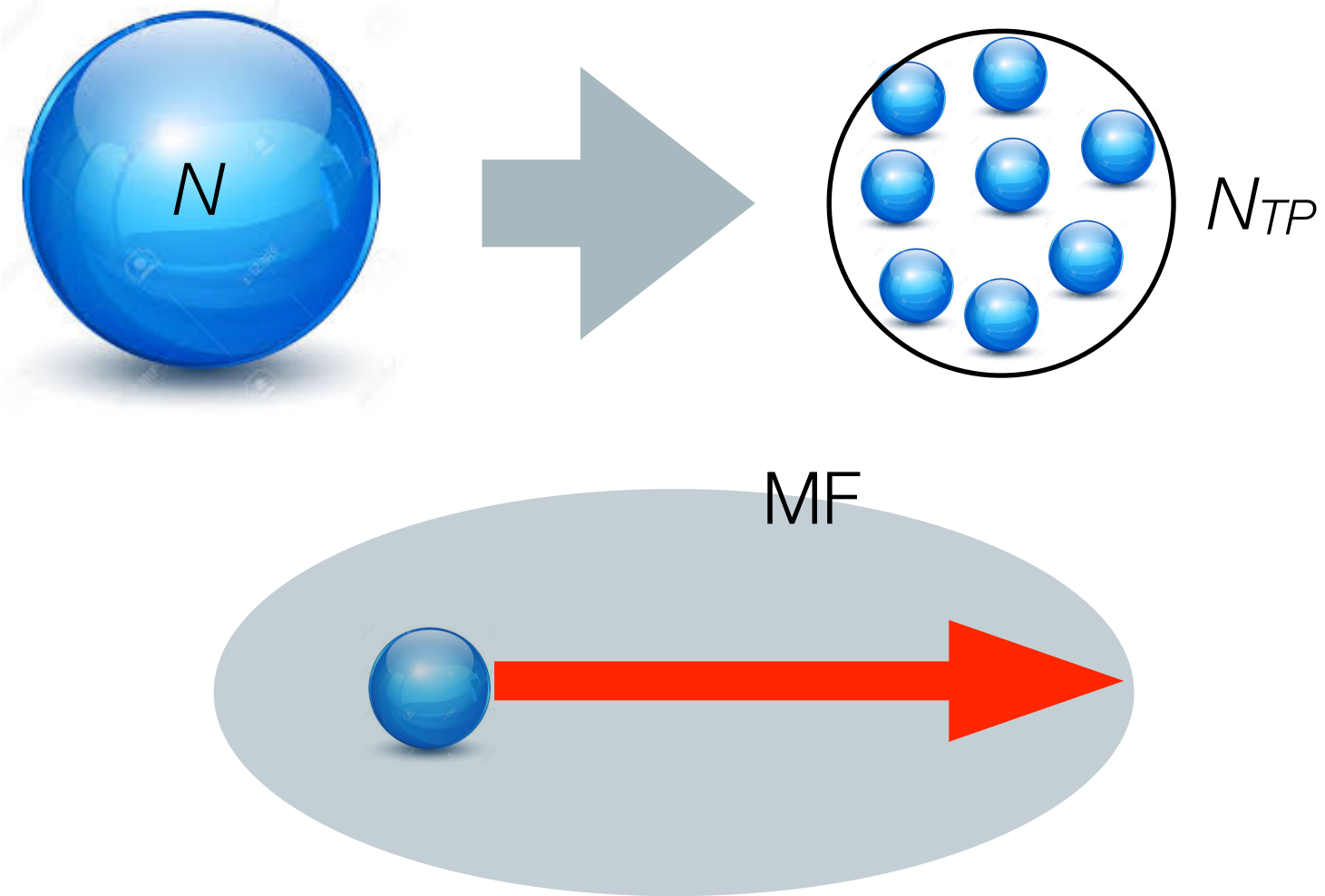
$$(p^{*0})^{-1} \left[\underbrace{p^{*\mu} \partial_{\mu} - (p^{*\mu} \mathcal{F}^{\mu i} - m^* \partial^i m^*(x))}_{\text{under the RMF potential}} \frac{\partial}{\partial p^{*i}} \right] \underbrace{f(\vec{x}, \vec{p}^*)}_{\text{propagation of } f(x,p^*)} = \underbrace{C(\vec{x}, \vec{p}^*)}_{\text{up to 2-body coll.}}$$

$$C^{(2)}(\vec{x}, \vec{p}_1) = \frac{1}{2} \int \frac{d^3 p_2}{(2\pi)^3 2p_2^0} \int \frac{d^3 p_{1'}}{(2\pi)^3 2p_{1'}^0} \int \frac{d^3 p_{2'}}{(2\pi)^3 2p_{2'}^0} \underbrace{|\mathcal{M}_{12 \rightarrow 1'2'}|^2}_{\text{cross sections}} (2\pi)^4 \underbrace{\delta(p_1 + p_2 - p_{1'} - p_{2'})}_{\text{energy cons.}} \underbrace{[f_1(\vec{x}, \vec{p}_{1'}) f_2(\vec{x}, \vec{p}_2) \tilde{f}_1(\vec{x}, \vec{p}_1) \tilde{f}_2(\vec{x}, \vec{p}_2) - f_1(\vec{x}, \vec{p}_1) f_2(\vec{x}, \vec{p}_2) \tilde{f}_1(\vec{x}, \vec{p}_{1'}) \tilde{f}_2(\vec{x}, \vec{p}_{2'})]}_{\text{Pauli blocking}}$$

- possible collisions up to two-body collisions
- uncorrelated momenta of two incoming (p_1, p_2) as well as outgoing ($p_{1'}, p_{2'}$)
- local collisions in time & space ($x_i = x_{i'}$)
- Pauli exclusion principle in collision term by $1-f(x,p)$

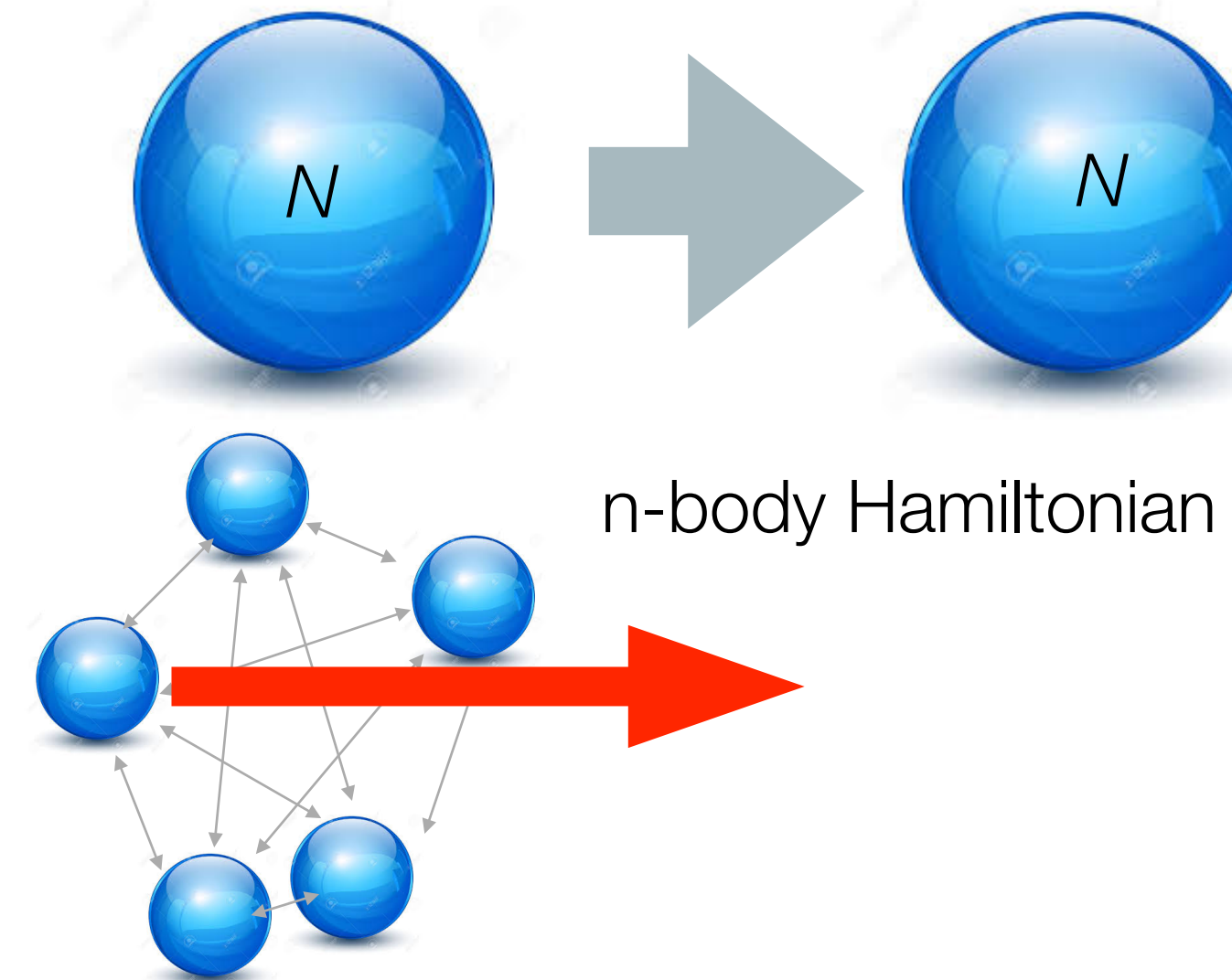
Transport model and families

Boltzmann-Uehling-Uhlenbeck (BUU)



- nucleons divided by N_{TP}
(infinite N_{TP} = exact solution of BUU eq.)
- 1-body phase-space function under MF potential
- Point or finite size of particles

Quantum Molecular Dynamics (QMD)



- Gaussian wave packets ($N_{TP} = 1$)
- n-body Hamiltonian
- Correlation & fluctuations

What DJBUU is

Philosophy: EASY HANDLING & OPTIMIZING to RAON experiments

- DaeJeon Boltzmann-Uehling-Uhlenbeck project
- Oct. 2015 - DJBUU project initiated by S. Jeon in RISP (C.-H. Lee and Y. Kim)
- Jan. 2016 - Primary version of DJBUU (c/c++)
- 2016 ~ 2017 - innumerable test runs by M. Kim (short article in New Physics: Sae Mulli) supporting parallel calculation by openMP
- 2018 - advertising and joining Transport Model Evaluation Project (TMEP)
- 2019 ~ 2020 - application of parity doublet model in HIC (dynamical properties)
- 2021 ~ - study of pion production and symmetry energy

Transport Model Evaluation Project

- Transport2014 (2014): Mainly 100A MeV, also 400A MeV Au+Au collisions. Stability, stopping, and flow of NN scatterings

Understanding transport simulations of heavy-ion collisions at 100A and 400A MeV: Comparison of heavy-ion transport codes under controlled conditions

PHYSICAL REVIEW C **93**, 044609 (2016)

Jun Xu,^{1,*} Lie-Wen Chen,^{2,†} ManYee Betty Tsang,^{3,‡} Hermann Wolter,^{4,§} Ying-Xun Zhang,^{5,||} Joerg Aichelin,⁶ Maria Colonna,⁷ Dan Cozma,⁸ Pawel Danielewicz,³ Zhao-Qing Feng,⁹ Arnaud Le Fèvre,¹⁰ Theodoros Gaitanos,¹¹ Christoph Hartnack,⁶ **Kyungil Kim,¹² Youngman Kim,¹²** Che-Ming Ko,¹³ Bao-An Li,¹⁴ Qing-Feng Li,¹⁵ Zhu-Xia Li,⁵ Paolo Napolitani,¹⁶ Akira Ono,¹⁷ Massimo Papa,¹⁸ Taesoo Song,¹⁹ Jun Su,²⁰ Jun-Long Tian,²¹ Ning Wang,²² Yong-Jia Wang,¹⁵ Janus Weil,¹⁹ Wen-Jie Xie,²³ Feng-Shou Zhang,²⁴ and Guo-Qiang Zhang¹

RBUU from Germany

- Transport2017 (2017): Box calculation of NN scatterings, mean-field evolutions, and pion-like particle production

Comparison of heavy-ion transport simulations: Collision integral in a box

PHYSICAL REVIEW C **97**, 034625 (2018)

Ying-Xun Zhang,^{1,2,*} Yong-Jia Wang,^{3,†} Maria Colonna,^{4,‡} Pawel Danielewicz,^{5,§} Akira Ono,^{6,||} Manyee Betty Tsang,^{5,¶} Hermann Wolter,^{7,#} Jun Xu,^{8,**} Lie-Wen Chen,⁹ Dan Cozma,¹⁰ Zhao-Qing Feng,¹¹ Subal Das Gupta,¹² Natsumi Ikeno,¹³ Che-Ming Ko,¹⁴ Bao-An Li,¹⁵ Qing-Feng Li,^{3,11} Zhu-Xia Li,¹ Swagata Mallik,¹⁶ Yasushi Nara,¹⁷ Tatsuhiko Ogawa,¹⁸ Akira Ohnishi,¹⁹ Dmytro Oliinychenko,²⁰ Massimo Papa,⁴ Hannah Petersen,^{20,21,22} Jun Su,²³ Taesoo Song,^{20,21} Janus Weil,²⁰ Ning Wang,²⁴ Feng-Shou Zhang,^{25,26} and Zhen Zhang¹⁴

Comparison of heavy-ion transport simulations:

Collision integral with pions and Δ resonances in a box

PHYSICAL REVIEW C **100**, 044617 (2019)

Akira Ono,^{1,*} Jun Xu,^{2,3,†} Maria Colonna,⁴ Pawel Danielewicz,⁵ Che Ming Ko,⁶ Manyee Betty Tsang,⁵ Yong-Jia Wang,⁷ Hermann Wolter,⁸ Ying-Xun Zhang,^{9,10} Lie-Wen Chen,¹¹ Dan Cozma,¹² Hannah Elfner,^{13,14,15} Zhao-Qing Feng,¹⁶ Natsumi Ikeno,^{17,18} Bao-An Li,¹⁹ Swagata Mallik,²⁰ Yasushi Nara,²¹ Tatsuhiko Ogawa,²² Akira Ohnishi,²³ Dmytro Oliinychenko,²⁴ Jun Su,²⁵ Taesoo Song,¹³ Feng-Shou Zhang,^{26,27} and Zhen Zhang²⁵

DJBUU from Korea

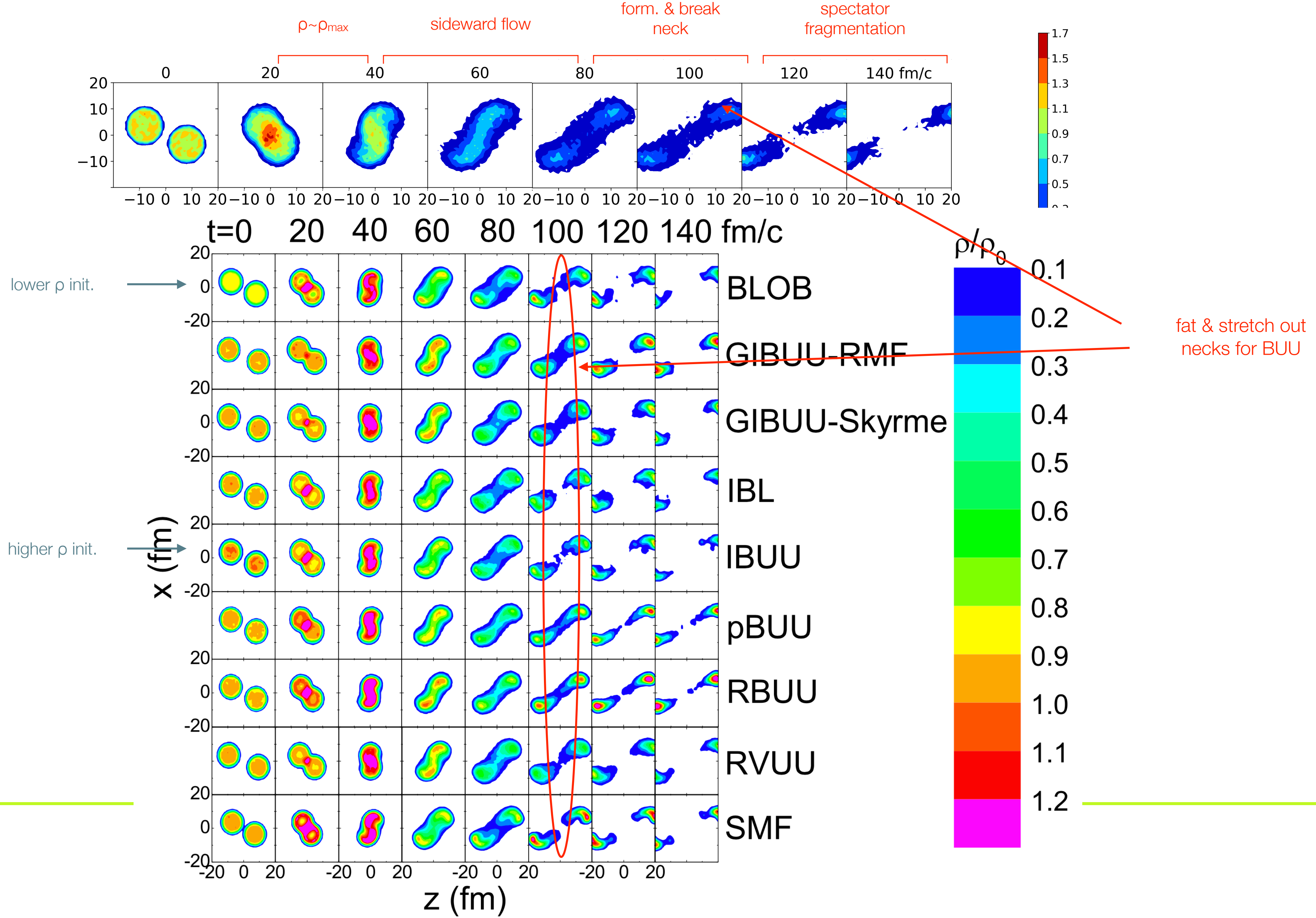
Comparison of heavy-ion transport simulations: Mean-field dynamics in a box

PHYSICAL REVIEW C **104**, 024603 (2021)

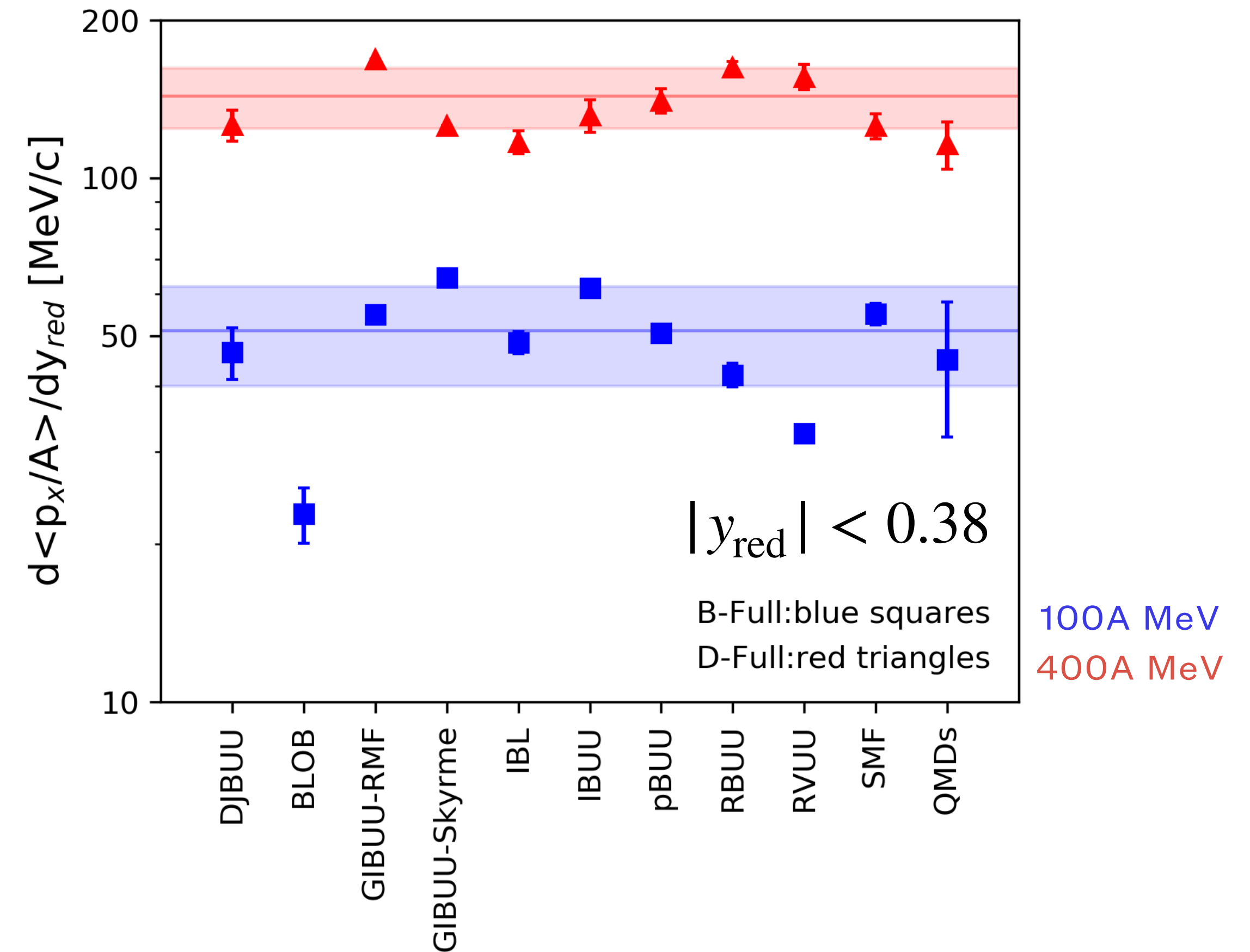
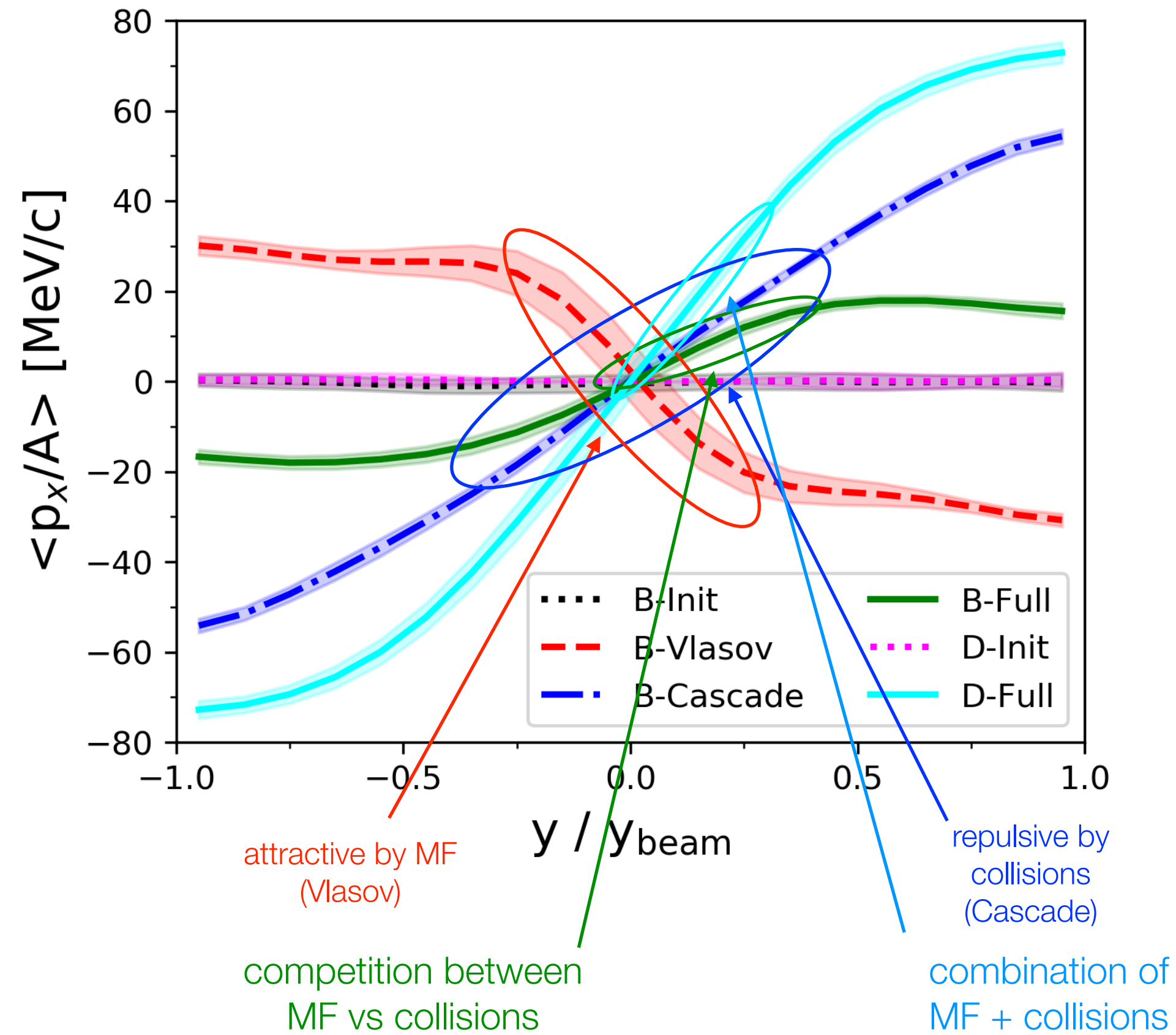
Maria Colonna,^{1,†} Ying-Xun Zhang,^{2,3,‡} Yong-Jia Wang,^{4,§} Dan Cozma,⁵ Pawel Danielewicz,^{6,§} Che Ming Ko,⁷ Akira Ono,^{8,||} Manyee Betty Tsang,^{6,¶} Rui Wang,^{9,||} Hermann Wolter,^{11,#} Jun Xu,^{12,9,**} Zhen Zhang,¹³ Lie-Wen Chen,¹⁴ Hui-Gan Cheng,¹⁵ Hannah Elfner,^{16,17,18} Zhao-Qing Feng,¹⁹ **Myungkuk Kim,¹⁹ Youngman Kim,²⁰ Sangyong Jeon,²¹ Chang-Hwan Lee,²²** Bao-An Li,²³ Qing-Feng Li,^{4,24} Zhu-Xia Li,² Swagata Mallik,²⁵ Dmytro Oliinychenko,^{26,27} Jun Su,¹³ Taesoo Song,^{16,28} Agnieszka Sorensen,²⁹ and Feng-Shou Zhang^{30,31}

- Transport2019 (2019): production of pion-like particles at 270A MeV Sn+Sn collisions.

Average density in time steps of Au+Au @ 100A MeV



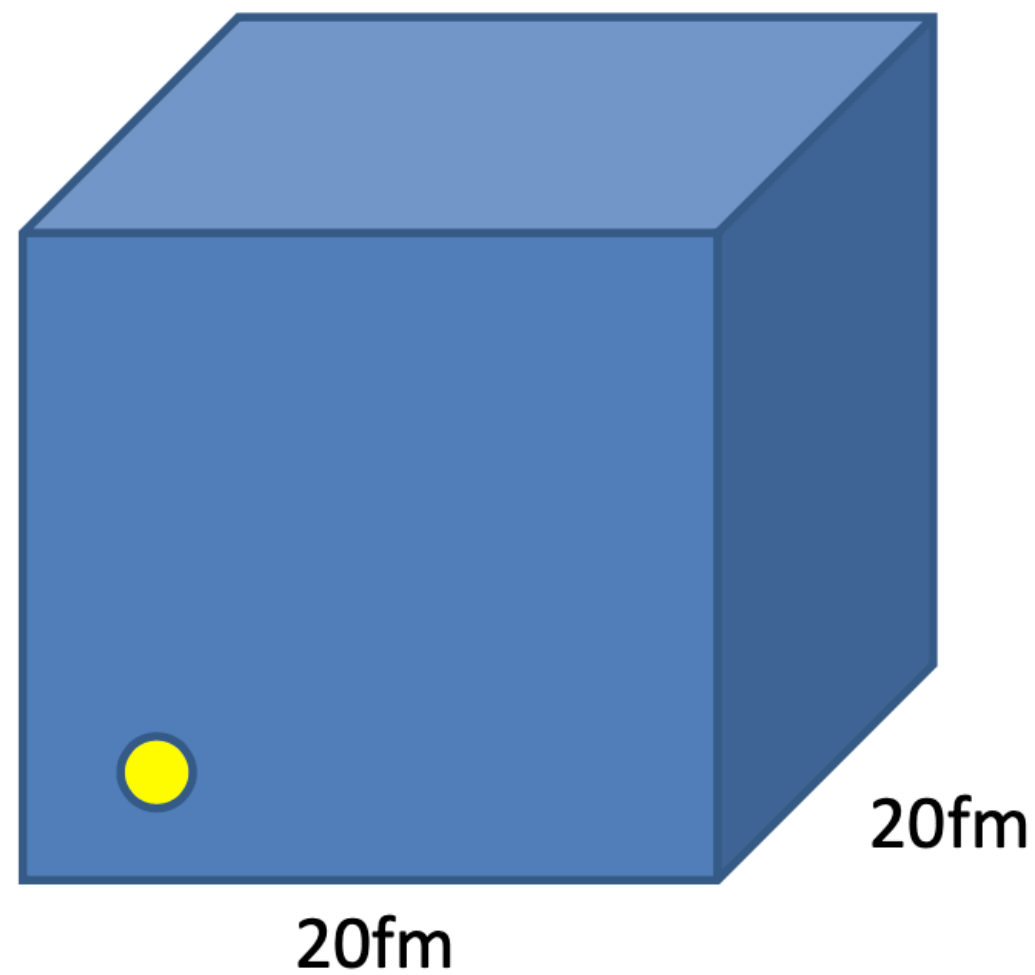
Transverse flow and slop parameter



- Theoretical uncertainties of flow parameter: about 30% at 100A MeV and 13% at 400A MeV

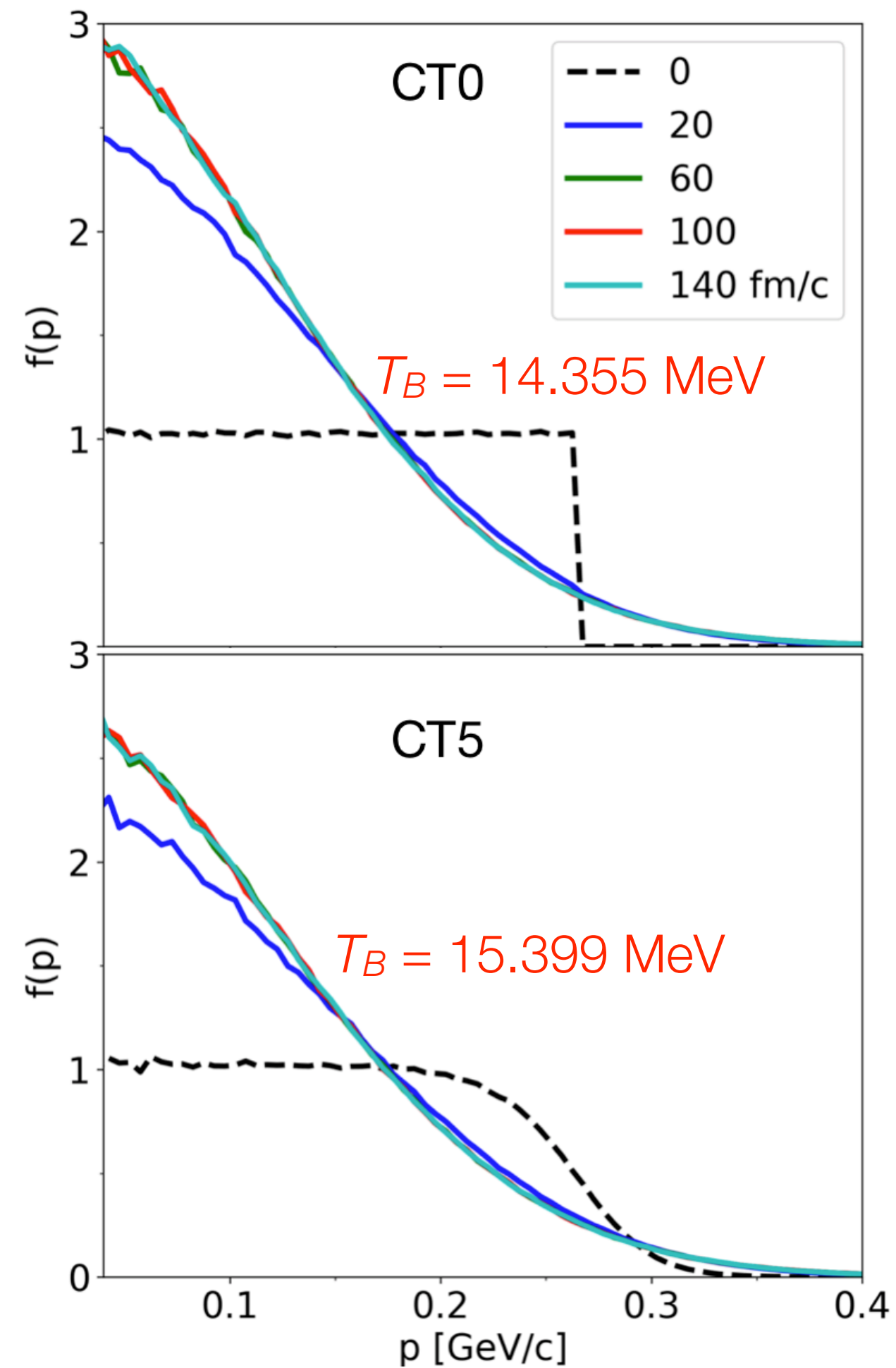
- What is the origin of the uncertainties? from collisions or interactions (MF)

Box calculations with periodic boundary conditions

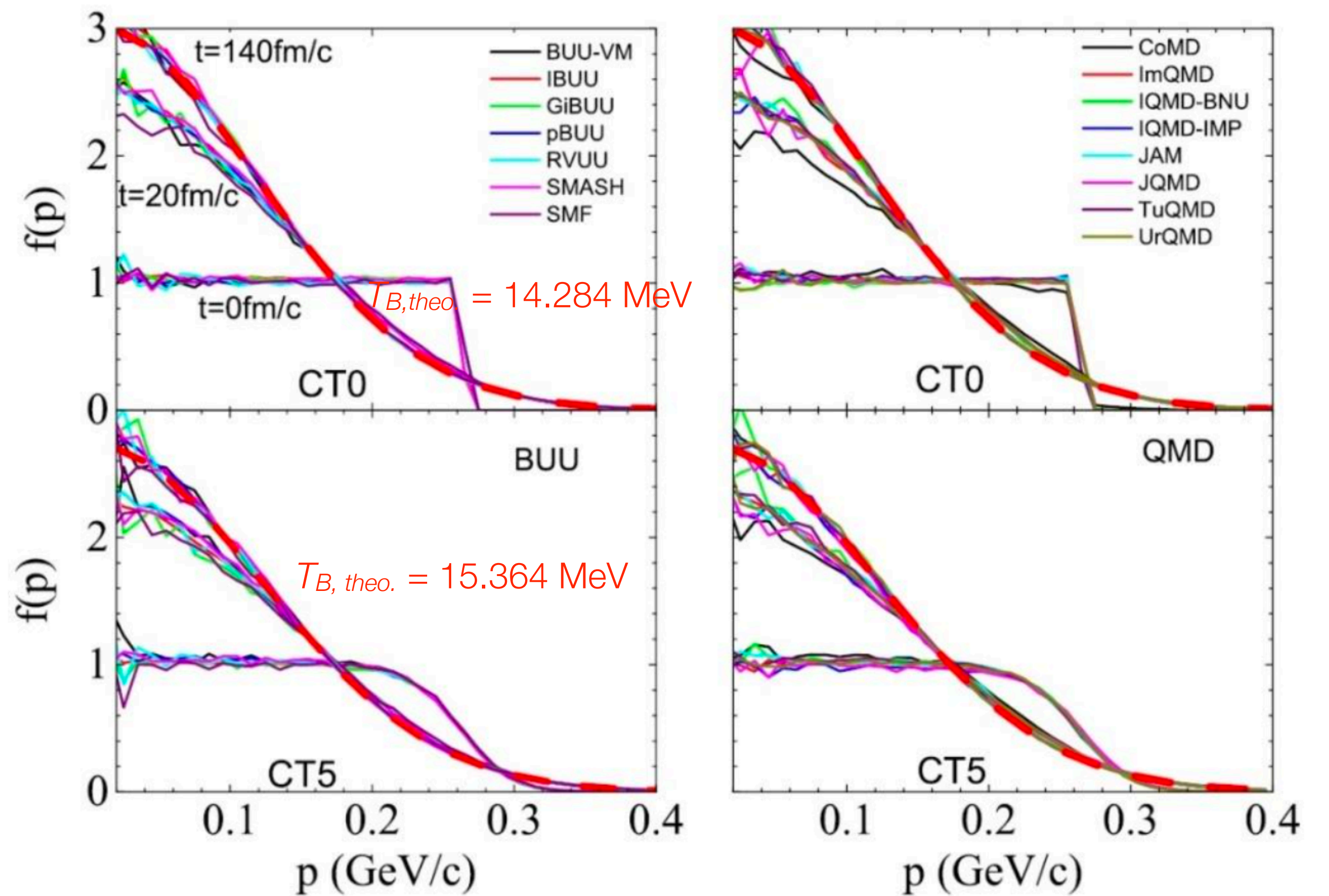


- Details of periodic boundary conditions
 - a box of volume $V = L1*L2*L3$, where the system is confined
 - the position of the center of box is $(L1/2, L2/2, L3/2)$
 - a particle leaving the box, entering the opposite side w/ same momentum (number of particle is conserved)
- Initialization
 - uniform density with $\rho_0 = 0.16 \text{ fm}^{-3}$, with isospin asymmetry = 0 (1280 nucleons, 640 protons and 640 neutrons)

Box-Cascade calculation (NN scatterings w/o PB)

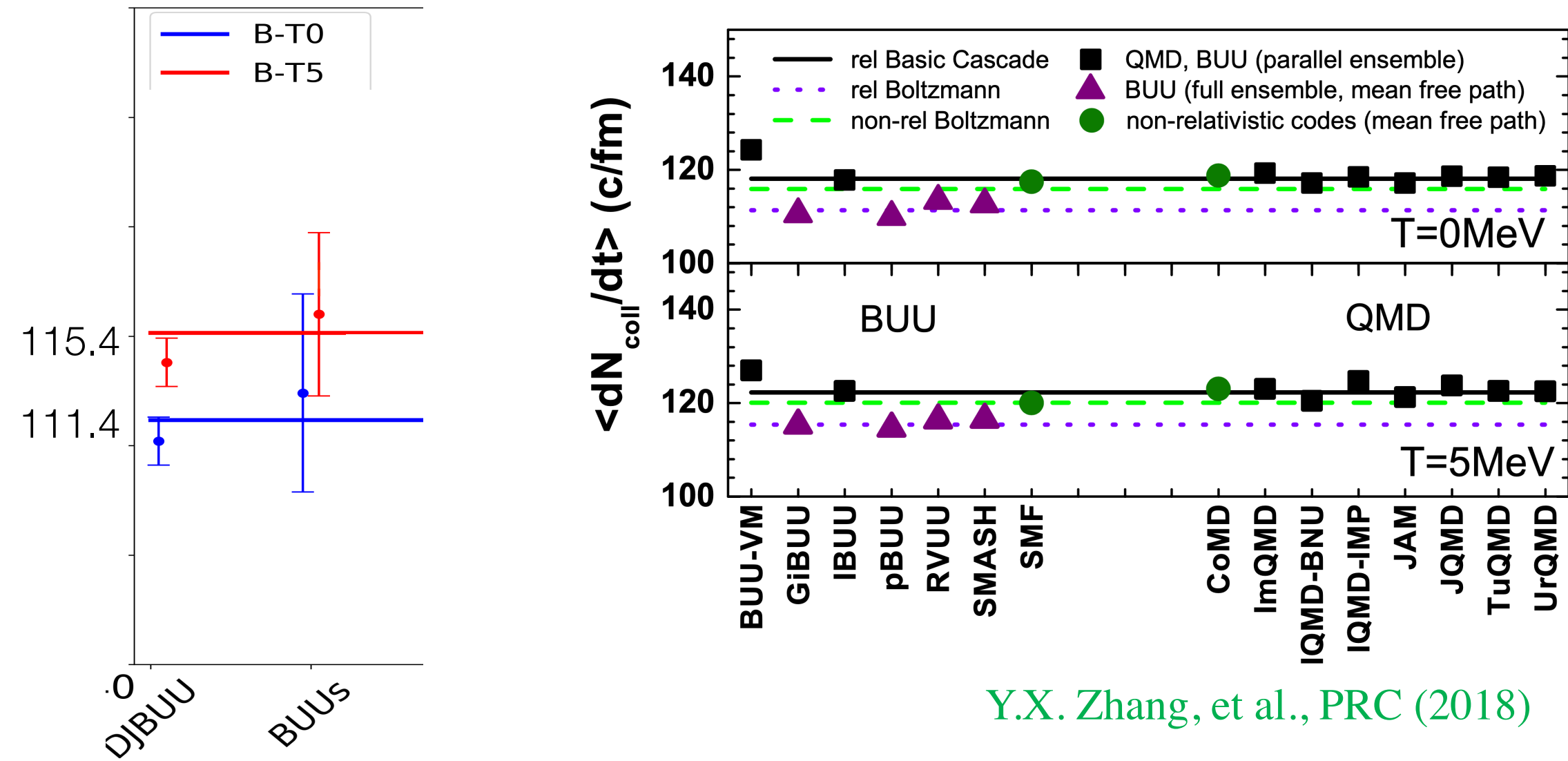


Time evolution of momentum distribution



Box-Cascade calculation

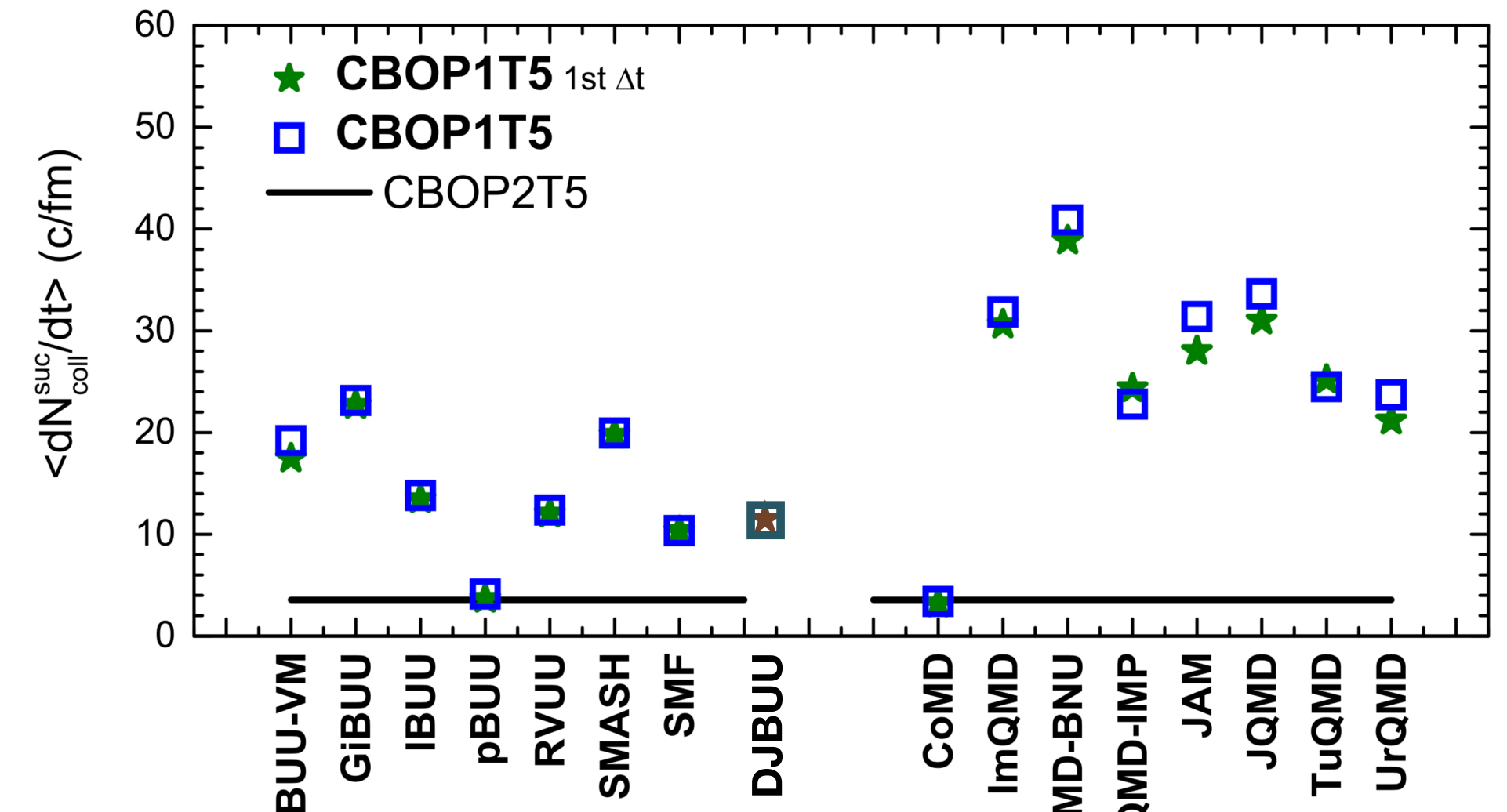
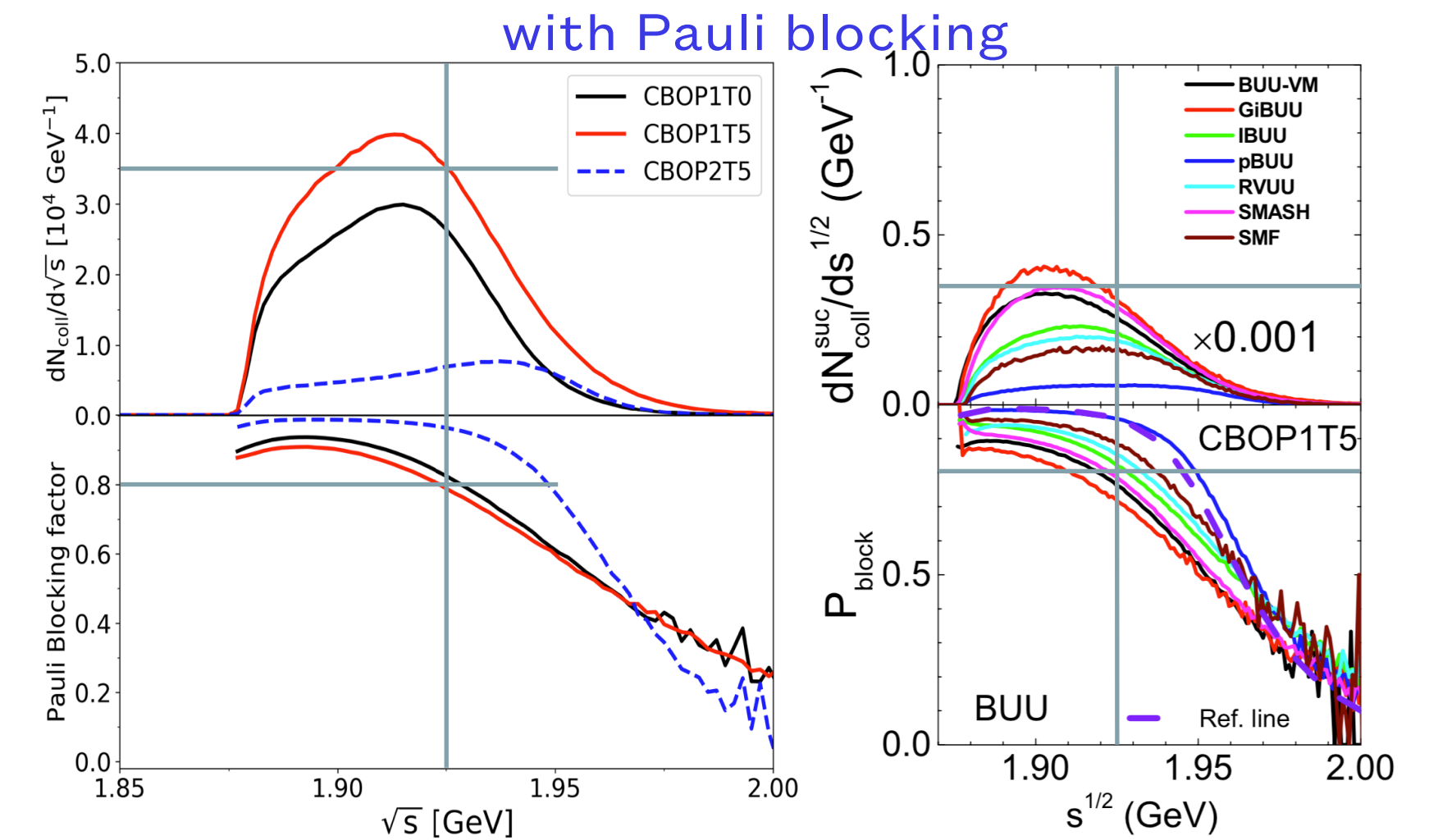
without Pauli blocking
averaged over $t=60-140$ fm/c



Y.X. Zhang, et al., PRC (2018)

comparable DJBUU with rel. kinetic theory

- well under control
- not essentially affect to results of HIC simulation

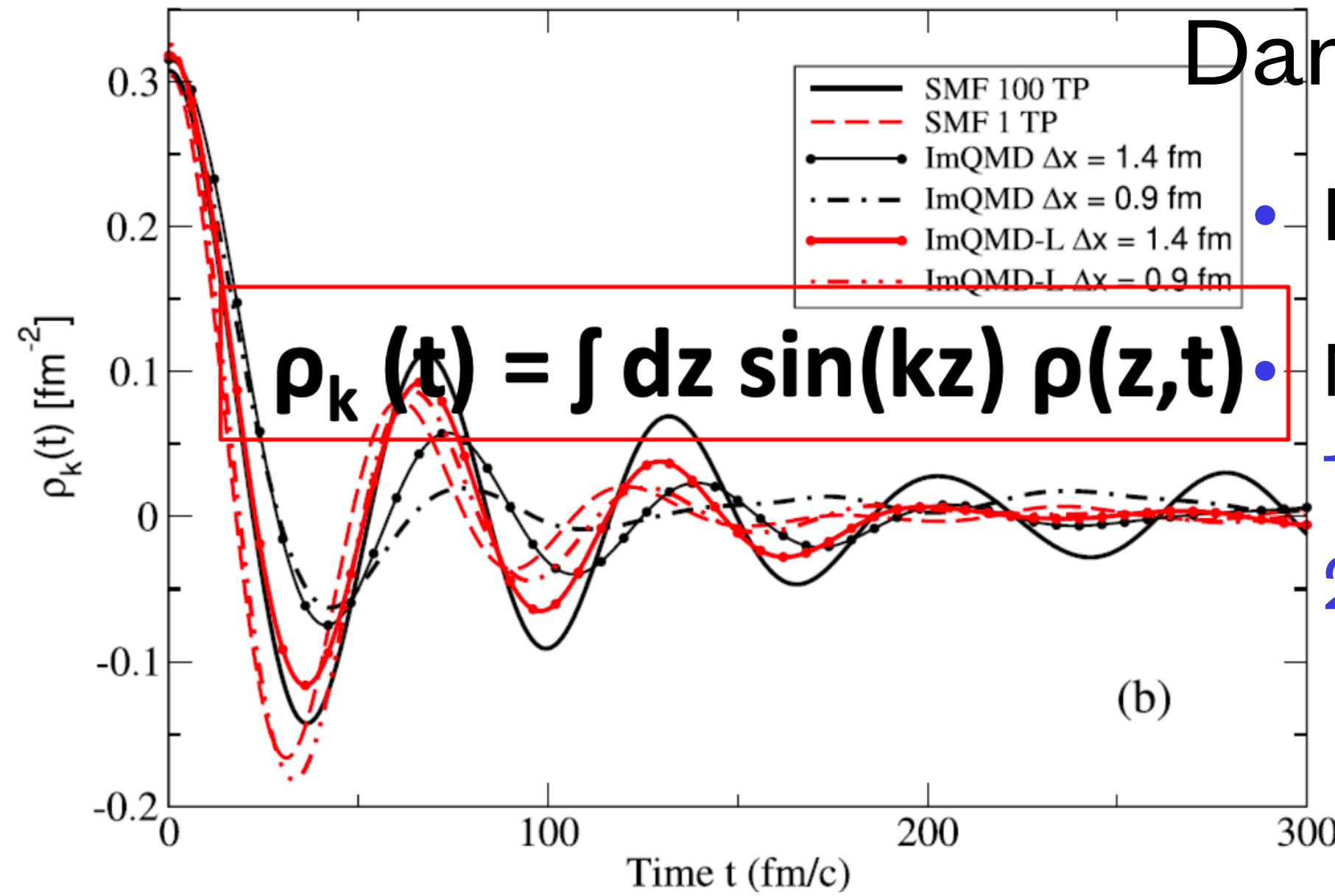
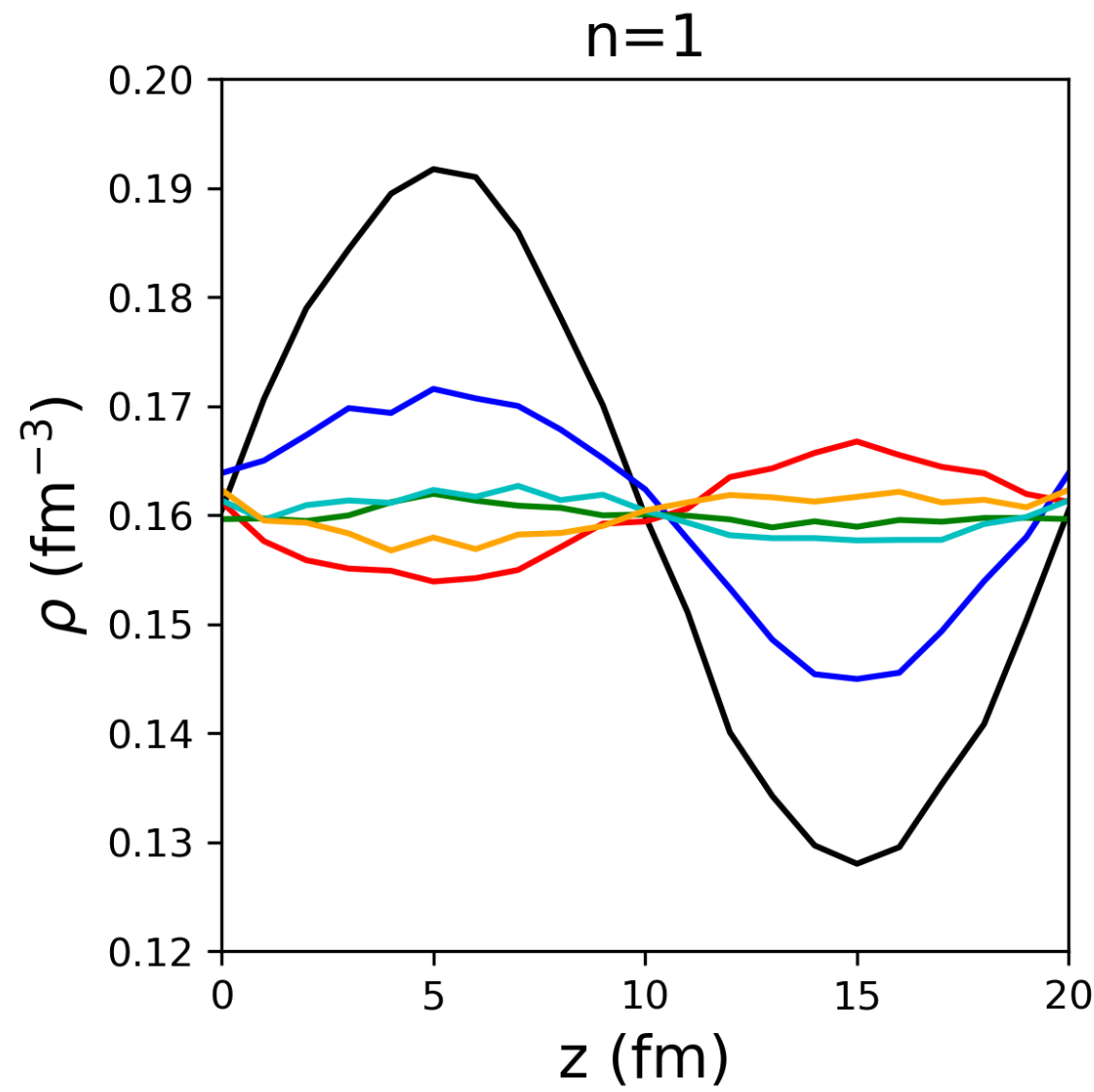


- Pauli blocking - evolution of phase space occupations

- numerical fluctuations
 - BUU - shape & TP, QMD - width

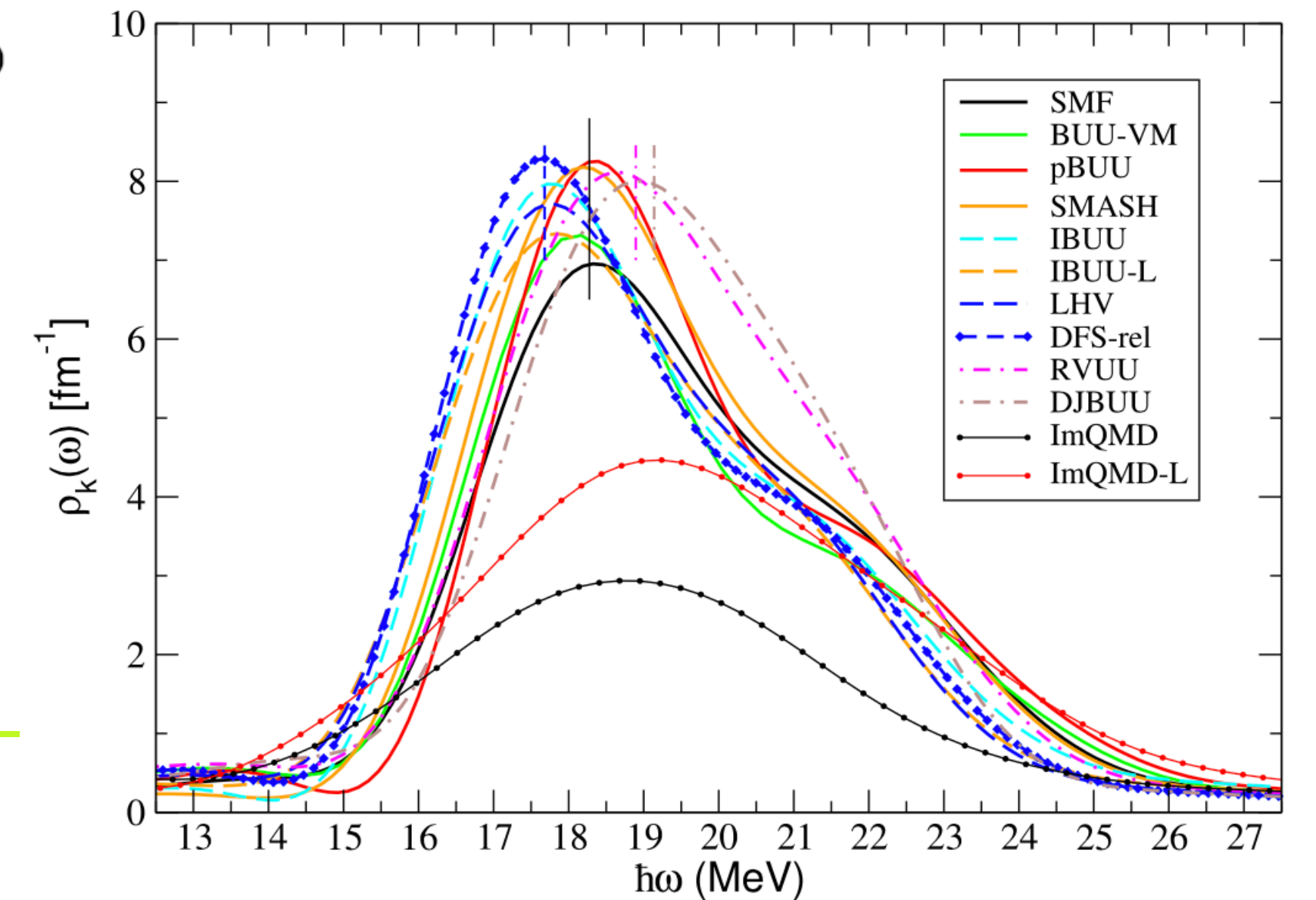
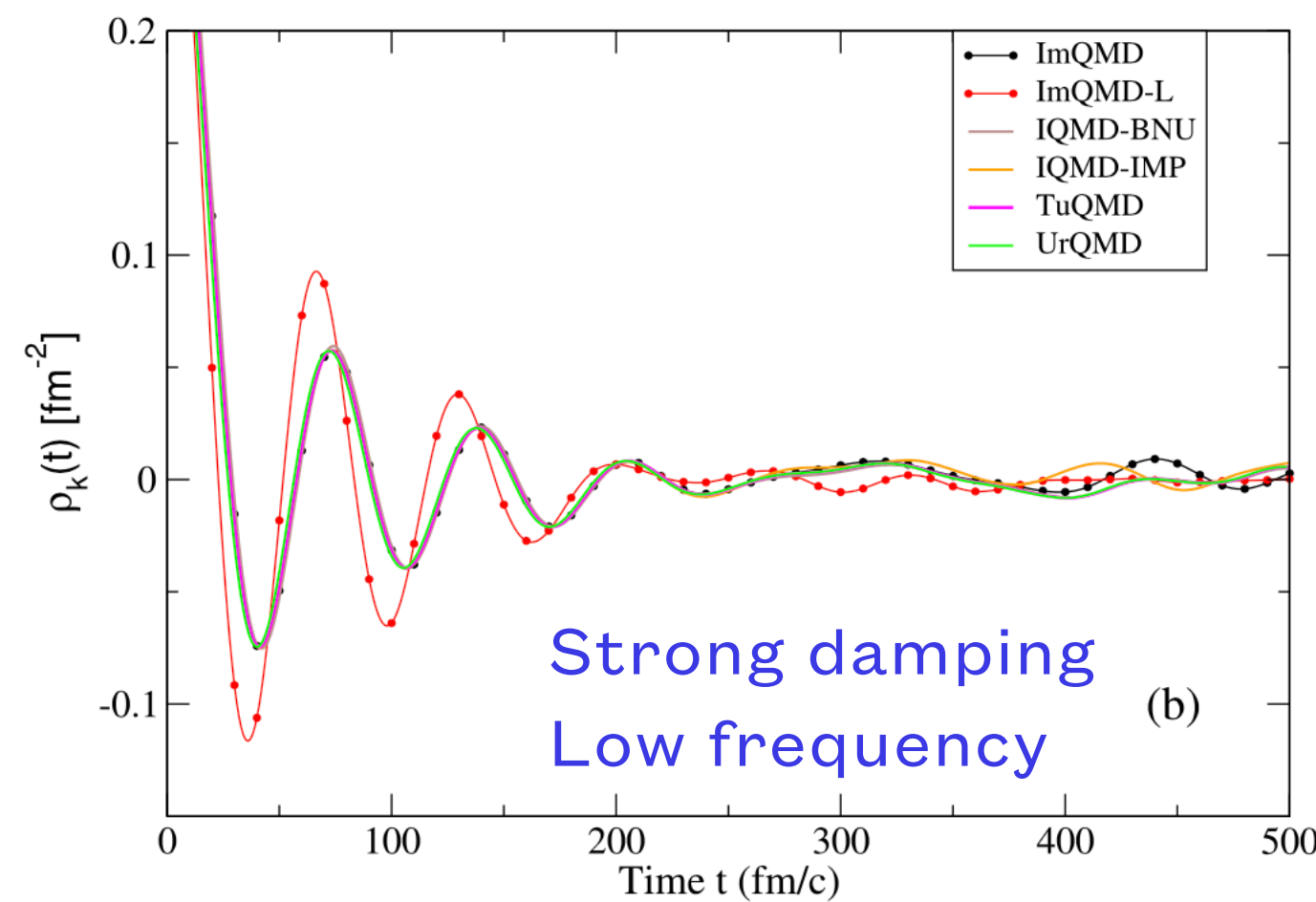
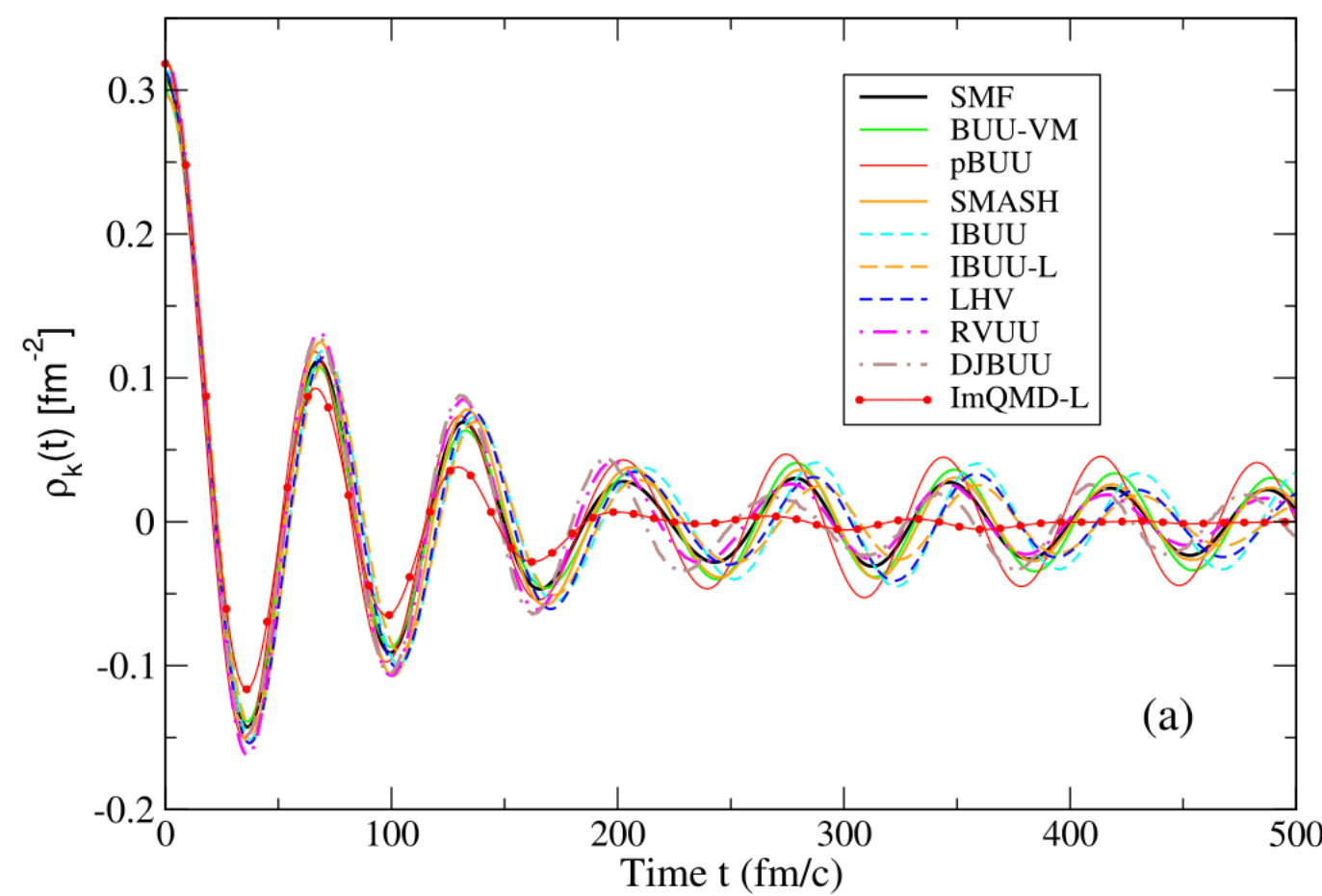
Box-Vlasov calculation

M. Colonna, et al., PRC (2021)



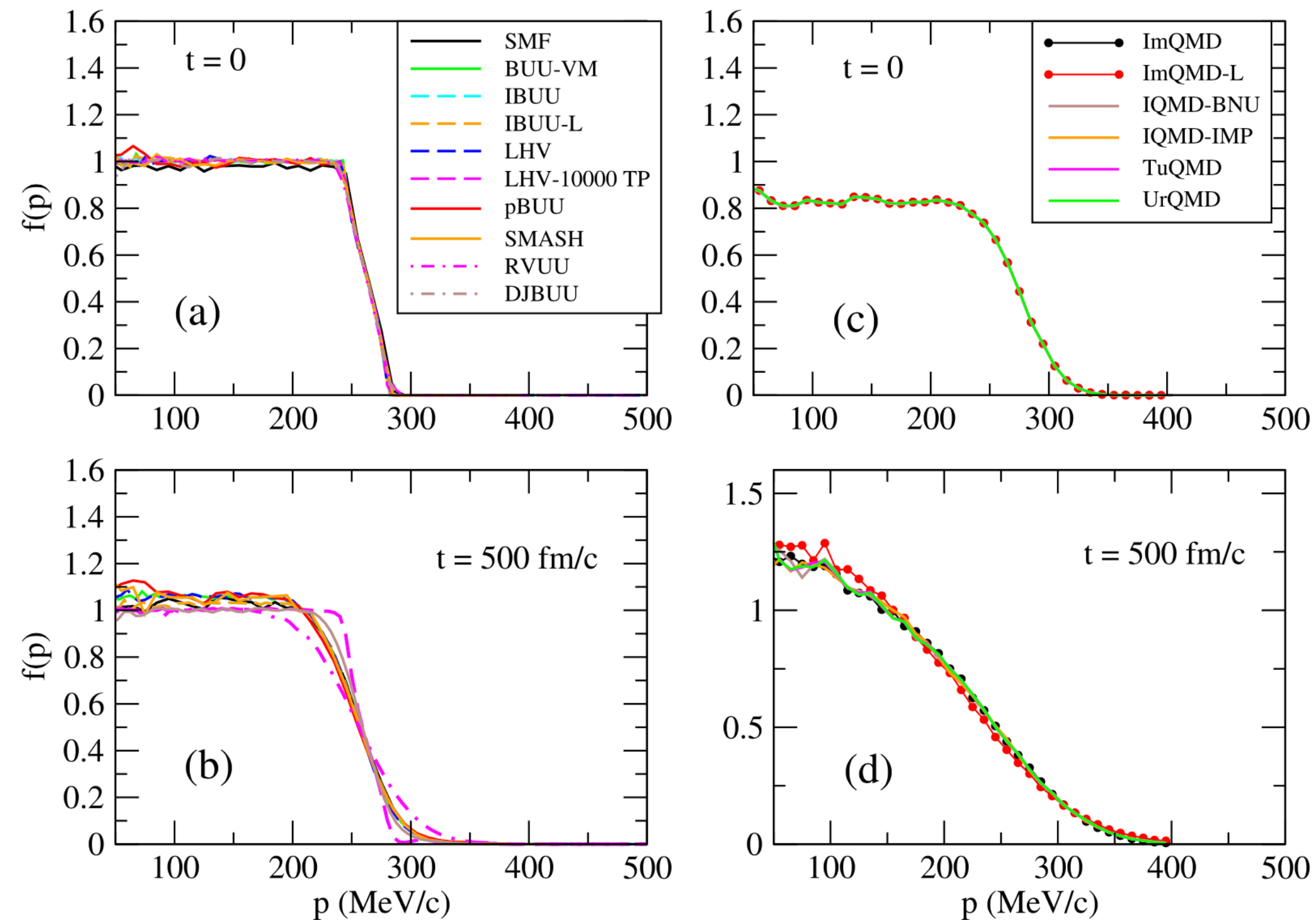
Damping sources:

- Landau damping: mixing modes
- Numerical damping: fluctuations
- 1. Decreases with increasing TP numbers
- 2. Decreases with increasing particle size



Box-Vlasov calculation

Momentum distribution



M. Colonna, et al., PRC (2021)

- top: initial configurations
- bottom: final configurations
- larger smearing in QMD due to larger intrinsic initial density fluctuations
- more Boltzmann-like statistics in QMD by inherent larger fluctuations

RAON / LAMPS

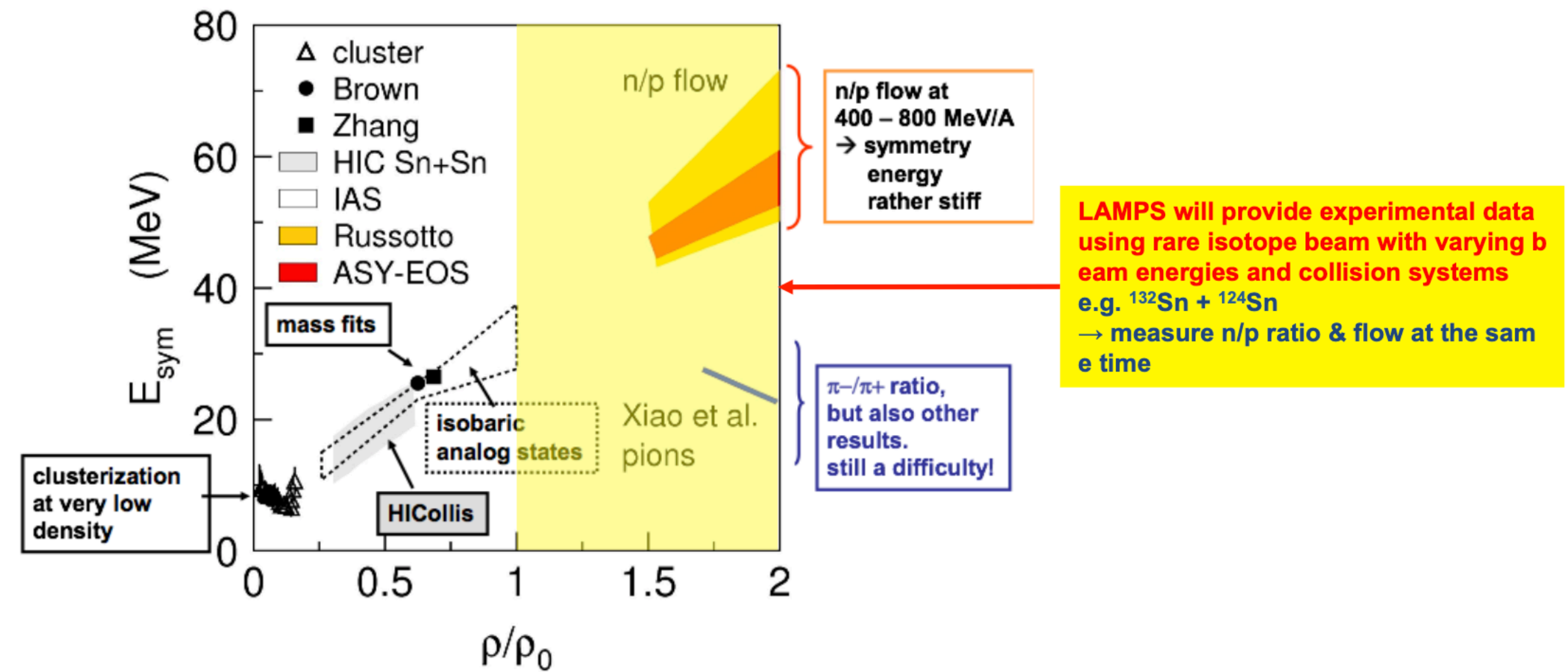


LAMPS (Large Acceptance Multi-Purpose Spectrometer)



- Possible experiment
 - Using 18.5 ~ 250 MeV/u RI beam through IF separator, perform N/Z controlled heavy-ion collision experiment for studying density dependent symmetry energy of nuclear matter possible Day-1 experiment : $^{50,54}\text{Ca} + ^{40}\text{Ca}$ to measure proton, neutron spectrum
 - Then, series of experiment for $^{50,54}\text{Ca} + ^{40}\text{Ca}$, $^{68,70,72}\text{Ni} + ^{58}\text{Ni}$, $^{106,112,124,130,132}\text{Sn} + ^{112,118,124}\text{Sn}$ to measure particle spectrum, yield, ratio, collective flow etc. at the same time

Present Constraints on the Symmetry Energy (shown as $E_{\text{sym}}(\rho/\rho_0)$)

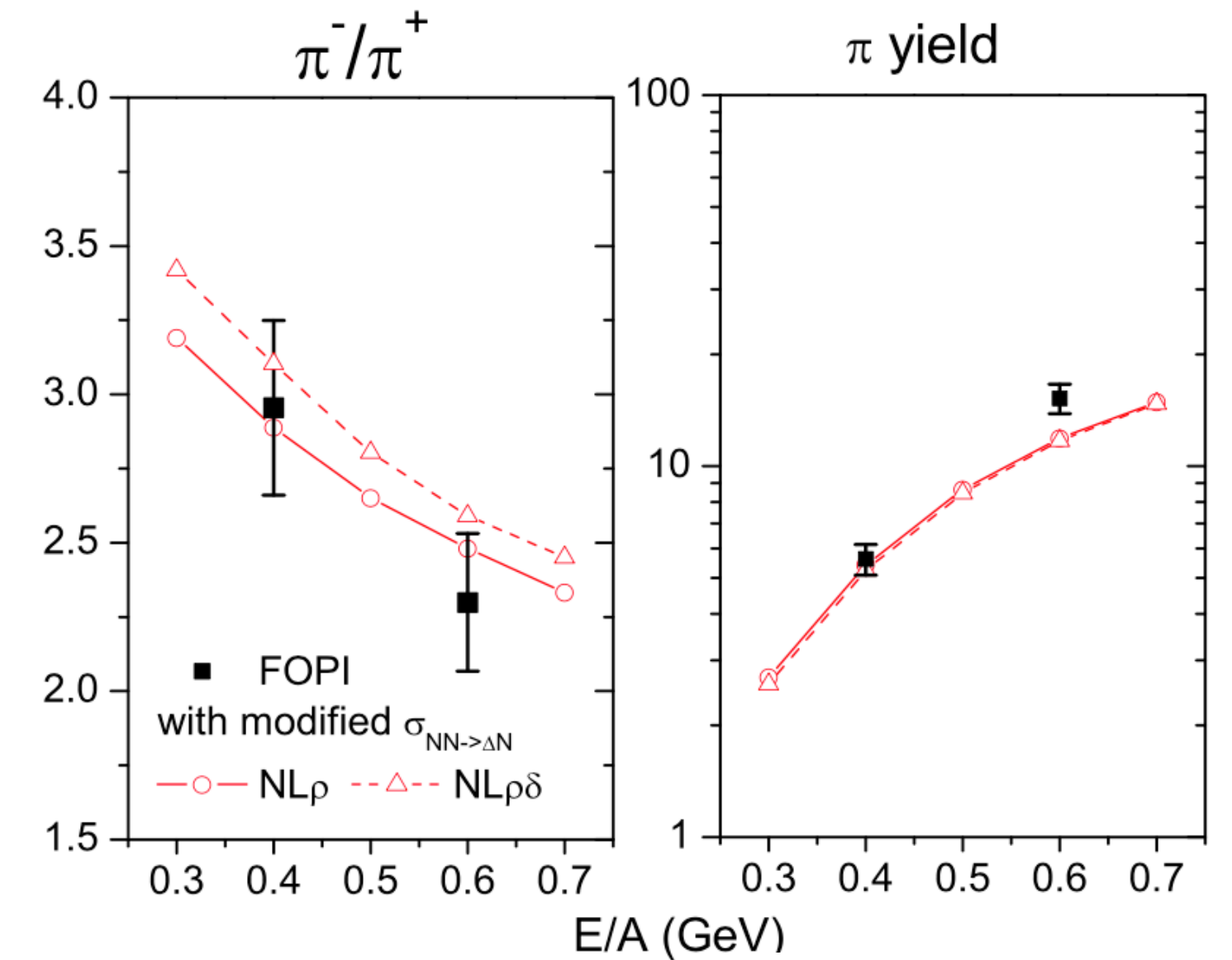
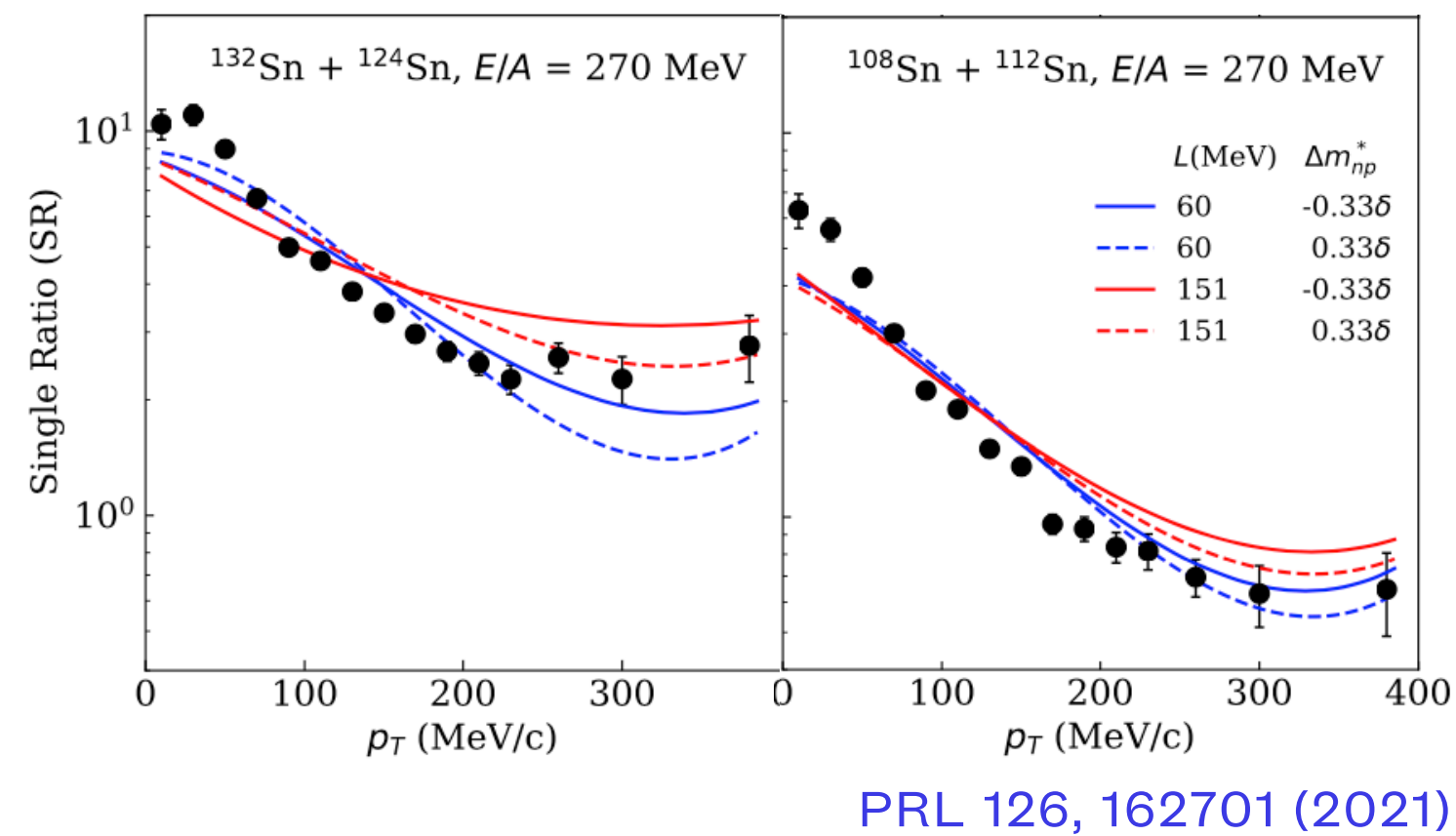
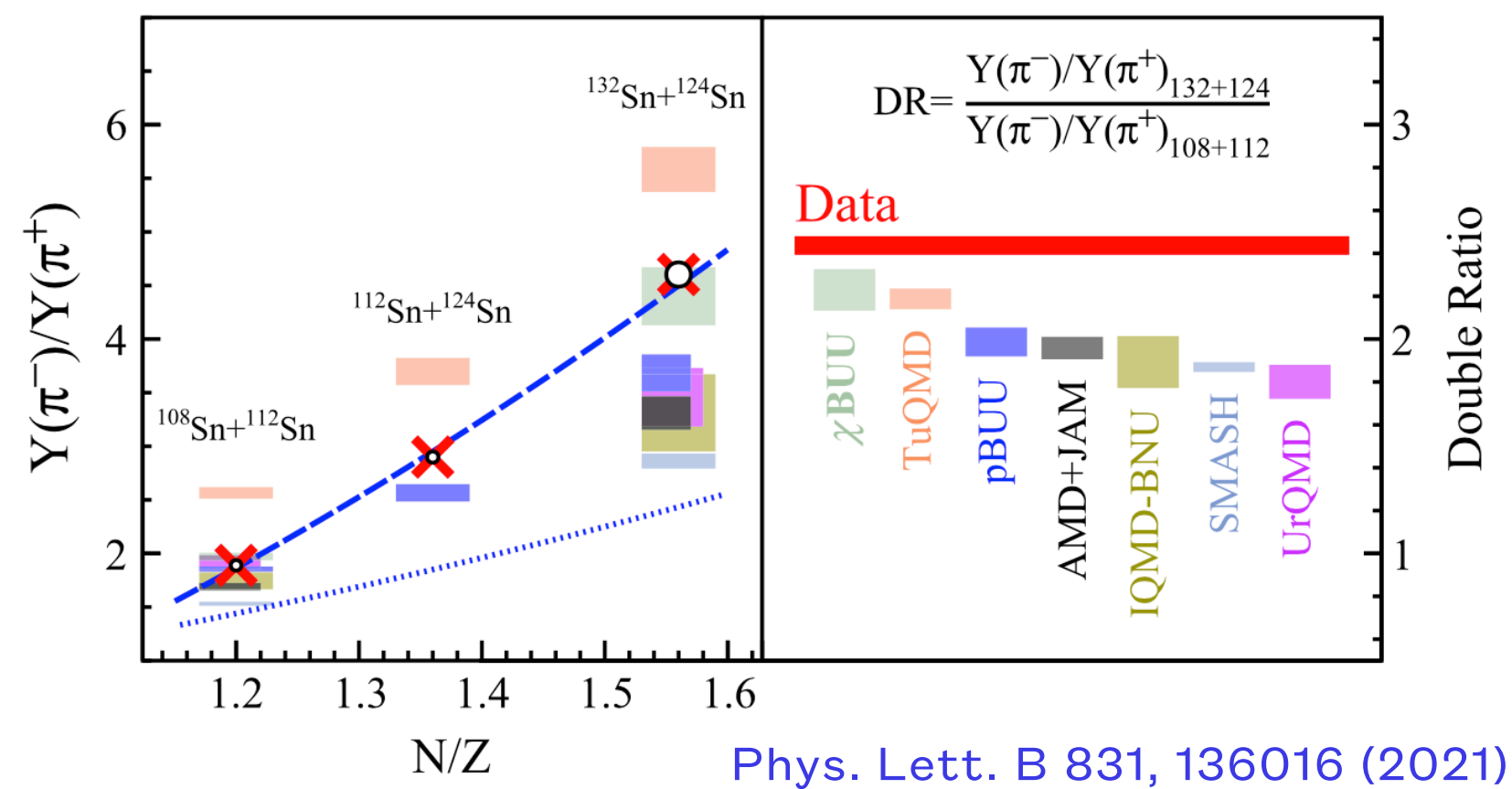


LAMPS will provide experimental data using rare isotope beam with varying beam energies and collision systems e.g. $^{132}\text{Sn} + ^{124}\text{Sn}$ → measure n/p ratio & flow at the same time

- Experimental data are measured with stable beams
- data of pion ratio and data of n/p flow are from different experiments
- Models in the market show different results even within same observable

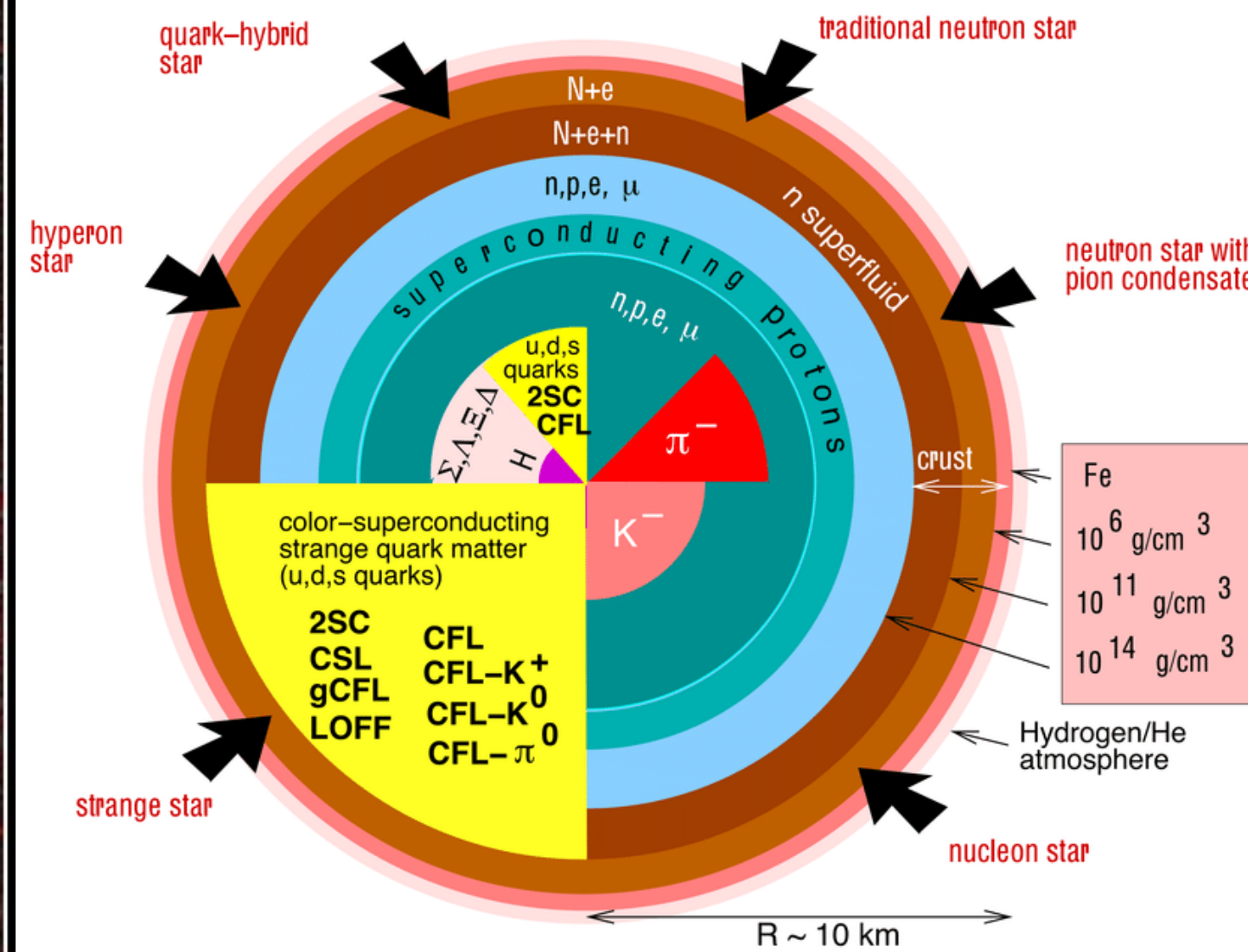
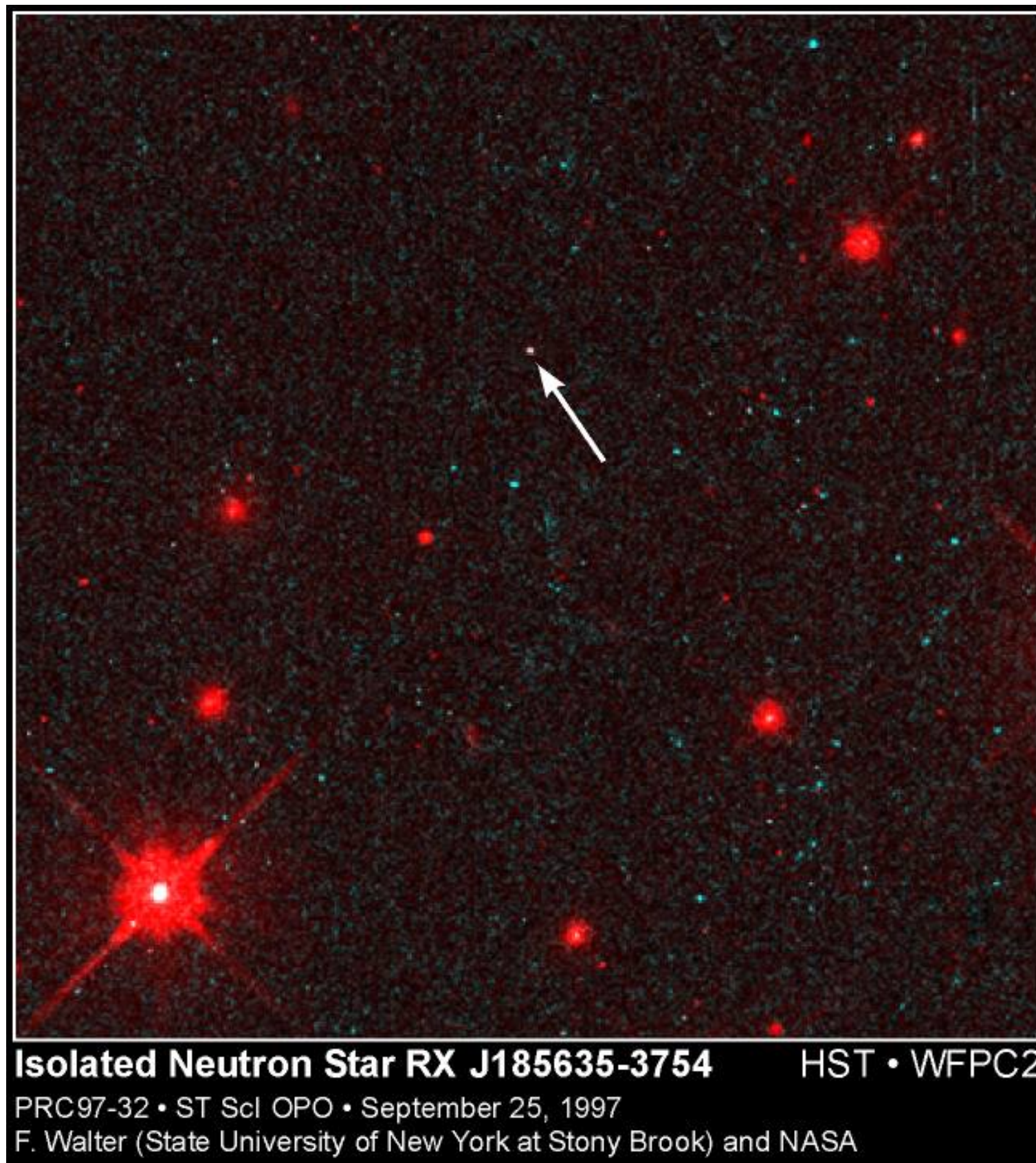
Symmetry energy and pion productions

- Pion production and comparison with $S\pi RIT$ @ RIKEN and FOPI @ GSI experiments
- Pion production w/ our NL model set in DJBUU (on going)
- Expansion to HICs with rare isotope : π^- from neutron-rich
- rare isotope HICs @ RAON can be a key for symmetry energy since more π^- from neutron rich



Neutron Stars - dense matter in universe

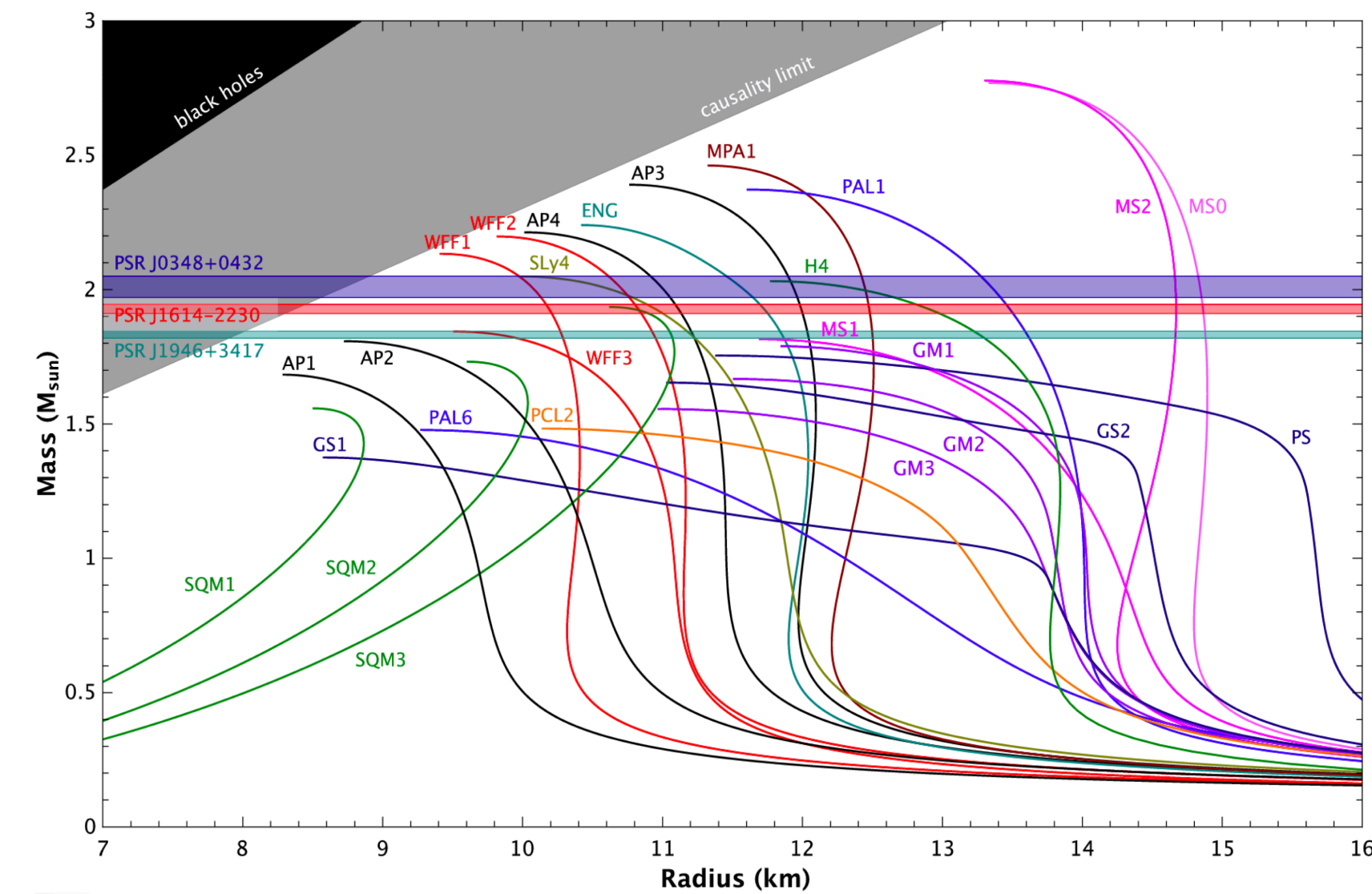
- densest visible matter(?), $\rho_{\text{center}} \sim 2-8 \rho_0$
- M: 1.5-2 solar mass, R: ~15km



solving TOV eq.

$$\frac{dP(r)}{dr} = -G \frac{[\epsilon(r) + P(r)][M(r) + 4\pi r^3 P(r)]}{r^2 [1 - 2GM(r)/r]}$$

$$\frac{dM(r)}{dr} = 4\pi \epsilon(r) r^2,$$



Mass and Radius estimation from X-ray bursts

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**Astronomy
&
Astrophysics**

Measuring the masses and radii of neutron stars in low-mass X-ray binaries: Effects of the atmospheric composition and touchdown radius

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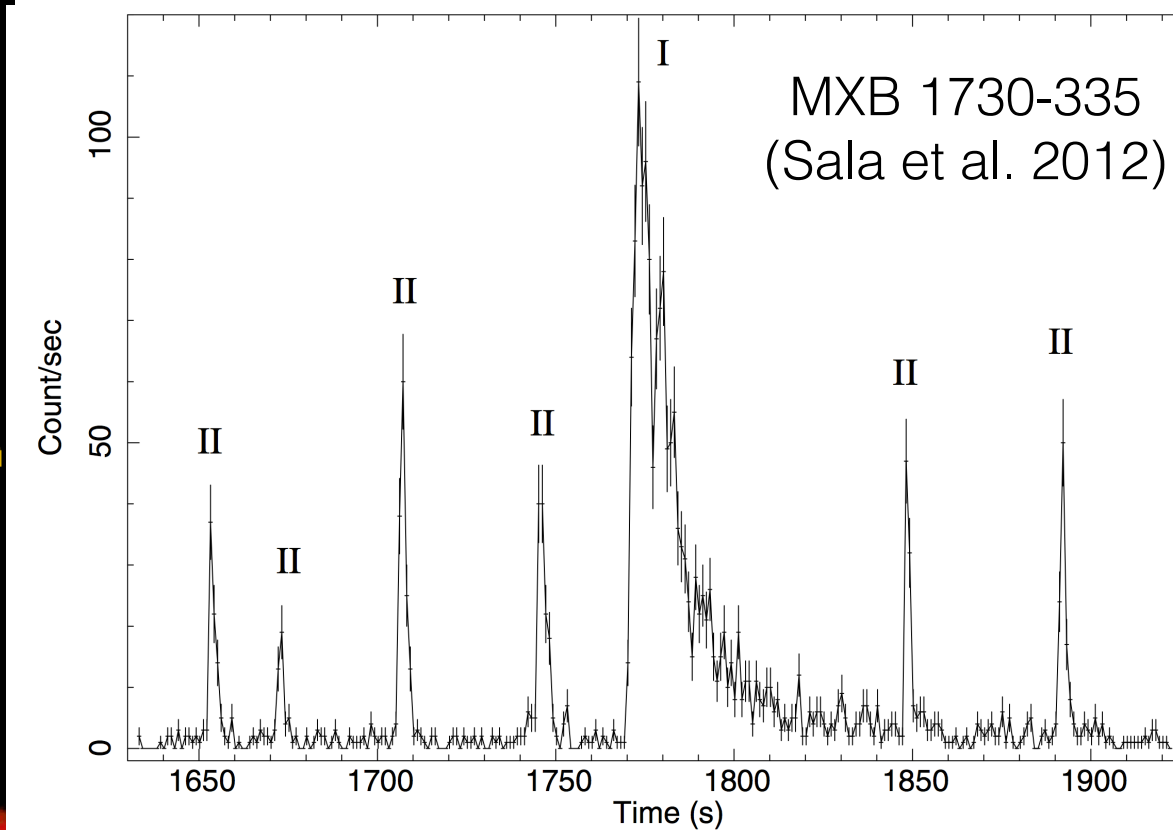
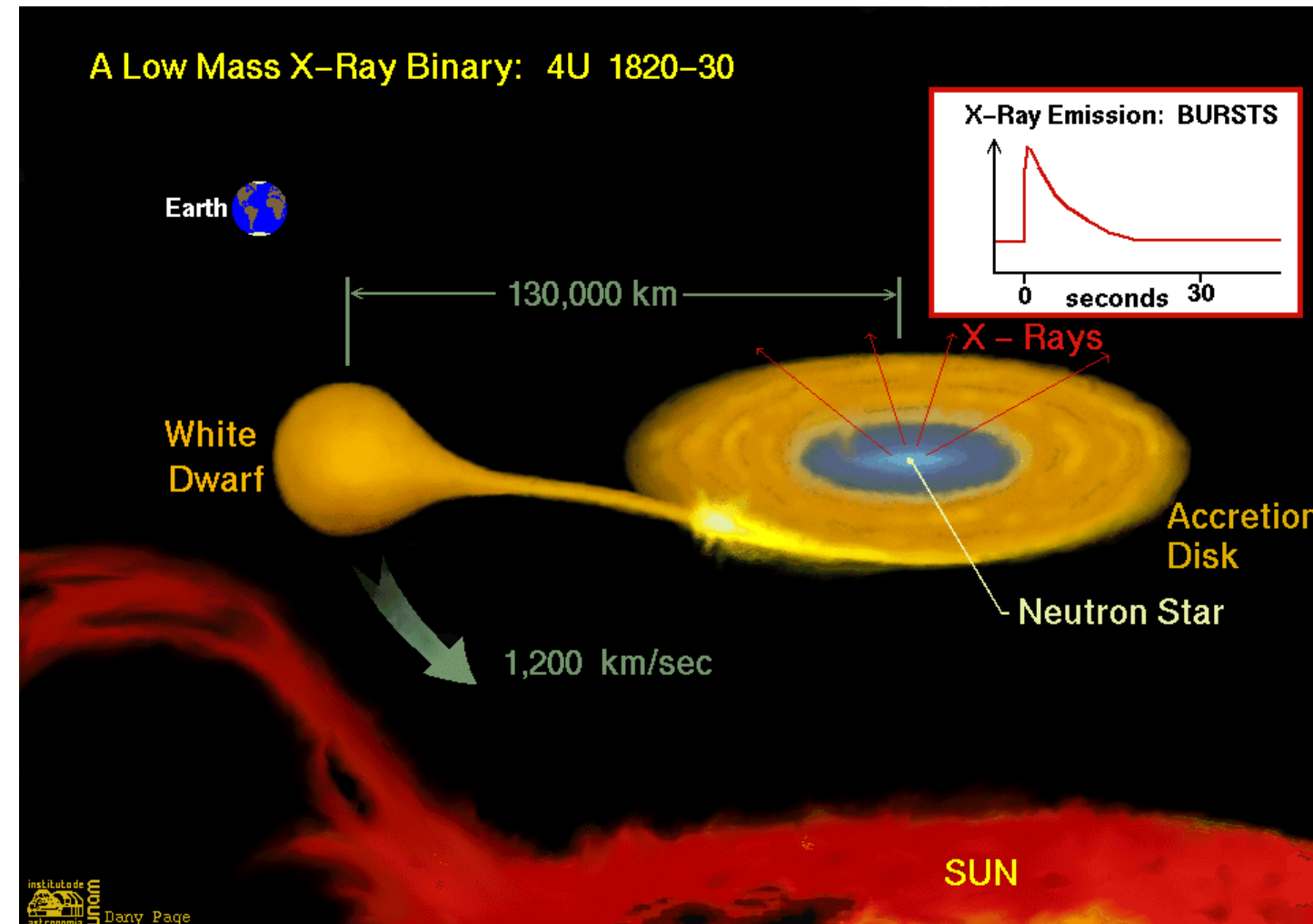
Received 9 April 2020 / Accepted 26 March 2021

ABSTRACT

Low-Mass X-ray Binaries and X-ray Bursts

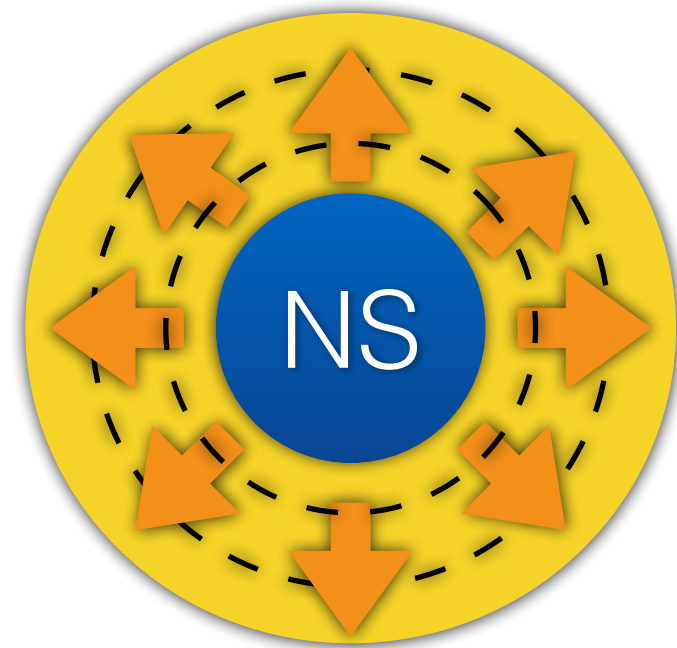


- Binary star system (NS or BH - MS or WD or RG)
- Mass transfer by Roche lobe overflow
- quiescent X-ray from NS surface and accretion disk

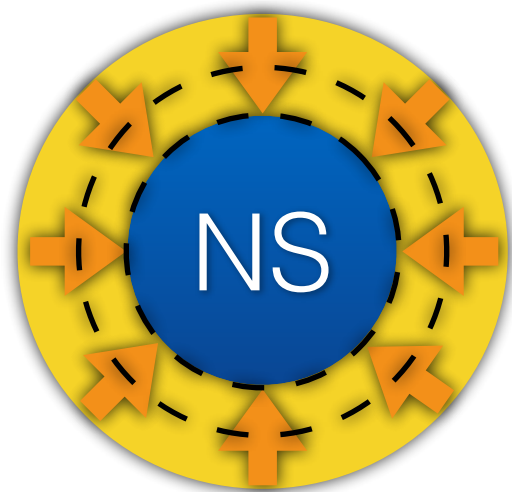


- Thermonuclear explosion (H and/or He ignition)
- Energy range ~ 10 keV (soft X-ray)
- $L_{\max} \sim 10^{38}$ erg/s (Eddington limit)
- X-ray softening during decay
- 84 bursts in 160 LMXBs (2007)

Photospheric Radius Expansion & MR estimation



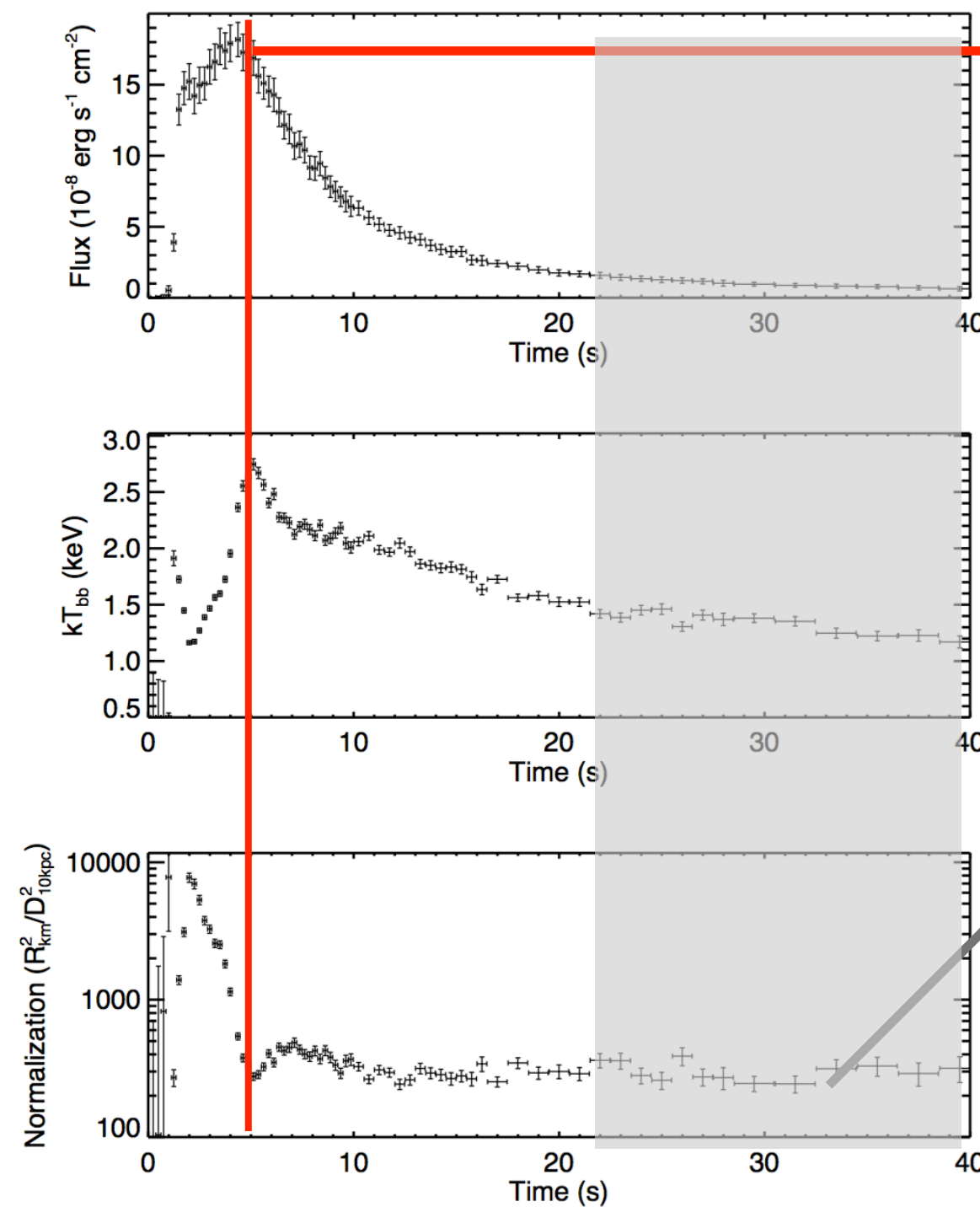
Expansion



Touchdown

Source	App. angular area (km/10 kpc) ²	Touchdown Flux (10 ⁻⁸ erg cm ⁻² s ⁻¹)	Spin Freq. ^a (Hz)	Distance ^a (kpc)
4U 1820-30	89.9±15.9	5.98±0.66	...	7.6±0.4 (4) 8.4±0.6 (5-6)
SAX J1748.9-2021	89.7±9.6	4.03±0.54	410 (1)	8.2±0.6 (4, 5, 7)
EXO 1745-248	117.8±19.9	6.69±0.74	...	6.3±0.63 ^b (8-9)
KS 1731-260	96.0±7.9	4.71±0.52	524 (2)	7-9 ^c (10)
4U 1724-207	113.8±15.4	5.29±0.58	...	7.4±0.5
4U 1608-52	314±44.3	18.5±2.0	620 (3)	4.0±2.0, D _{cutoff} > 3.9 ^d

Photospheric Radius Expansion & MR estimation



Touchdown Flux : F_{td}

apparent radius : A_{∞}

$$F_{TD,\infty} = \frac{GMc}{\kappa D^2} \left(1 - \frac{2GM}{Rc^2}\right)^{1/2} \left[1 + \left(\frac{kT_c}{38.8 \text{ keV}}\right)^{a_g} \left(1 - \frac{2GM}{Rc^2}\right)^{-a_g/2}\right]$$

$$A = f_c^{-4} \frac{R^2}{D^2} \left(1 - \frac{2GM}{Rc^2}\right)^{-1} \left\{1 + \left[\left(0.108 - 0.096 \frac{M}{M_{\odot}}\right) + \left(-0.061 + 0.114 \frac{M}{M_{\odot}}\right) \frac{R}{10\text{km}} - 0.128 \left(\frac{R}{10\text{km}}\right)^2\right] \left(\frac{f_{NS}}{1000\text{Hz}}\right)^2\right\}^2$$

- need two more theoretical parameters, $f_c = 1.4$ & $\kappa = 0.2(1 + X) \text{ cm}^2 \text{ g}^{-1}$

Mass and radius estimation

obs. $\alpha \equiv \frac{F_{\text{td}}}{\sqrt{A_\infty}} \frac{\kappa D}{c^3 f_c^2}$

$$\gamma \equiv \frac{A_\infty c^3 f_c^4}{F_{\text{td}} \kappa}$$

$$\beta = \frac{GM}{Rc^2}$$

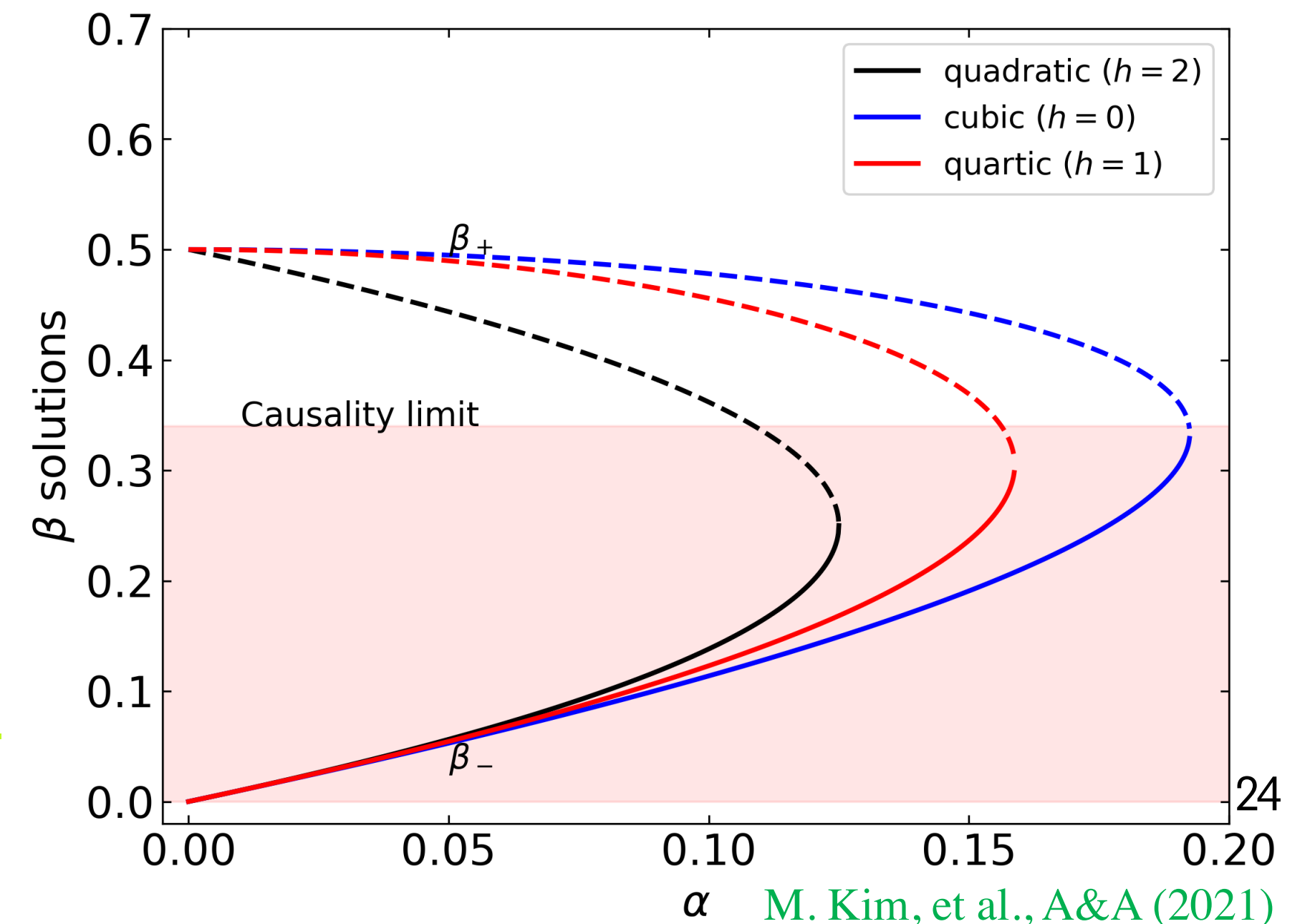
eq. $\alpha = \beta \sqrt{1 - 2\beta} \sqrt{1 - h\beta}$

$$\gamma = \frac{R}{\beta(1 - 2\beta) \sqrt{1 - h\beta}}$$

$$R = \alpha \gamma \sqrt{1 - 2\beta}$$

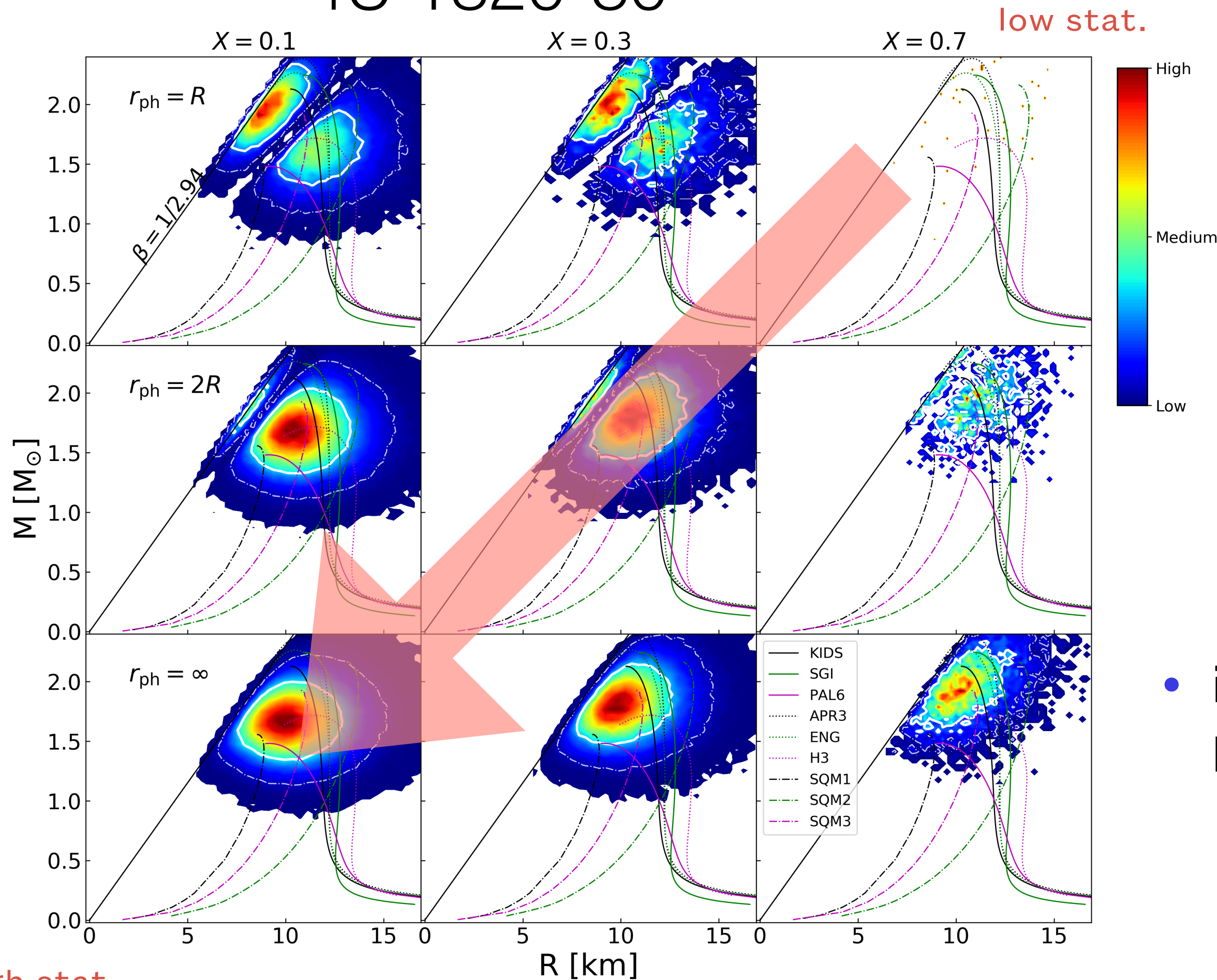
$$M = \beta R c^2 / G$$

- introducing two parameters α, γ then quadratic to quartic eq. of beta
- $h = 2R_{\text{ns}} / r_{\text{ph}}$ ($h = 0 \sim 2$)
- Monte Carlo sampling ($\sim 5,000,000$)



MR credible regions and acceptance rate

4U 1820-30

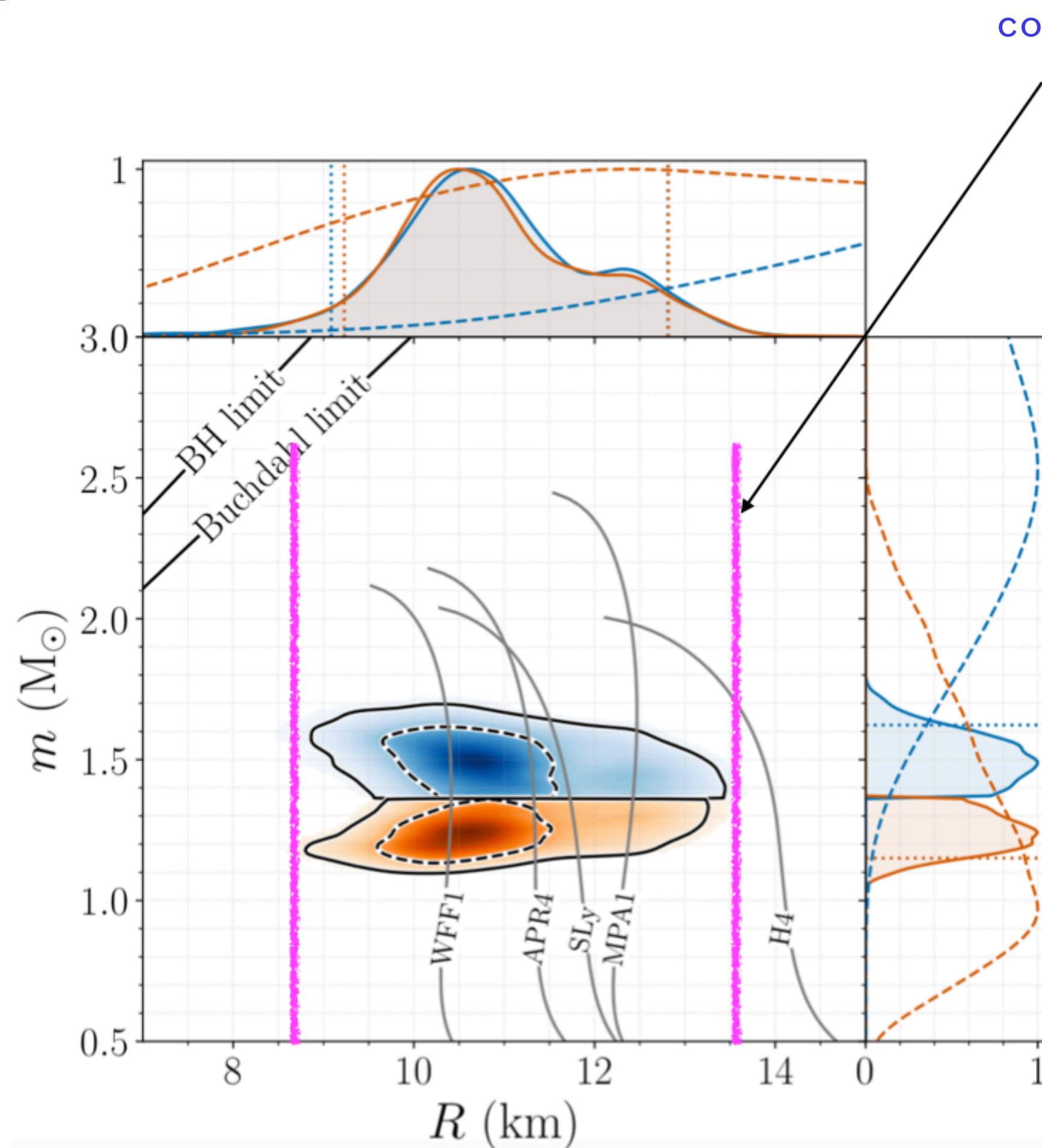


$r_{\text{ph}} = R$	4U 1820-30	$r_{\text{ph}} = 2R$	4U 1820-30	$r_{\text{ph}} = \infty$	4U 1820-30
		hydrogen poor ($X=0.1$)			
Sol.	1.2 (1.0)	Sol.	12.2 (1.1)	Sol.	31.4 (0)
Causality	0 (0.3)	Causality	0 (11.1)	Causality	0 (31.2)
Unphys.	≥ 98.7	Unphys.	87.8 (87.8)	Unphys.	68.6 (68.8)
		intermediate ($X=0.3$)			
Sol.	≤ 0.08	Sol.	1.8 (0.2)	Sol.	7.5 (0)
Causality	0 (0.01)	Causality	0 (1.6)	Causality	0 (7.4)
Unphys.	≥ 99.9	Unphys.	98.2 (98.2)	Unphys.	92.5 (92.6)
		hydrogen rich ($X=0.7$)			
Sol.	0.0	Sol.	≤ 0.05	Sol.	≤ 0.2
Causality	0.0	Causality	≤ 0.05	Causality	≤ 0.2
Unphys.	100.0	Unphys.	≥ 99.9	Unphys.	≥ 99.6

- in Monte Carlo samplings, $h=0$ and hydrogen poor are favored

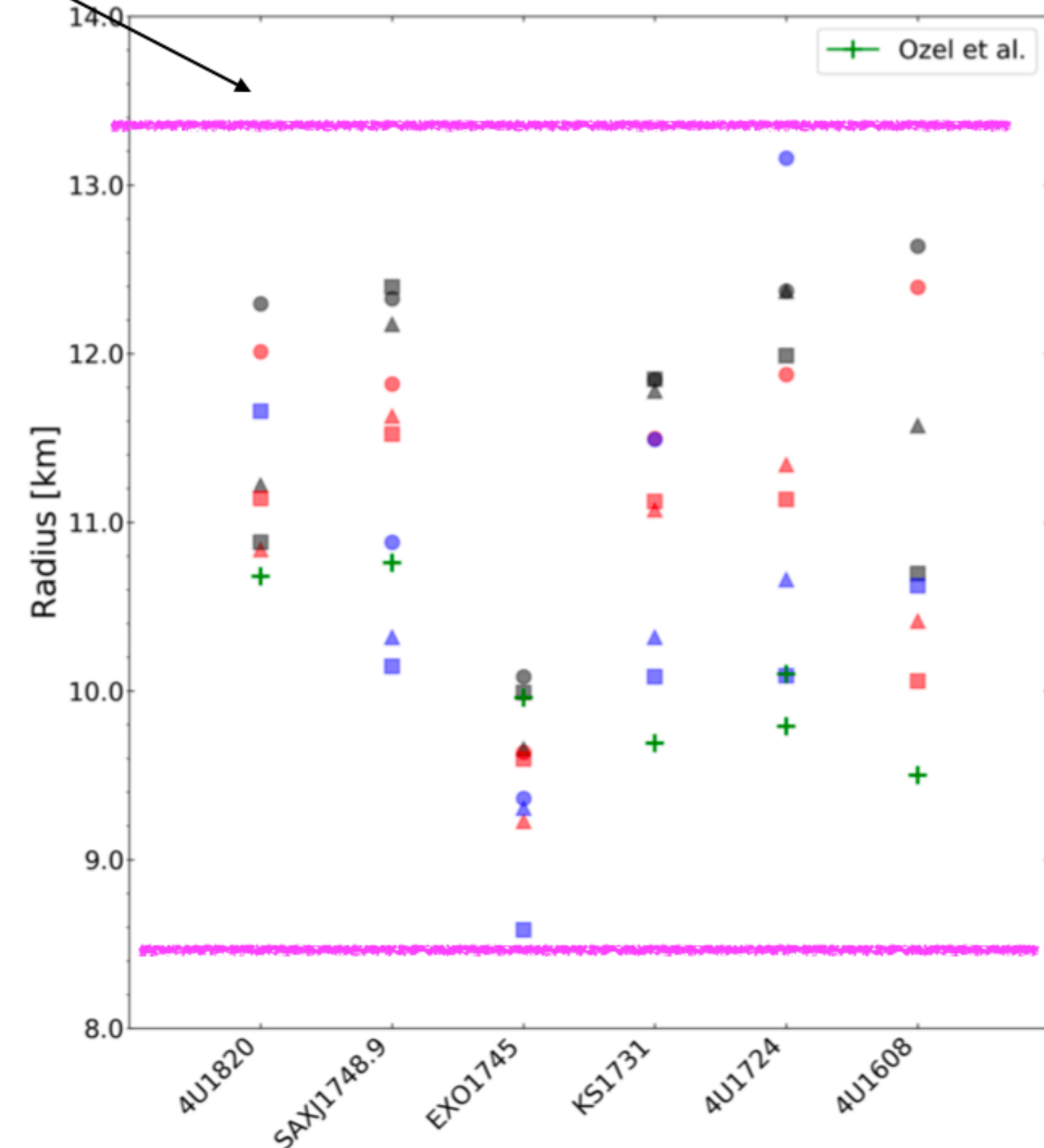
high stat.

Most probable values and GW constraint



Abbott et al. (LSC and Virgo), PRL 121.161101

consistent



M. Kim, Y.-M. Kim et al. (A&A 2021)

Summary

- We developed a new BUU type transport model aiming for LAMPS/RAON experiments
 - We tested DJBUU for elastic reactions and compared with TMEP results for Au+Au collisions, Box-collisions and Box-MF dynamics
 - We expect DJBUU will give hints for symmetry energy by pion-like particle productions
 - We estimated the mass and radius of neutron stars showing PRE in X-ray bursts
 - We can give constraints of EoS by using the MR estimations
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Hulk vs Iron man, Marvel comics

Thank you.
