Sterile neutrino dark matter with dipole interaction

Based on the work with Wonsub Cho, KYChoi, Osamu Seto, in preparation

Kiark Yesing the take: ideas on tabletop experiments for dark matt



Darkness on the table: ideas on tabletop experiments for dark

Darkness on the table: ideas on tabletop experiments for dark matter/exotic particle search

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SM + RH neutrinos + dipole interaction ↓ Dark Matter

Dark Matter









- 3.25% of the present energy density of the universe
- 4. cold (or warm) : non-relativistic to seed the structure formation

Candidates of DM

Strong CP problem : axion

Neutrino sector : sterile neutrino, RH neutrino, Majoron

Technicolor : Techni-baryon, Techni-dilaton

Supersymmetry : neutralino, gravitino, axino, scalar neutrino

Extra dimension : Kaluza-Klein particle

and WIMPzillas, primordial Balck-Hole, dilaton

and more



Standard Model

BOSONS			List of fundamental particles						
Unified Ele	ectroweak s	spin = 1				and in	teract	ions	
Name	Mass GeV/c ²	Electric charge	(н	iggs					
Y photon	0	0		.885					
W	80.39	-1	FERMIONS matter constituents spin = 1/2, 3/2, 5/2,						
W+	80.39	+1	Leptons spin =1/2			Quarks spin = 1/2			
W bosons	91.188	0	Flavor	Mass GeV/c ²	Electric charge	Flavor	Approx. Mass GeV/c ²	Electric charge	
Z boson			VL lightest neutrino*	(0-0.13)×10 ⁻⁹	0	u up	0.002	2/3	
Strong (color) spin =1			e electron	0.000511	-1	d down	0.005	-1/3	
Name	Mass	Electric	𝒴 middle neutrino*	(0.009-0.13)×10 ⁻⁹	0	C charm	1.3	2/3	
	Gev/c ²	cnarge	μ muon	0.106	-1	S strange	0.1	-1/3	
g	0	0	V _H heaviest	(0.04-0.14)×10 ⁻⁹	0	t top	173	2/3	
gluon				1.777	-1	b bottom	4.2	-1/3	

Neutrinos neutral and weakly interacting but massless!

Neutrino Oscillation

Change of flavors with time

For two-body case, $P(\nu_1 \to \nu_2) = |\langle \nu_2(0) | \nu_1(t) \rangle|^2 = \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2 L}{4E}\right)$



Neutrino Oscillation

 $\Delta m_{21}^2 [10^{-5} \text{ eV}^2] = 7.54_{-0.22}^{+0.26} \text{ solar neutrino } \sin^2 \theta_{12} = 0.308 \pm 0.017$ $|\Delta m^2| [10^{-3} \text{ eV}^2] = 2.43 \pm 0.06 \text{ atm. neutrino } \sin^2 \theta_{23} = 0.437_{-0.023}^{+0.033}$ Three masses with two conditions: one is free parameter.

Normal hierarchy

$$m_1 < m_2 < m_3, \quad \Delta m_A^2 = \Delta m_{31}^2 > 0, \quad \Delta m_{\odot}^2 = \Delta m_{21}^2 > 0,$$

 $m_{2(3)} = (m_1^2 + \Delta m_{21(31)}^2)^{1/2}.$

Inverted hierarchy

$$m_3 < m_1 < m_2, \quad \Delta m_A^2 = \Delta m_{32}^2 < 0, \quad \Delta m_\odot^2 = \Delta m_{21}^2 > 0,$$

 $m_2 = (m_3^2 + \Delta m_{23}^2)^{1/2}, \quad m_1 = (m_3^2 + \Delta m_{23}^2 - \Delta m_{21}^2)^{1/2}.$

Neutrino as DM?

The only EM neutral and stable particles, neutrino, was a candidate for hot dark matter.

Neutrinos decouple from a relativistic thermal bath at $T \sim I$ MeV in the early Universe with a relic density today as

$$\Omega_{\nu}h^2 = \frac{\sum_i m_{\nu_i}}{90 \text{ eV}}$$

$$\ll \Omega_{DM} h^2$$

It is too small!

With observational constraints

 $\sum m_{\nu} < 1.3 \,\mathrm{eV} \quad (95\% \, CL) \quad \text{[Komatsu et al., 2011]}$

The fluctuations are damped smaller than the neutrino free streaming scale

 $\lambda_{FS} \sim 20 \left(\frac{30 \text{ eV}}{m_{\nu}} \right) \text{ Mpc}$ It is too hot! top-down structure formation

Tremaine-Gunn bound (1979): minimal mass for fermion DM around 400 MeV due to exclusion principle It is too light!

Neutrinos become massive!

Dirac neutrino

- small Yukawa coupling $\sim 10^{-12}$

See-saw mechanism

- suppressed mass from the heavy Majorana mass

Radiative mass

- massless at classical level, quantum correction generates mass with small couplings

Mass from the interaction with background matter

 massless at vacuum, effective mass generated when interacting with background medium [Choi, Chun, Kim, 2020]

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and more

Neutrino Minimal Standard Model (nuMSM) $(\nu_R)^c \equiv C \overline{\nu_R}^T$

Three RH neutrinos with Majorana mass and Yukawa couplings. After electroweak symmetry breaking, the mass term

$$\frac{1}{2} (\overline{\nu_L} \ \overline{\nu_R^c}) \begin{pmatrix} 0 & m_D \\ m_D^T & M_M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix} + h.c.,$$

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The mass hierarchy $m_D \equiv Fv \ll M_M$ gives mass eigenvalues

: the light active neutrino and heavy sterile neutrino.



$$\Theta = m_D M_{\nu_R}^{-1} \ll 1,$$

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and the light active neutrino mass

$$m_{\nu} \simeq -m_D \frac{1}{M_{\nu_R}} m_D^T = -\Theta M_{\nu_R} \Theta^T.$$
 seesaw mechanism

Interaction of RH Neutrino

RH sterile neutrinos can interaction with SM sector through

- mass mixing after electroweak symmetry breaking
- -Yukawa interaction with Higgs and LH neutrino

The interactions induce

- Decay of sterile neutrino DM: X-ray signal



Sterile Neutrino DM in the nuMSM

To explain the mass-squared difference observed in the neutrino oscillation, only 2 RH neutrino are required. So the 3rd RH neutrino mass can be light and candidate dark matter. [Asaka et al., 2005]



Magnetic Moment of Neutrino

Review [Giunti, Studenikin, 1403.6344] and [Kim, 1911.06883]

Pauli in 1930 Letter

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- as a possible interaction of neutrino

Theoretical study on the neutrino magnetic moment [Kim, Mathur, Okubo, 1974] [Kim, 1976] [Kim, 1978] [Marciano, Sanda, 1977] [Lee, Shrock, 1977] [Fetcov, 1977] [Pal, Wolfenstein, 1982] [Shrock, 1982] [Bilenky, Fetcov, 1987]

> [44] J. Bernstein and T. D. Lee, Phys. Rev. Lett. 11 (1963), 512-516 doi:10.1103/PhysRevLett.11.512

Dirac Neutrino Magnetic Form Factor



At the zero momentum of photon,

()

$$\begin{split} & \mathbb{f}_Q(0) = \mathbb{q}, \quad \mathbb{f}_M(0) = \mathbb{\mu}, \quad \mathbb{f}_E(0) = \mathbb{e}, \quad \mathbb{f}_A(0) = \mathbb{a}, \\ & \text{charge} & \text{magnetic} & \text{electric moment} & \text{anapole moment} \\ & \text{(toroidal dipole moment)} \\ & \text{nly EDM violates CP.} \end{split}$$

Dirac Neutrino Magnetic Form Factor with flavors $\nu(p_i)$ $\nu(p_f)$ $\nu(p_f)$ $\gamma(q)$ $\Lambda_{\mu}^{fi}(q) = \left(\gamma_{\mu} - q_{\mu} \not{q}/q^{2}\right) \left[f_{Q}^{fi}(q^{2}) + f_{A}^{fi}(q^{2})q^{2}\gamma_{5} \right]$ $\gamma(q)$ $- i\sigma_{\mu\nu}q^{\nu} \left[f_{M}^{fi}(q^{2}) + if_{E}^{fi}(q^{2})\gamma_{5} \right], \quad (3.35)$ $f_{\Omega}^{fi} = (f_{\Omega}^{ij})^{*} \quad (\Omega = Q, M, E, A).$

At the zero momentum of photon,

:)

$$\begin{split} \mathbb{f}_Q^{fi}(0) &= \mathbb{q}_{fi}, \ \mathbb{f}_M^{fi}(0) = \mathbb{p}_{fi}, \ \mathbb{f}_E^{fi}(0) = \mathbb{e}_{fi}, \ \mathbb{f}_A^{fi}(0) = \mathbb{a}_{fi}, \\ \\ \begin{array}{c} \text{charge} \end{array} & \begin{array}{c} \text{magnetic} & \text{electric moment} & \text{anapole moment} \\ \end{array} \\ \text{There are diagonal and off-diagonal (transition) types.} \end{split}$$

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CP invariance

$$CP \iff \begin{cases} f_{\Omega} = f_{\Omega}^{T} = f_{\Omega}^{*} & (\Omega = Q, M, A), \\ f_{E} = -f_{E}^{T} = -f_{E}^{*}. \end{cases}$$

Majorana Neutrino Form Factor



charge, magnetic, and electric form factors are antisymmetric and anapole form factors are symmetric.

Majorana neutrinos have only transition dipole moment.

Dipole Moment of RH Neutrinos

We consider [Aparici etal, 0904.3244]

 $\widetilde{\Phi} = \epsilon \Phi^*$ $U(1)_Y$ gauge field B_μ in the SM

$$\mathcal{L}_{\nu_R} = -\frac{1}{2} \overline{\nu_{Ri}^c} M_{\nu_{Rij}} \nu_{Rj} + y_{\nu\alpha i} \overline{L_\alpha} \widetilde{\Phi} \nu_{Ri} + C_{ij} \overline{\nu_{Ri}^c} [\gamma^\mu, \gamma^\nu] \nu_{Rj} B_{\mu\nu} + \text{h.c.}.$$

RH Majorana mass Yukawa coupling

magnetic moment

$$M_{\nu_{R_{ij}}} = \text{diag}(M_{\nu_{R_1}}, M_{\nu_{R_2}}, M_{\nu_{R_3}})$$

 $C_{ij} = \frac{c_{ij}}{\Lambda_5}$ antisymmetric
dim-5 operator from new physics

Collider, astrophysical, cosmological study in [Aparici etal, 0904.3244] We don't consider Dirac dipole operator, since it is dim-6 operator

$$\frac{1}{\Lambda_6^2} \overline{L} \widetilde{\Phi}[\gamma^{\mu}, \gamma^{\nu}] \nu_R B_{\mu\nu} \to \frac{v}{\Lambda_6^2} \overline{\nu}[\gamma^{\mu}, \gamma^{\nu}] \nu_s F_{\mu\nu},$$

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Dipole Moment of RH Neutrino DM

$$\begin{split} \widetilde{\Phi} &= \epsilon \Phi^* \\ \text{We consider [Cho, Choi, Seto, in preparation]}} & \widetilde{\Phi} &= \epsilon \Phi^* \\ & U(1)_Y \text{ gauge field } B_\mu \text{ in the SM}} \\ \mathcal{L}_{i_R} &= -\frac{1}{2} \overline{\nu_{Ri}^c} M_{\nu_{Rij}} \nu_{Rj} + y_{\nu\alpha i} \overline{L_{\alpha}} \widetilde{\Phi} \nu_{Ri} + C_{ij} \overline{\nu_{Ri}^c} [\gamma^\mu, \gamma^\nu] \nu_{Rj} B_{\mu\nu} + \text{h.c..} \\ \text{RH Majorana mass Yukawa coupling}} & \text{magnetic moment} \\ M_{\nu_{Rij}} &= \text{diag}(M_{\nu_{R1}}, M_{\nu_{R2}}, M_{\nu_{R3}}) & C_{ij} &= \frac{c_{ij}}{\Lambda_5} \text{ antisymmetric} \end{split}$$

dim-5 operator from new physics

Collider, astrophysical, cosmological studies in [Aparici etal, 0904.3244]

We don't consider Dirac dipole operator, since it is dim-6 operator

$$\frac{1}{\Lambda_6^2} \overline{L} \widetilde{\Phi}[\gamma^{\mu}, \gamma^{\nu}] \nu_R B_{\mu\nu} \to \frac{v}{\Lambda_6^2} \overline{\nu}[\gamma^{\mu}, \gamma^{\nu}] \nu_s F_{\mu\nu},$$

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Sterile Neutrino DM

To explain the mass-squared difference observed in the neutrino oscillation, only 2 RH neutrino are required. So the 3rd RH neutrino mass can be light and candidate dark matter. [Asaka et al., 2005]

In this case, the lightest active neutrino mass is effectively zero, and the Yukawa coupling can be written as

 $y_{\nu} = \begin{pmatrix} 0 & y_{\nu e 2} & y_{\nu e 3} \\ 0 & y_{\nu \mu 2} & y_{\nu \mu 3} \\ 0 & y_{\nu \tau 2} & y_{\nu \tau 3} \end{pmatrix} \longrightarrow$ DM has no mixing with active neutrinos

with the relation [Casas, Ibarra, 2001]

$$y_{\nu\alpha i}\frac{v}{\sqrt{2}} = iU(m_{\nu}^{\text{diag}})^{1/2}\Omega(M_{\nu_R})^{1/2}, \quad \begin{array}{c} \text{complex orthogonal} \\ \text{matrix} \quad \Omega\Omega^T = 1 \end{array}$$

 $U^{\dagger}m_{\nu}U^{*} = \text{diag}(m_{1}, m_{2}, m_{3}) = m_{\nu}^{\text{diag}}$

To be Dark Matter

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Lifetime is long enough

Amount of present relic density

Other constraints

Lagrangian in the mass eigenstates

$$\mathcal{L}_{\mathrm{DI}} = (c_W F_{\mu\nu} - s_W Z_{\mu\nu}) \left(\overline{\nu_i} (C_V^{\nu\nu} + C_A^{\nu\nu} \gamma_5)_{ij} [\gamma^{\mu}, \gamma^{\nu}] \nu_j + \overline{\nu_i} (C_V^{\nu\nus} + C_A^{\mu\nus} \gamma_5)_{ij} [\gamma^{\mu}, \gamma^{\nu}] \nu_{sj} \right. \\ \left. + \overline{\nu_{si}} (C_V^{\nus\nu} + C_A^{\nus\nu} \gamma_5)_{ij} [\gamma^{\mu}, \gamma^{\nu}] \nu_l + \overline{\nu_{si}} (C_V^{\nus\nus} + C_A^{\nus\nus} \gamma_5)_{ij} [\gamma^{\mu}, \gamma^{\nu}] \nu_{sj} \right) . \\ \left. (C_V^{\nu\nu} + C_A^{\mu\nu} \gamma_5)_{ij} = (U^{\dagger} \Theta)_{ik} C_{kl} (\Theta^T U^*)_{lj} P_L - (U^T \Theta^*)_{ik} C_{kl}^{\dagger} (\Theta^{\dagger} U)_{lj} P_R, \\ \left. (C_V^{\nu\nus} + C_A^{\nu\nus} \gamma_5)_{ij} = (U^{\dagger} \Theta)_{ik} C_{kj} P_L - (U^T \Theta^*)_{ik} C_{kj}^{\dagger} P_R, \\ \left. (C_V^{\nus\nu} + C_A^{\nus\nus} \gamma_5)_{ij} = C_{ik} (\Theta^T U^*)_{kj} P_R - C_{ik}^{\dagger} (\Theta^{\dagger} U)_{kj} P_L, \right] \right. \\ \left. (C_V^{\nus\nus} + C_A^{\nus\nus} \gamma_5)_{ij} = C_{ij} P_R - C_{ij}^{\dagger} P_L, \right]$$

$$C_{ij} = \frac{c_{ij}}{\Lambda_5}$$

Stability of RH neutrino DM

DM has negligible direct mixing with active neutrinos but it can decay through the off-diagonal dipole term and mixing of the heavier sterile neutrinos with active neutrinos.

The decay rate and its lifetime is [Cho, Choi, Seto, in preparation]

$$\begin{split} \Gamma(\nu_s \to \nu \gamma) \simeq &\frac{1}{2\pi} c_W^2 \sum_{i=2}^3 [|C_{Vi1}^{\nu \nu_s}|^2 + |C_{Ai1}^{\nu \nu_s}|^2] m_{\nu_{s1}}^3 \\ \sim &\frac{1}{10^{28} \, \text{sec}} \left(\frac{10^{15} \, \text{GeV}}{\Lambda_5}\right)^2 \left(\frac{|\Theta|}{10^{-6}}\right)^2 \left(\frac{m_{\nu_s}}{1 \, \text{MeV}}\right)^3. \end{split}$$

We require that the lifetime is longer than around 10^{28} sec. It means large scale of new physics, and no constraints or signals from collider or astrophysics.

The lightest RH neutrino DM can produced from the scatterings of the thermal particles through the off-diagonal magnetic dipole interaction. The interaction is very small small, but small amount is produced, which is similar to that of FIMP.

The dominant ones are scatterings mediated by B-bosons

$$\begin{array}{ll} \mbox{t-channel} & f\nu_{sj} \to f\nu_{si} \\ \mbox{s-channel} & f\bar{f} \to \nu_s\nu_{sj} \end{array} \\ \sigma_t \simeq & \frac{N_c (Y_f g_Y)^2 c_{1j}^2 g_f g_{\nu_{sj}}}{2\pi\Lambda_5^2} \left[-2 - (1 + 2m_B^2/s) \log\left(\frac{m_B^2}{s + m_B^2}\right) \right], \\ \sigma_s \simeq & \frac{N_c (Y_f g_Y)^2 c_{1j}^2 g_f g_{\bar{f}}}{12\pi\Lambda_5^2}, \end{array}$$

Thermal Production of very weakly interacting particles

- : the destruction can be ignores since their number density is too small
- Boltzmann equation from

from thermal particles

$$\frac{dn_{\tilde{N}}}{dt} + 3Hn_{\tilde{N}} \simeq \sum_{i,j} \langle \sigma(i+j) \rightarrow \tilde{N} + \cdots \rangle v_{rel} \rangle n_i n_j$$
$$+ \sum_i \langle \Gamma(i) \rightarrow \tilde{N} + \cdots \rangle \rangle n_i,$$

Thermal production from scattering and decay

$$\begin{split} Y_{ij}^{\text{scat}} &= \int_{T_0}^{T_R} dT \frac{\langle \sigma(i+j \to \tilde{N} + \cdots) v_{rel} \rangle n_i n_j}{sHT}, \\ Y_i^{\text{dec}} &= \int_{T_0}^{T_R} dT \frac{\langle \Gamma(i \to \tilde{N} + \cdots) \rangle n_i}{sHT}. \end{split}$$

The abundance of the super-weakly interacting particles from the scatterings are given by

$$Y_{\nu_s}^{TP} = \int_{T_0}^{T_R} \frac{1}{sTH} \langle \sigma v(ij \to \nu_{s1} X) \rangle n_i n_j dT,$$

and the relic density by

$$\Omega_{\nu_s}^{\rm TP} h^2 = \frac{m_{\nu_s}}{\rho_{\rm crit}/s_0} Y_{\nu_s}^{TP} \simeq 0.28 \left(\frac{m_{\nu_s}}{1\,{\rm MeV}}\right) \left(\frac{Y_{\nu_s}^{TP}}{10^{-6}}\right),$$

$$s_0 = \frac{2\pi^2}{45} \times 3.91 \times T_0^3 \qquad (\rho_{\rm crit}/s_0)^{-1} = 2.8 \times 10^8 / {\rm GeV}$$

 $\rho_{\rm crit} = 3M_P^2 H_0^2$





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The lightest RH neutrino DM is produced from the decay of the heavier RH neutrinos

$$\Omega_{\nu_s}^{\text{NTP}} h^2 = \frac{m_s s_0}{\rho_{\text{crit}}} \sum_{i=2,3} \text{Br}(\nu_{sj} \to \gamma \nu_s) \times Y_{\nu_{sj}}^{dec},$$
$$\simeq 2 \times 10^{-9} \left(\frac{m_s}{1 \text{ MeV}}\right) \left(\frac{1 \text{ GeV}}{m_{sj}}\right) \left(\frac{10^{16} \text{ GeV}}{\Lambda_5}\right)^2 \left(\frac{6 \times 10^{-9}}{\sum_{\alpha} |\Theta_{\alpha j}|^2}\right)$$

It is much suppressed compared to that from thermal production.

Constraints from BBN

[Atre etal, 0901.3589]

The decay of the heavier RH neutrinos produce EM, hadronic and then affect the Big Bang Nucleosynthesis.



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Summary

• Neutrino mass and dark matter



- Production of RH neutrino dark matter
 - : thermal (scattering) + non-thermal
 - 10 keV 100 MeV mass cold dark matter, with GUT scale new physics
 - Reheating temperature around 10¹⁰ GeV
 - No constraint from the structure formation
 - Constraint and possible signal from X-ray or Gamma-ray

Thank You!